# DESIGN OF A 120 MWt REACTOR FOR A SURFACE WARSHIP

By
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CLEAR ENGINEERING AND TECHNOLOGY PROGRAMME

AN INSTITUTE OF TECHNOLOGY KANPUR AUGUST, 1984

# DESIGN OF A 120 MWt REACTOR FOR A SURFACE WARSHIP

A Thesis Submitted in Partial Fulfilment of the Requirements for the Degree of

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Ву

Lt. ARUN J. RAO, IN

to the

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AUGUST, 1984

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# To My dear Father and Mother, My best teachers



#### CERTIFICATE

This is to certify that the work "DESIGN

OF A 120 MWt REACTOR FOR A SURFACE WARSHIP", has been

carried out by Lt. Arun J Rao, IN under our supervision

and that it has not been submitted elsewhere for a degree.

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#### SYNOPS15

DESIGN OF A 120 MWt REACTOR FOR A SURFACE WARSHIP by

LT. ARUN J. RAO, IN

Never before has the strategy of maritime warfare diversified so much as with the ingress of the nuclear reactor onto warships. Subsurface or surface, the nuclear propelled warships are far superior both tactically and in performance over their conventional counterparts. With the fast dwindling number of warships due to their esclating costs, the possession of nuclear-powered warships for maintaining the same effectiveness and punch is becoming increasingly inescapable.

Reactor design is a multi-dimensional complex problem embracing many fields of engineering. The warship reactor design is more intricate than the land-based ones at it involves certain additional specialized problems like ship-motion effects, manoeuvring, vibrations, etc. The physical parameters of the core is restricted mostly by thermal considerations. Hence the Thermal hydraulic design requires careful attention to prevent core melt-down or coolant bulk-boiling. The Reactor physics design involves evolution of core enrichment and certain

other parameters to result in optimal design. Knowledge of the neutron flux distribution is also required. Here, two-group theory for heterogeneous core lattices has been used. The Shielding design involves meticulous calculations to produce the smallest possible reactor shield, both in size and weight which is of paramount concern in a warship design.

Control of a marine reactor is different from the land-based ones. Due to stringent manoeuvring requirements, Power excursions from 20% to full-load require automatic control with a high power increment/decrement rate of 3%. The system has to be prompt acting, stable at all times of operation with no unallowable overshoots. Finally, when the reactor goes on the ship, certain other problems like ship-motion effects, vibrations, etc., come in.

Due to the immense calculations involved, any modern reactor design process is impossible without the aid of a digital computer. Here, 3 computer CODES have been developed, one each for thermal hydraulic, Reactor physics and Shielding designs. The CODES & their results have been presented separately.

The different design processes discussed till now are inherently interactive among themselves and cannot be considered isolatedly. This has been highlighted in the early part of the thesis. It has, however, been the earnest endeavour of the author to ensure an overall non-conflicting design.

\* \* \* \* \* \*

Works.

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I am indebted to my dear parents, brother Anand and sister Revathi for the deep inspiration they instilled in me towards the successful completion of this work.

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# CONTENTS

Chapter			Page
		LIST OF TABLES	<b>%</b> :
		LIST OF FIGURES	xi
		NOMENCLATURE	хіі
1		INTRODUCTION	
	1.1	Scope of the thesis	2
	1.2	Literature Review	3
	1.3	Thesis Abstract	6
2		MARINE ASPECTS OF NUCLEAR REACTORS	
	2.1	History of the Reactor at sea	11
	2.2	Tactical Aspects of Nuclear Warships	16
	2.3	Salient Features of Marine Reactors	23
3		REACTOR DESIGN PROCESS	
	3.1	Choice of Reactor	29
	3.2	PWR Design Scheme	31
	3.3	Fuel Assembly Design	33
	3_4	Steam Cycle used .	37
	3.5	Inference	37

<u>Chapter</u>			Page
4		CORE THERMAL DESIGN	
	4.1	Introduction	<b>3</b> 9
	4.2	Design Characteristics	41
	4.3	Thermal & Hydraulic Design	47
	4.4	Results & comments	59
5		REACTOR PHYSICS DESIGN	
	5.1	Introduction	62
	5.2	Criticality of the Reactor	64
	5.3	Flux Distribution	77
	5.4	Results	86
6		REACTOR SHILLDING DESIGN	
6	-1	Introduction	88
6	.2	Salient Features	93
6	.3	Radiation Attenuation in Shield	96
6	. 4	Comments 1	.16

Chapter		Page
7	REACTOR CONTROL DESIGN	
	7.1 Reactivity Computations	118
	7.2 Reactor Control Systems	127
	7.3 Stability Analysis	131
	7.4 Results and Comments	138
8	REACTOR ON SHIP	
	8.1 Ship's Motion Effects	140
	8.2 Collision Barrier & Grounding Protection	142
	8.3 Miscellaneous Features	143
9	CONCLUSION	
	9.1 Summary	145
	9.2 Suggestions for further study	147
	BIBLIOGRAPHY	150
•	APPENDIX .	154
	COMPUTER PRINT-OUTS	172

4

# LIST OF TABLES

<u>Table</u>		Page
2.1	World's Nuclear Fleet	22
2.2	Comparison between Marine	
	and Land-based Reactors	23
6.2	Optimal Shield Designed	95
6.3	Core Gammas	108
6.4	Fluxes for unit tissue dose-rates	112
7.1	Reactivity Coefficients of Fuel & Moderator	124
7.2	Core Reactivity Balance	126
7.3	2-Temperature Feedback Parameters	134
7.4	Boiler Transfer Function Parameters	137
9.1	Overall Design Characteristics	145

# LIST O.' FIGURES

Figure		Page
3.1	Reactor Design Interactions	32
3.2	The Fuel Assembly	34
3.3	The Core Configuration	34
3.4	PWR Steam Cycle (Schematic)	36
4.1	Core Flux Functions used	42
5.1	Core Neutron Cycle	63
5.2	Core-reflector configuration	79
5.3	Radial Flux Distribution	85
6.1	Thermal Snield in PWR	92
6.3	Primary and secondary Radiations from	
	Core	97
6.4	Neutron Flux Distribution	113- -114
6.5	Gamma-ray Cross-section for Iron	106
7.1	Reactor Control System (Schematic)	128
7.2	Nyquist Plotoof 2-Temperature Feeaback	135
7.3	Bode Plot of Boiler Transfer Function	138

#### NOMENCLATURE

#### MAIN SCRIPTS :-

- A Area: Mass number of elements
- B Buckling
- C Specific heat of material
- D Diffusion constant
- E Neutron Energy
- F Hot channel Factor
- f Friction factor: Thermal utilization factor
- g Non-1/v factor for Maxwellian Distribution; Acceleration due to gravity.
- H Height (of fuel rod )
- h Heat Transfer Coefficient
- I Resonance Integral; I<sup>135</sup> concentration
- K Thermal Conductivity
- k Multiplication constant
- L Diffusion Length; Non-leakage Probability
- Neutron life-time (Thermal)
- m Coolant mass flow rate
- N Number density of perticles
- Nu Nusselt's number
- P Pressure; Promethium concentration

```
Resonance escape probability
p
             Prandtl number
Pr
             Heat flux/intensity
q
R
          - Core radius
Re
             Renault's number
             Coupling coefficient; Source Strength;
S
             Samarium concentration
             Fuel-rod pitch
s
Т
             Temperature
             Volume
             Coolant velocity through core
Х
             Xenon concentration
             Fission Yield
Y
ß
             One group neutron percursor fraction
ε
             Surface roughness factor; Fast fission factor
          - \eta of the fuel
η
λ
             Decay constant
             Viscosity of coolant
μ
             Neutrons released per fission
             Logorithmic Energy decrement of neutrons
             Density
\Sigma
             Macroscopic neutron cross-section
σ
             Microscopic neutron cross-section
τ
             Neutron age; Time constant
```

Neutron flux

φ

#### SUBSCRIPTS:-

Core parameter

2 - Reflector parameter

 $25.28 - U^{235}, U^{238}$ 

a - Absorption

av - Average

ac - Average coolant

B - Bulk coolant

circ - For smooth circular tubes

cl - Cladding

e - Extrapolotion distance

eff - Effective

F - Fuel-rod parameter; Fast neutron

fp - Fission product

fu - Fuel rod parameter

f - Fission

inf - Infinity

M,m - Moderator

o - Initial value; at core centre

P - Poison; Promethium

r - Removal

S - Samarium

s - Scattering; cladding parameter

Sat - At Saturation level

ss - Stainless steel

T - Thermal

t - Total

Tr - Transport

X - Xenon

# CHAPTER - I.

R	E.	S	U	M	E

# INTRODUCTION

- 1.1 SCOPE OF THE THESIS
  - 1.2. LITERATURE REVIEW
    - 1.3 THESIS ABSTRACT

#### INTRODUCTION

In the modern era of fast depleting oil, coal and other forms of fossil fuels, nuclear energy takes a leading seat as the future global energy source. The nuclear reactor is virtually an interminable source of energy. Tapping of this energy is an engineering feat by itself. Though marginally more expensive, it is only a matter of time in this energy-crisised world before the reactor establishes itself as an inevitable source of energy. All this, and it is a mere 42 years old!

Today the cost of a nuclear reactor is prohibitive. Why then nuclear propulsion? The answer is straightforward - No repeated refuelling for the ship; which opens an entirely new era at sea! Where economic consideration is counterbalanced by military requirement, nuclear propulsion for Naval ships become essential. For the merchant ships, however, this is not so, as money is the key factor for trade. Consequently, we have only a handful of Nuclear merchant ships whereas the number of naval ships in the world (with nuclear propulsion) exceed three hundred.

A compact low weight system is of paramount importance in plants designed for ship propulsion. Marine

reactor design by itself, is a very vast topic merging land-based reactor design with certain specialized aspects like marine environment, light weight, limited space, etc. Our goal is to design a reactor system for a frigate/destroyer class warship. A drawing board design involves a vast amount of data, time and generation of numerous highly essential computer codes. This is definitely not being attempted. In the following pages, certain basic aspects of marine reactors have been discussed and a skeletal design attempted to highlight the varied & complex problem of marine reactor design. It is beyond the scope of this thesis to cover all topics envolving the design, be the skeletal stage itself. All important aspects have, however, been covered.

#### LITERATURE REVIEW

Most of the information regarding Naval reactors is classified. Though information on reactors of merchant ships are easily available, they don't satisfy the stringent measures of manoe Krability, high power-to-weight ratio and the limited space available in a warship where economic considerations fall into the background. Yet, a fair idea on problems encountered in marine reactor design, is available from them. International symposiums on Nuclear ships have been held in (1960), Hamburg (1971) and Madrid (1972).

A subcommittee on military applications of the U.S. has presented the tactical and effective use of Nuclear Propulsion for Naval Warships (4) It argues that though economically dear, when faced with the threat of submarines armed with either torpedoes or cruise missiles, or bombers or surface ships armed with cruise missles, the all-nuclear task force (consisting of an aircraft carrier and a few destroyers/frigates, all nuclear-powered) is less vulnerable to attack than a task force of conventional ships. The committee concludes, nuclear frigates for independent missions are far superior in performance than their conventional counterparts. John R Lamarsh (16) states that submarine reactors, being very small and compact, use fuel enriched in y to over 90 w% A.M. Petrosy ants (3) educidating problems of nuclear science & technology, discusses Russian ships with nuclear engines - 'Lenin' & 'Arktika' (both ice-breakers) & their vastly superior performances over diesel icebreakers.

Extensive study & analysis of the world's first nuclear-propelled merchant ship 'Savannah' (5), in its sea environment, has thrown light over the problems faced by Marine reactors. Analysis of its core performance has been done by WJ Gallagher and Kaiz (1). The Japanese Nuclear ship 'Mutsu' has also been discussed in detail by S. Sasaki (6). Off-late, L. Chinaglia (2) of Fiat, Italy has presented a new design of

a PWR for ship propulsion. The inherent design interactions among various design aspects like thermal hydraulic design, nuclear design, shielding design, etc. has been well illustrated: by RA Knief (13).

El-Vakil (17) deals with PWR thermal hydraulic design. Weisman (26) describes at length the various hot-spot factors concerning the thermal design. Regarding reactor physics analysis, Meem (22), with his 2-gp theory, gives sample calculations for reactor designers, that has been extensively referred. The Nuclear Engineering handbook (21) by Etherington has been used for related figures & references as and when mentioned. IAEA reports: Vienna, 1964 (27), highlight the reactor shielding design and problem. B. Chinaglia (28) of Fiat, Italy, has also worked on shielding studies & control of ship-based gaseous activity release.

J. Brown & A. Jackson (29) have carried out a study on shielding of Marine reactor installations. S.J. Thunell (30) has presented a comparative study on neutron fluxes in a metal-water shield in merchant ship reactors.

A Marine Reactor control & in-core instrumentation system design has been done by F. Basile, R.Merino & G. Selvaca. wherein they have pointed out the differences between land+based reactor & marine reactor control. The control scheme used in the thesis is one evolved by Chinaglia (2) of Italy.

A detailed treatment of controllers has been illustrated by MA Schults (33); this has been used, nowever, after a study of non-linear control system. References for other aspects on reactor control have been Lewins (34) and Glasstone & Sesonoke (12) and D.L. Hetrick (36).

Specialized marine problems like ship-motion effects on steam-generator performance, collision barrier. & grounding protection barrier for ships-reactors, and safety of crew have been studied, respectively, by V. Jecob and G. Selveggi<sup>(37)</sup>, W. Jager & H. Lettnin <sup>(38)</sup> and L. Chinaglia & P. Rucci<sup>(32)</sup>.

# 1.3 THESIS ABSTRACT

The thesis starts with a brief history of marine reactors. The tactical aspect of nuclear-powered vessels over their conventional counterparts is discussed—this may make the difference between winning or losing a battle which is vital for any fighting force. The salient features of ship-board reactors over the land-based ones are discussed. The modern trends of marine reactors are also elucidated.

Chapter 3 highlights the design process. The different aspects of reactor design like thermal hydraulic design, nuclear design, shielding design, etc. are inherently interactive among themselves and hence cannot be independently considered; this is highlighted. A reactor core configuration.

is then evolved and the systems used mentioned.

Core thermal hydraulic design is developed in chapter 4. A linear power rating of 11.0 KW/m is used. Since the power generated by a reactor is essentially restricted by the effective heat removal, this portion of the design is carefully considered as we desire the most compact and light-weight reactor for ship-board installation. A computer CODE, so vital for any thermal analysis, has been developed and used to arrive at optimum reactor Parameters. With this knowledge, we next move over to the reactor physics design (chapter 5). Two-group theory is used and the core studied for criticality using 2 regions (water as reflector). A computer CODE has been evolved which computes the effective multiplication constant  $(K_{col})$ , the fast and thermal flux.es in both the regions, as well as the various 'poison' (unwanted neutron absorbants) activities in the core. The amount of control poison required for reactor control is also evolved. The control design hence would chiefly depend on the parameters obtained in this chapter. Care has been taken in the CODE that temperature and pressure dependencies of all parameters are considered.

We are aware that the overall reactor weight and size has to be the minimum possible for a marine reactor.

Bulk of this weight, however, is taken up by the biological shields. Consequently, reactor shielding assumes considerable importance and is analyzed at length in chapter-6. Biological shielding is mainly required for the fast neutron and gamma fluxes emerging from the shield materials due to thermal neutron capture. The biological dose rate from the secondary shielding is to be restricted to 0.75 mrem/hr. This has been achieved after the formulation of a shielding CODE. In addition an approximate weight calculation of the reactor (with shield materials) is demonstrated.

The control of a marine reactor is greatly different from a land-besed one. This is because of high manoeuvring demands and a requirement of controlling the reactor automatically from full-load to part-load (20%). Chapter-7 elaborates these aspects and evolves a reactor control system. Careful stability analysis is also done from full-load to part-load using a two temperature feedback for the reactor. Certain other aspects of stability are also attempted after the calculation of the temperature coefficients of reactivity as applicable. A reactivity balance of the core using the CODE of chapter 5 is displayed. The control policy used is elucidated subsequently.

The integrated aspect of the reactor with the ship increases the design complexity further. Its effects are of practical significance to the operator on-board. Chapter-8 embellishes this integrated view. The ships three dimensional motion at sea has its effects on the steam generator performance. Collision barrier and grounding protection structure is required for the reactor compartment.

Chapter-9 concludes the present work illustrating the design that is ultimately arrived at. Other aspects of marine reactor design beyond the scope of this thesis are mentioned and suggestions for further study given. All references made in the current task are listed in the bibliography.

\* \* \* \* \*

### CHAPTER - II

#### MARINE LSPECTS

OF

#### NUCLEAR REACTORS

#### Resume

- 2.1 History of the nuclear reactor at sea in :-
  - 2.1.1 Merchant Ships
  - 2.1.2 Warships
  - 2.1.3 Future trends of marine reactors
- 2.2 Tactical aspects of nuclear warships :-
  - 2.2.1 Drawbacks of conventional ships
  - 2.2.2 Nuclear submarines
  - 2.2.3 Nuclear surface ships- the importance of all nuclear task force
  - 2.2.4 Nuclear Propulsion for frigates
  - 2.2.5 Nuclear fleet strength of the world Navies
- 2.3 Salient Features of Marine Reactors:-
  - 2.3.1 Comparison with land-based reactors
  - 2.3.2 Basic design & safety criteria for warships

In 1942, Fermi & his co-workers made the world's first reactor critical at the University of Chicago. However, not until 1957 was a propulsion unit designed to operate on nuclear fuel. It was a small highly-enriched Pressurized Water Reactor (PWR), installed on board the Submarine USS NAUTILUS. As of today, there are over 300 ships propelled by nuclear energy. Most of these, however, are warships where economy is not the deciding factor in the choice of propulsion system.

#### 2.1 BRIEF HISTORY

#### 2.1.1 NUCLEAR MERCHANT SHIPS

The history of nuclear merchant vessels have never been bright. Nuclear power in merchant ships was used for the first time on a 16,000 ton Russian ice-breaker 'LENIN' in 1960. The decision was based not on economy but efficiency over the prevailing diesel electric system. In Arctic areas of heavy ice, nuclear ice-breakers with a 50% higher specific capacity\*, can operate most of the year; but the conventional ones can make way only for 3-summer months due to danger of running out of fuel. The second ship was 'SAVANNAH', a U.S. Cargo-liner commissioned in dec '62 (no longer in active service). It's purpose was to test safety of nuclear plant aboardship & entrance of nuclear

<sup>\*</sup> Specific capacity - power-to-displacement ratio.

vessels to civilian ports.

The 'OTTOHAHN' of FRG is a small scale experimental ship not planned for profitable operation (1968 virtage).

Her purpose is to furnish all types of information theoritical, practical, economic & scientific with regards to nuclear propelled merchant ships at sea & refute arguments about their safety. The Japanese, on similar lines as FRG, launched a 10,400 ton specialized nuclear cargo ship in 1970 (MUTSU).

Russia, finding the need for a second nuclear ice-breaker commissioned 'ARKTIKA' (displacement 23,460 tons) in 1975.

The reason for this bleak growth of nuclear ships are plain:-

- (i) Cost economy Capital cost of nuclear ships are 60%
  higher than conventional. The fuel cost
  is also higher. Till such time fossil fuel
  becomes prohibitive enough to counterbalance the above two reasons, nuclear
  ships will not be easily accepted.
- (ii) Uncertainties-of investment cost; the future development in this area is hardly predictable.
- (iii)Safety problems- Nuclear ships are not easily accepted

  by most of the civilian ports; psychological

  fear of public is mainly responsible for

  this.

#### 2.1.2 NUCLEAR WARSHIPS

Nuclear Energy took birth in warships in the form of a submarine reactor for 'NAUTILUS', a U.S. Submarine, on 17 Jan '55. She generated 15,000 SHP, having 2 shafts and displacing 4040 tons. Initially she steamed submerged from Key West, Florida, to New London, a distance of 1397 sea miles. She was refuelled after 2 years and 62,562 miles of steaming. Her success gave rise to a 'gold rush' and the US Navy ordered a pack of submarine reactors from Westinghouse Corporation. In 1960, Russia started her submarine fleet.

'ENTERPRISE', a 89,60C' tons US Attack carrier, was the first surface ship to have nuclear propulsion (in 1961).

She has 8 PWRs on 4 shafts, giving her a power of 280,000 SHP and a maximum speed of 35 knots\*\*. She has had her core changed thrice, with the present feed giving her a sustainence of 10 to 13 years. In 1962, 'BAINBRIDGE', a U.S. Nuclear-Powered Guided Missile cruiser was the first cruiser to be nuclear-propelled (displacement 8580 tons).

Changes in ship reactor technology have also been incorporated to make ships more versatile and independent. The newer US aircraft carrier 'NIMITZ' (launched in 1975) has only 2 reactors contrary to her predecessor.

'ENTERPRISE' with 8: this generates a power of 260,000 SHP or 4 shafts, giving her 93,400 tons a maximum speed of 35 knot. She is the largest warship ever...

<sup>\* 1</sup> sea mile (or nautical mile) = 1.83 kms (2000 yarda) .
\*\* 1 know = 1 nautical mile/hour.

built. She can steam an estimated 800,000 to 1 million miles before refuelling. Interestingly, the energy equivalent of her cores is 462 mega gallons (1.60 million tons) of fuel oil—this is where nuclear energy scores over the conventional form.

The largest submarine ever built, however, is a Russian one, a 'typhoon' class Ballastic Missile submarine (SSBN), launched in 1980. She displaces 30,000 tons dived with speed exceeding 24 knots and having 2 nuclear reactors, one per shaft, supplying a total of 120,000 SHP; she carries 20 SLBMs ( Submarine Launched Ballistic Missiles). Presently, nuclear submarines far outnumber nuclear surface ships. However, many surface ships both cruisers and destroyers are increasingly becoming nuclear-propelled, mainly due to tactical reasons.

Due to the prohibitive cost & superior technology for marine reactors, nuclear warships are expensive toys handled only by a few economically advanced countries. However with the Indian Ocean swarming with subsurface & surface, nuclear & conventional warships, possession of nuclear warships to effectively safeguard our exclusive economic zone & sea-frontiers, is becoming increasingly inescapable.

#### 2.1.3 FUTURE TRENDS

For merchant ships greater than 70,000 tons (23) displacement, preliminary studies indicate nuclear Power to so re over conventional power when operated for long durations. This might be used for constructing huge nuclear container ships in future when nuclear energy gets accepted in the merchant marine field. The smallest nuclear ship ever built is a US nuclear -powered ocean engineering & research vehicle 'NR-1' (1969), a submersible, built by USAEC', Knolls' Atomic Power laboratory. The vessel displaces only 400 tons, having dimensions of 136.4 x 12.4 x 14.6 with 2 propellors & carrying 5 crew members and 2 scientists. Such vessels are very useful for conducting detailed undisturbed experimentation on the continental shelf over long durations.

Now we hear the concept of NUFIS - Nuclear Floating Island, brought forward by Japanese scientists. Because of small area & dense population, the siting of Nuclear Power Plants in Japan is limited. Hence, the feasibility of NUFIS has been studied and the project is about to commence. It is to be located 20 kms offshore at a sea-depth of 150 m. It is to have a 1200 MWe PWR Plant on a 140 m x 140 m floating platform with a displacement of 298,000 tons. The power plant & the associated facilities are to be situated

on it. Hence, the marine reactor technology will have to be applied to it. The technological feasibility of a floating centre for fuel fabrication, reprocessing, etc., is also being thought 1.

#### 2.2 TACTICAL ASPECTS OF NUCLEAR WARSHIPS

It was stated that the elimination of repeated refuelling opens an entirely new era at sea. Let us explore the tactical boost this gives.

Nuclear propulsion enables warships to traverse across seas at high speeds without parsing to refuel and without replemishment. With the escalating cost of warships, many many times that of equivalent merchant ships, the number of warships in the fleet is bound to dwindle. Hence, nuclear propulsion becomes prominent to maintain the same effectiveness with lesser warships. With the fast depleting oil sources, in future, nuclear propulsion is going to become a necessity. It gives an additional tactical flexibility and opens new courses of action to the operators of the Naval.

Forces which would otherwise be unavailable. A nuclear productive results in any operation; such a force would be, in addition, less vulnerable to the action of the enemy.

#### 2.2.1 DRAWBACKS OF CONVENTIONAL SHIPS

Here, mobility is limited by the need for refuelling at sea. Enemy action, bad weather & other uncontrollable forces directly impact upon refuelling ability which is not only time consuming but also requires the services of a considerable oil tanker fleet/train. The Fuel oil carried by ships being inflammable, in addition, poses a fire hazard onboard. A nuclear fleet, contrarily, is freed from the constraints of tankers & base support; hence it has increased speed, reliability, range, less fuel requirements & more payload.

#### 2.2.2 NUCLEAR SUBMARINES

In the modern warfield, no other weapon has proved to be such an imminent threat as the nuclear submarine. As we see from Table 2.1, the super powers have maintained a parity on the number of nuclear submarines. Admiral Moorer of US Navy has stated (4) that he would rather have one nuclear powered, tactical cruise missile submarine (55BN) than 5 of its conventional counterparts. Submarines are a particular threat because of their potential for approaching to within weapon ranges without being detected.

When their batteries run down, diesel submarines have to periodically 'snort'. The quantity of fuel they carry

<sup>\*</sup>Snort'- come up to near sea-surface level to to run diesel engines for charging batteries that are used for propulsion underwater.

limit their edurance. The nuclear submarines, ostensibly, never require to surface and can continuously move at high speeds of 20-30 knots (almost double of diesel submarines). The modern nuclear submarine being more quieter\*, have a high probability of going undetected by enemy sonars. Hence, they are much more effective in penetrating anti-submarine defences than diesel submarines.

#### 2.2.3 SURFACE SHIPS - THE ALL NUCLEAR TASK FORCE

A naval task force consists of an aircraft carrier with her modern air-wing, and her escorts of 3 to 4 destroyers/frigates to provide additional protection against surface, sub-surface and air threats. The capability and punch of the force is restricted by the endurance of each of its ships. Hence, for maximum effectiveness, all ships in it have to be nuclear-propelled. When faced with the threat of submarines either armed with torpedoes or cruise missiles, or bombers, or surface ships armed with cruise missiles, the all-nuclear task force is less vulnerable to attack than a task force of conventional ships which must show down to refuel in an extended encounter. It is therefore much more difficult for the submarine to get in a favourable position to attack the all-nuclear force. Further, the logistic support forces upon which the conventional striking forces are more dependent, are even more vulnerable to attack that

<sup>\* &#</sup>x27;quieter' - Vibrations of hull due to inner machinery is of lesser magnitude, making passive underwater detection more difficult.

warship..

	The tactical advantages of nuclear propulsion for
ships	of a nuclear task force can hence be summed up as
wcllct	S:=
**************************************	They can move where required at top speeds without
	establishing logistic support before departure.
	Their virtually unlimited range enables them to use
	their superior speed to arrive at crisised situation
	much earlier than their conventional counterparts.
	When they do get there in a less vulnerable condition,
	they have far greater staying power, not only in terms
	of their ability to stick on without fuel, but also,
	significantly, in terms of aviation fuel & eviation
	ordanance for their airwing. For example, USS
	'NIMITZ' has 50% more aviation ordinance & twice as
	much jet fuel than equivalent conventional carriers.
***************************************	It can continue combat operation without support
	until aircraft fuel, ammunition, food or other
	supplies are exhausted.
	It can disengage if required to retire at top speed
	to less vulnerable sources of aircraft fuel & ammunition
	replenishment.

#### 2.2.4 NUCLEAR PROPULSION FOR FRIGATES

By virtue of possesing their capability for high sustained speeds and uninhibited endurance, nuclear frigates are uniquely suited for assignment to independent tasks with an effectiveness no non-nuclear ship can match. This can mean difference between winning or losing engagements. In independent operations, it matches the endurance of any nuclear submarine. Since the aim of the thesis is design of a reactor for frigate / destroyer, let us explore its tactical aspects a bit deeper.

Nuclear frigates combine the essentially unlimited endurance of nuclear propulsion with the capabilities of the most modern anti-air and anti-submarine weapon systems. Their nuclear propulsion results in major improvements in offensive & defensive capabilities:-

- ---- greater attack effectiveness due to increased mobility
  & freedom of independent action; ability to transit at
  high-speeds and thus arrive in attack position earlier
  & ready to conduct operations immediately without pausing
  to refuel; ability to be on attack station a higher
  percentage of time; the freedom to extend attack to
  larger areas.
  - --- reduce vulnerability due to freedom from dependence upon replenishment in compat areas; and ability to avoid submarine attack by transiting at high speed & using evagive transit routes.
- --- significantly reduced need for sea-based & land-based logistic support forces.

- --- increased propulsion plant reliability due to the higher standards required in the design & construction of nuclear propulsion plants.
- ----increased overall effectiveness of the entire fleet by reducing the total number of combatant ships required to protect oilers.

### 2.2.5 WORLD'S NUCLEAR FLEET STRENGTH

Table 2.1 lists the nuclear strength of the world navies as of today. Though nuclear submarines for outnumber nuclear surface ships, we can see that the numbers of the latter has more than tripled in the last 10 years and many are being built.

TABLE 2.1

WORLD'S NUCLEAR FLEET

		- 1	17	8 8 11	a d	U.S.	A.	U.K.		FRANCE	CE	CHINA	3
S.No.	S.No. TYPE	OF WARSHIP		1972	1982	1972	1982.	1972	1982	1972	1982	1972	1982
-	A. SUBI	A. SUBMARINES							•	``	•		
<del>-</del>	SSBN () tactic Missil	SSBN (Nuclear Powered tactical Ballastic Missile Submarine)	red	35	69	41	37+7*+2	4	ተ ተ *	<b>ન</b>	•		1
3	SSGN ( Nuc tactical g Submarine)	ssGN (Nuclear powered 40 tactical guided Missile Submarine)	ered ssil	40 e	49+1*	1	ı	ľ	<b>t</b> ,	1	1		1
<u>.</u> .	SSN (Nattack	SSN (Nuclear powered attack submarine)	eq eq	25	58+3*+8	,+8 56	85+18* +3+5	4.	11	, 	1	<b>!</b>	7
_	TOTAL			100	188	97	157	ω	6	<b>н</b> .		I	2
Tota Subm	Total of No. Supmarines:	Total of Non-nuclear Supmarines:		243	293	41	47	26	96	19	ا مور مور	20	
,	B. SUR	B. SURFACE WARSHIPS	വ		,	· ·	(	***************************************		_	_		
<u>.</u>	CVN (N Aircra	CVN (Nuclear Powered Aircraft Carrler)	 p.		<b>н</b>	rd	×2+5	I	1	1	<b>!</b>	ı	ı
<u>.</u>	CGN (N Missil	CGN (Nuclear Powered Missile Cruisers)	eq		* + + + + + + + + + + + + + + + + + + +	ო	ön \	1	1	ľ		1	ı
ſ.,		TOTAL	177	1	m	4	41	ī	1	ı	1	1	1
			-	1	,								

\*(Active) + (Building)+ (Converting)+ (Reserve).

S.N	MARINE REACTORS	LAND BASED REACTORS
5.	The crew (& passengers) constitute a 'captive' audience; they have no place of shelter in case of accidents.  Most likely place of accident is in the least favourable location - the port areas.	In such an event,  people could be evacua- ted to safer areas.  This problem is non-existent.
	(ii) <u>DESIGN</u>	
7.	There are many more start-up and shutdowns as well as widely varying needs for power in man-ceuvering. This results on a greater stress & strain on the nuclear machinery (to be taken care of in design.)	The design need not be that stringent.
8.	Due to space limitations, the machinery of working plants is much more crowded than in stationary plants.	No such limitations.
9.	Due to weight & space limitat- ions, the shops, spare-parts and maintenance facilities are kept to a minimum.	- do -
10.	Design has to cater for specialist aspects on ships like vibrations (of propeller & machinery), sea conditions (roll, pitch, yaw) and limited space and weight.	Earthquake protection is required for reactors.

S.No.	MARINE REACTORS	LAMD_BASED REACTORS
Je IV	THE RESERVE TO SERVE THE PARTY OF THE PARTY	the new response
11.	Irrespective of economic considerations, only the best materials are to be chosen such as to achieve highest possible specific capacity.	Materials chosen should be such as to minimize capital & maintenance cost while still being effective.
12.	Reactor control should be such as to make it inherently safe. in the event of a tsunami or sinking of the ship.	No such restriction
13.	Propulsion system design should cater for an emergency conventi- onally powered propulsion system compatable with the main machine in the event of a complete break down.	LA,
14.	In warships, adequate shock protection for reactors is requiagainst firing of onboard guns and missiles; also required is  (i) protection against shelling  (ii) grounding & collision protection against external accidents.	catered for.
15.	Only PWR's are used as marine reactors.	All types of reactors are possible on land.

## 2.3,2 BASIC DESIGN CRITEPIA FOR NUCLEAR WARSHIPS

Threats to crew health & safety do not arise out of normal operation of nuclear ships but rather due to the possibility of internally and externally caused accidents to them. To minimize these, a variety of special safeguards in design, construction & operation are required. These will be briefly elucidated. There are also, a variety of recommendations applicable to nuclear ships; these, however, won't be discussed here but can be found in references (7) & (10).

Considerations such as the following lead to certain basic objectives that must be achieved in the design of a nuclear warship: :-

- There must be continual knowledge of the level of radioactivity in all normal effluent streams. & of the levels at various locations around the ship.
- There must be complete control of all normal effluent streams, with storage capacity sufficient to permit detailed release of effluents under unfavourable circumstances.
- There must be an extraordinary degree of conservatism/
  redundancy & dependability in the design of the reactor
  so that the likelihood of accidents will be reduced to the
  lowest practicable level. Following aspects are important:-...
  Marine environment like roll, pitch, yaw,

- ✓ Propeller & machinery vibrations of the reactor dompartment.
- Proper reactor containment design for safety.
- √ Collision & grounding barrier protection for reactor compartment.
- Protection of reactor against shocks impressed by weapons firing onboard.
- The ship should have highest possible specific capacity.
- There must be devices & safeguards to minimize the hazardous consequences in case serious accidents should occur.
- There must be an adequate conventional emergency propulsion system in case of complete main-engine breakdown.

Thus the importance of nuclear propulsion for warships as a means towards strategic mobility is obvious to all who pause to consider the matter. It will remain as until a superior form of ocean propulsion for the weapon systems is produced.

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## CHAPTER-3

### RESUME

## RNACTOR DESIGN PROCESS

- 3.1 CHOICE OF REACTOR
- 3.2 PWR DESIGN SCHEME
  - -3.2.1. PROCESS
    - 3.2.2 INTERACTIONS
- 3.3 FUEL ASSEMBLY DESIGN
- 3.4 STEAM CYCLE
- 3.5 INFERENCE

It is well known that only PWRs are used as mobile reactors. In this chapter, this has been justified. In addition, the design methodology, the fuel assembly design and the steam-cycle used has also been elaborated.

### 3.1 CHOICE OF PEACTOR

was fitted with a liquid metal (Nak) reactor called the Submarine Intermediate Reactor (SIR) in 1956. During dockside trials, steam-leaks developed due to Nak alloy coolant entering the superheater steam-piping. After repairs she was put to sea. However, due to recurrence of the above leaks in Dec '58, the reactor had to be replaced with a PWR.

The above experience was an eye-opener for the choice of mobile reactors. Alternately, if BWR; were used, they would give inherent system instability due to the reactor water level constantly varying with the ship-motion effects; in addition, for direct cycle the turbines require shielding, hiking up the grass machinery weight which is a very undesirable phenomenon.

Here, it is not possible to compare the various types of reactors due to space limitations. However, the salient features of a PWR over other reactors have been listed below:-

### Advantages

- Moderator and coolant same.
- Water easily available and cheap.
- Water poses no serious long-term radioactive hazard.
- A primary heat exchanger leak is not hazardous to personnel as primary loop is shielded.
- Reactor has a high negative temperature coefficient making it safe & stable to operate.
- For moderate enrichment and closely-packed lattices, burnup is the highest.
- Being pressurised, the reactor is compact and size a minimum due to high power densities.
- PWR technology is very well known as it is the most common type of naval reactor today.

## Disadvantages

- High primary loop pressure required due to the low boiling point of water; so pressure vessel should be very strong.
- -Poor thermodynamic efficiency-20-25% for mobile reactors.
- As ordinary (light) water has a large neutron absorption cross-section neutron economy is poor.
- Reactor should be shut-down for reloading; (i.e. reloading not possible at sea).

Despite its moderate disadvantages, the power-to-weight ratio of a PWR is the highest; this is a highly desirable factor where compactness and light-weight is a chief requirement. All marine reactors operating today are hence only PWFs.

### 3.2 THE DESIGN SCHME

### 3.2.1 THE PROCESS

This may be divided into the following categories:-

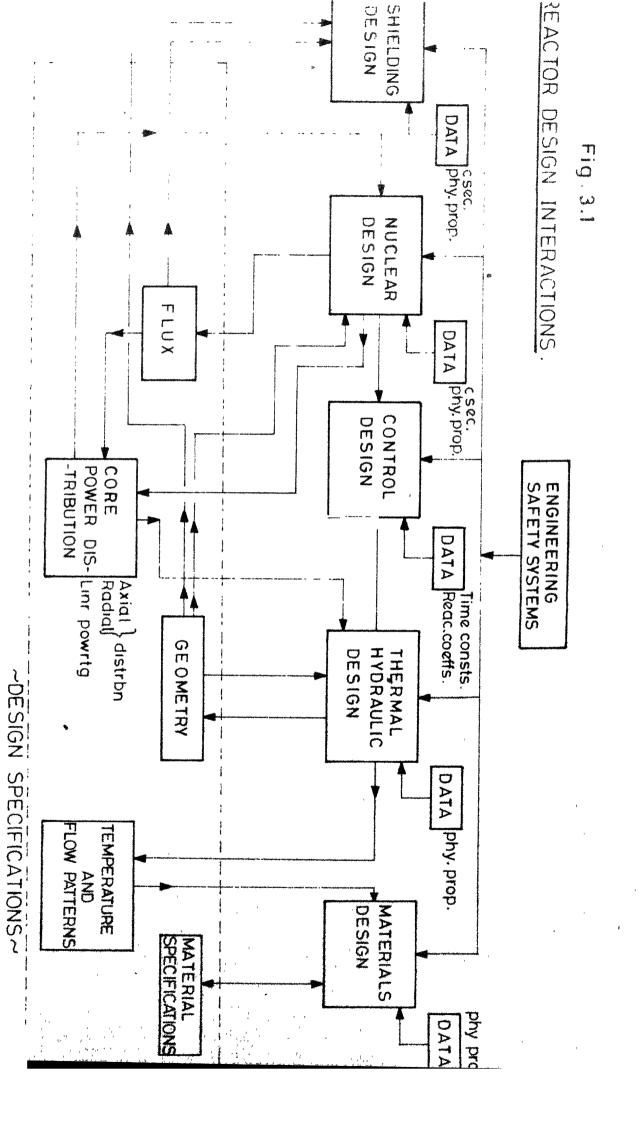
- (i) Core thermal hydraulics design
- (ii) Core Nuclear design
- (iii) Shielding Design
- (iv) Reactor control and safety
- (v) Materials Design

Since each of the categories is complex by itself, it is being treated separately in chapters that follow. The last topic (v), however, has not been included separately, but sketchily covered throughout. Being a reactor for defence purpose, no study on cost-economics has been done.

#### 3.2.2. INTERACTIONS

The integrated reactor design requires substantial interaction among often conflicting design principles of

(i) to (iv) above; safety considerations like biological dose



limitation, prevention of core melt-down, etc, provide very stringent constraints.

Fig 3.1 gives a pictorial view of these interactions in the present design. Nuclear, thermal-hydraulic and material design components result in composition, geometry and operational specifications that characterize the marine reactor system. Nuclear design begins with preliminary cross-sections data. For the calculational modules, flux-averaged cross-sections with appropriate modifications to the working conditions have been used. The flux, power distribution and burnup contribute to a final specification of enrichment. The thermal hydraulic design interacts with power distribution to develop a geometry and its related temperature and flow distributions, limited by material specifications. The nuclear design also yields the reactivity requirements required for the control design.

The control system design for marine reactors is intricate. Whereas a power variation of only 10% is altowed in land-based PWR'syariation from 100% down to 20% is required to be automatically controlled that too in much shorter times for marine reactors. This calls for a non-conventional control system design with careful stability analysis. This is dealt with in chapter-7.

3.3 <u>FUEL ASSEMBLY DESIGN</u>: The first step in core design is to evolve the type of fuel assembly required

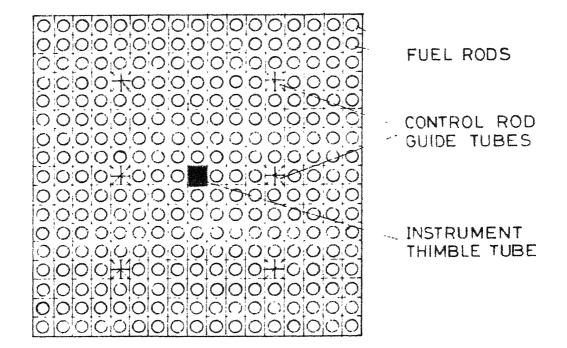


Fig. 3.2
The fuel assembly

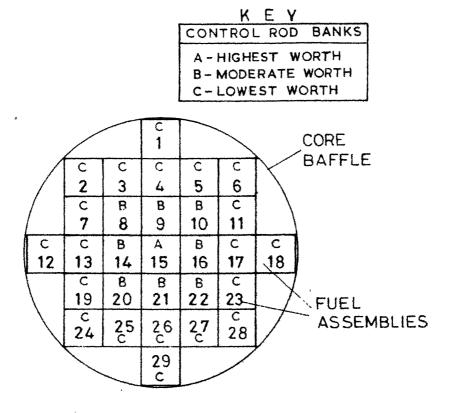


Fig.3.3

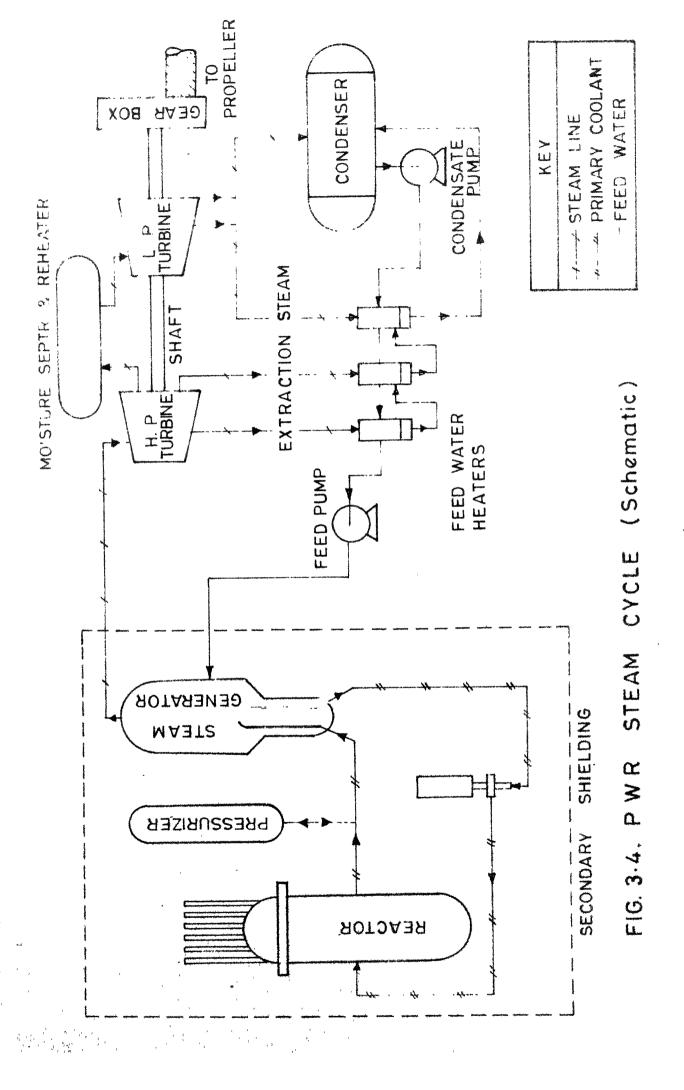
The core configuration

The basic features of the assembly selected is shown in Fig 3.2 (Ref.(7)). A 17 x 17 square pitch layout has been chosen with 282 cylinderical fuel rods per assembly. This configuration represents recent designs that enhance linear heat-rate limits (Ref.(13)). The taxonomy of the fuel assemblies is as shown in Fig. 3.3. This symmetrical arrangement employs an open lattice that permits some flow mixing between adjucent units which is a desirable phenomenon. The diameter of the core baffle is 7.071 times the width of a fuel assembly.

A constant fuel enrichment has been chosen throughout the core. For a linear power rating chosen as 11.00 KW/m (see chapter 4) and 120 MWt power output, the number of fuel assemblies required are 29 (8178 rods). This gives a core height of 133.39 cms. The core-radius is dependent on the fuel rod-pitch (which will be determined later).

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each finger being of the same length as the case. It contains  $B_4^{\text{C}}$  (Boron carbide) enclosed in stainless steel tubes. Their concentration and size are to be determined. The reactivity control is provided by 29 Rod Cluster Control (RCC) assemblies (1 rod-cluster per assembly). They have been constituted in 3 banks A, B and C as shown in Fig. 3.3. No burnable poison



or soluble poison scheme has been included. Each assembly, in addition, has been provided with a central instrument thimble space meant for a movable in core flux measurement detector

### 3.4 STEAM CYCLE

The steam cycle used is illustrated in Fig.3.4.

The 2-loop system is in vogue in almost all working PWR's.

The primary system contains water at 2000 psi (14 MPa).

Coolant pump regulates flow in the loop and pressure vessel.

The presurizer maintains the system pressure within a specified range...2 primary coolant loops supplying to 2 U-tube steam generators of 60 MWt capacity each are chosen.

The secondary loop generates steam at 500 psi (3.5 MPa) at 100% load at a quality of 0.9975. Regenerative been cycles for the turbines have used to improve efficiency. Further details about the steam cycle have not been attempted.

## 3.5 INFERENCE

We have now determined few of the reactor core parameters and the system we have to work on in the succeeding chapters. We also know about system interactions. While considering the various design processes in the subsequent chapters, these interactions have to be borne in mind for an overall non-conflicting design. This has been the earnest endeavour of the author.

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### CHAPTER-4

#### CORE THERMAL DESIGN

## RESUME

#### 4.1 INTRODUCTION

### 4.2 DESIGN CHARACTERISTICS

- 4.2.1 Salient Features
- 4.2.2 Core Flux Distribution
- 4.2.3 Hot-channel Factors
- 4.2.4 Thermal Hydraulic CODE

## 4.3 THERMAL & HYDRAULIC DESIGN

- 4.3.1 Flow Channel
- 4,3.2 Heat Generation
- 4,3.3 Temperature distributions
- 4.3.4 Coolant Pressure drop
- 4.3.5 Heat Transfer Coefficient
- 4.3.6 Tempr. increase in the flowing Coolant
- 4.3.7 Special considerations
- 4.3.8 Other Empirical Correlations

#### 4.4 PESULTS AND COMMENTS

#### 4.1 INTRODUCTION

A nuclear reactor is capable of operating at very high power densities. However, the core must be operated at such a power level that with the best available heat removal systems, the cladding and fuel temperatures anywhere in the core do not exceed safe limits. A fuel element damage, otherwise, will result either in the transfusion of the highly radio-active fission-products into the coolant, or in core-fuel meltdown. Both these effects are highly untesirable. Hence, the core design is dictated more by the thermal limitations rather than any nuclear consideration.

#### GOVERNING EQUATION

The rate of heat removal, (Q) is given by the simple relation (p:369,(17))

Q = h \* A \* At of Tempr.diff.between ht. transfer heat transfer fuel & coolant. coefficient.

'h' is governed by conductive heat transfer through fuel elements and cladding, and convictive heat transfer through coolant. As the fuel is UO2, its thermal conductivity is fixed. So fuel-cladding should have least resistance to heat conduction, in addition to low neutron absorption cross-section, workability,

ability to withstand high temperatures and withstand the corressive action of the coolant fluid; some of these considerations are conflicting; hence a compromise between high thermal conductivity and high temperature operation necessitated the use of stainless steel (\$\$\sigma\$-347) as the cladding material. Resistance to heat conduction is reduced by keeping the cladding thickness to the minimum. Heat transfer by convection to water depends on the properties of water at the operating conditions, and coolant velocity.

"A" is max.imized by having as many fuel rods as possible. Since a large quantity of heat is generated in the compact core, the maximum possible heat transfer area should be squeezed into it.

"At", finally, should be high; high rates of heat release requires low coolant temperatures; this conflicts with basic thermodynamic considerations as a good thermal efficiency requires high coolant temperatures. Hence, to keep coolant temperatures as high as possible and yet retain a high At in the core, fuel elements have to operate at the highest possible temperatures which are limited only by metallurgical & burn-up considerations.

Hence, it is seen that reactor core design necessital a compromise between often conflicting nuclear, metallurgical,

structural, thermodynamic and heat-transfer requirements. To ensure that the core is safe under all operating conditions and transients in our main motto.

#### 4.2 DESIGN CHARACTERISTICS

#### 4.2.1 SALIENT FEATURES

The main problems encountered in thermal hydraulic design are :-

- (i) assure inlet & outlet core flow distribution compatable with power distribution foreseen during the core lifetime.
- (ii) assure cooling of the control rod pins and hydraulic dashpot action (for slowing down control rod velocity at the end of its insertion) during all operating and accident conditions.
- (iii) DNB (Departure from Nucleate Boiling) should not occur under all operating conditions & transients ( i.e. Heat flux anywhere, to be kept below CHF (Gritifal Heat Flux))
- (iv) Bulk boiling of the coolant should hot be allowed to occur in any channel.
- (v) The fuel centre-line temperature should not exceed 2500°C under any circumstance (fuel m.p. 2850°C)
- (vi) Hot-channel factors should be judiciously chosen; with the heat-flux increased by these factors, points (iii), (iv) and (v) above should be satisfied.

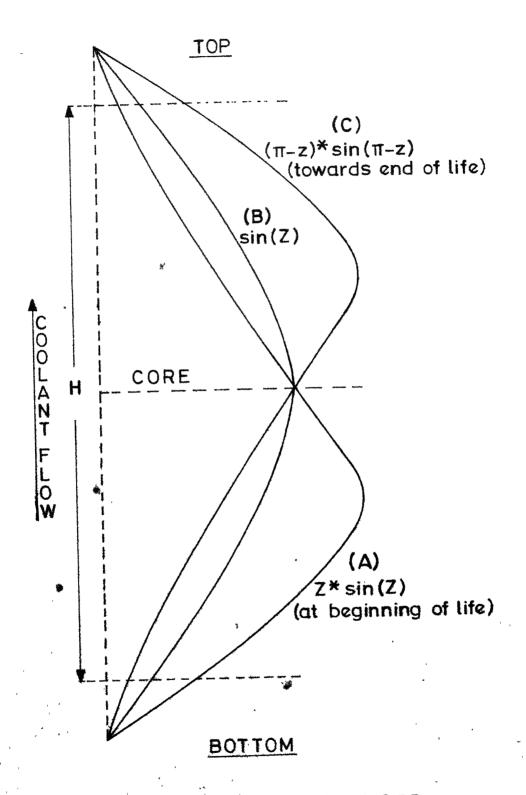


FIG. 4.1 FLUX FUNCTIONS USED
(also refer P. 27 of computer print-outs)

#### 4.2.2 CORE FLUX DISTRIBUTION

The basic core flux distribution has been taken from the "Reactor'Physics Design" section (Ch.5). Radial flux distribution has been assumed as a truncated Bessel's function; the axial distribution, truncated cosine. Due to the high inbuilty reactivity of the core, control rods remain partially inserted in the core. At the BOC (Beginning of Life, of Core) the flux peaks as snown in Fig.(4.1), (A). As the rods are gradually retracted due to burnup, the flux assumes a more sinussidal distribution. Finally at the EOL (End of Life), the distribution assumes profile (C). For calculational purposes, (B) is assumed as Sin(Z) and (A) and (C) as Z-Sin(Z) and  $(\pi-Z).Sin(\pi-Z)$  respectively. For comparitive purposes, the normalized flux distributions have been shown as a computer printout. (See p.27 of computer printouts)

## 4.2.3 HOT CHANNEL FACTORS

In the thermal design of a marine reactor core one is concerned with the most severe conditions in the core. If the design is adequate for these conditions, it is certain to be satisfactory elsewhere. Hence the 'hot-channel' is that coolant channel where heat-flux and enthalpy rise are at a maximum.

# (a) Nuclear hot channel factor $(F_O^N)$

or Nuclear heat flux factor is defined as:

Estimated maximum heat flux in core(based on nominal  $F_Q^N = \frac{\text{fuel enrichment \& dimensions).}}{}$ 

Mean Heat flux in core

 $F_Q^N = F_Z^N * F_R^N$  where, subscripts 'Z' & 'R' stand for axial & radial flux factors. This is the peaking of the flux in the axial & radial directions given as "Feaking Factors" in the CODE.

 $F_R^N \ll 2.32$ ;  $F_Z^N \ll 1.57$  for Sin(Z) flux to  $F_Z^N \ll 1.82$  for Z-Sin(Z) and ( $\pi$ -Z)Sin( $\pi$ -Z) fluxes. This causes  $F_Q^N \ll 4.2224$  (We have obtained  $F_Q^N = 3.4411$  for Z·Sin(Z) flux.) This factor has already been included in the CODE.

(b) Engineering hot-channel factor ( $F_O^E$ ).

The maximum heat flux may increase under the following engineering uncertainties:-

- (i) Local fuel density being greater than nominal (factor concerned  $\mathbf{F}_{\varrho}^{E}$  ) .
- (ii) Fuel dimensions being in excess of nominal ( $F_d^E$ ) (iii) Local fuel enrichments being greater than nominal ( $F_a^E$ ).

$$F_O^E = F_3^E * F_C^E * F_E^E$$

For a PWR this gives a value of 1.08 to 1.10 (Ref(26), pp.170-177). But this approach is unnecessarily conservative and the effect of fabrication tolerances is evaluated statistically giving

$$F_Q^E = 1.04 \cdot (Ref.(20))$$

(c) Engineering hot-channel factor for enthalpy rise :- ( $\mathbf{E}_{\Delta h}^{E}$ ).

This accounts for engineering uncertainties in the maximum enthalpy rise in the concerned hot-channel.

- $F_{\lambda h}^{E}$  depends on the following factors:
  (i) Fabrication tolerance subfactor,  $F_{\lambda h,Fab}^{E}$ , accounts for fuel enrichment variation, fuel weight variation & coolant flow variation; it is evaluated statistically.
- (ii) Core Flow Sub-factor  $(E_{h,Flow}^{E})$ . accounts for the hot-channel receiving less than its expected share of coolant flow.
- (iii) Core mixing sub-factor (FE \_Ah, mix), accounts for flow from surrounding cooler channels mixing with flow in the hottest channel. This is favourable countering the deleterious effect of the other subfactors.

Typical values of above for a PWR are:-

$$F_{\triangle h}^{E} = F_{\triangle h, Fab}^{E} * F_{\triangle h, Flow}^{E} * F_{\triangle h, mix}^{E} = 1.08$$

(d) Overall hot-channel Factor(F)

The engineering ( $F^{E}$ ) uncertainty factor would be

$$F^{E} = F_{Q}^{E} * F_{\Delta h}^{E}$$
 ( 1.167 for PWR )

However, in the Italian ship Design (Ref(2),p.598)  $F_{\Delta h}^E$  = 1.22 has been used instead of the above figure, giving  $F^E$  =1.269; this has been used in this analysis. This means if the heat flux is increased by this amount in the CODE, the core design should

should sustain itself. (F $_{\rm Q}^{\rm N}$  has, as stated earlier, already been included in the C^-2 ).

The overall factor F, would hence be:

$$F = F_O^N * F^E = 4.367$$

This implies the core should sustain a heat flux over its average value, of 4,367 times everywhere in the core.

#### 4.2.4 THE THERMAL HYDRAULIC CODE

impossible without the aid of a computer. In the computer Composition of material properties with temperature. It lists output in a 3-dimensional manner giving axial variations of temperatures & pressure for the rods at the core centre, and then at discrete steps upto the core periphere. The analysis of the rod is for:-

- (i) Coolant integrity
- (ii) Cladding integrity.
- (iii) Coolant exit conditions and pressure drop.

In addition for:-

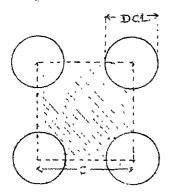
- (iv) Radial flux variation in the core
- (v) Pumping requirements for primary system.
- (vi)Determination of core diameter (for 120 MWth power),
   and total number of rods.
- (vii) Temperature feedback for reactor neutronics calculations.

The importance of the CODE is felt when one has to do repeated analysis of a core with small variations in input, to arrive at an optimum solution. In addition, cores of different reactors can easily be analysed since material properties are fixed. The CODE developed is versatile enough to be used either for stainless steel or Zirconium cladding, and either a square-arrayed core or a hexagonal arrayed core.

### 4.3 THERMAL AND HYDRAULIC DESIGN

The fuel rod has been axially divided into 50 equal segments. The properties of materials in one segment are considered constant and so also temperatures, axially. The basic theory governing the temperature distribution, heat transfer rates, pressure drops & energy balance is presented below, and done for each of the 50 segments, successively. Temperature distribution, in fuel & cladding are calculated using one-dimensional radial heat conduction. The pressure drops & heat transfer coefficients are calculated using empirical relations for flow channels.

#### 4.3.1 FLOW CHANNEL



In this core design, the square arrary has been used. For the fuel rods of diameter DCL and pitch s, the flow area (A) per rod is given by

$$A = S^{2} - \frac{\pi * DCL^{2}}{4}$$
 (shaded portion)  
...Eqn..(4.1)

#### 4.3.2 HEAT GENERATION

Fission heat generated is directly proportional to thermal flux (taking cross-sections as constant). The volumetric source strength  $\P^{n}$  is :-

$$4 = 3.204 \times 10^{-11} \times \frac{5}{f} \cdot \text{g (r,z)} \cdot \text{J/cm}^3 - \text{s}$$

Thus, q varies axially & radially as:

$$q''(z,r) = q_0' * Cos(\frac{\pi}{R+d}z) * J_0(\frac{2.405}{R+d}.r)$$
 .... Eqn (4.2)

for z=0 to H

r=0 to  $\sqrt{2}$  where  $q_0$  is the peak flux at centre of core.

R= Core Radius

d= distance from core face where
 flux = 0.

An important quantity required to be known beforehand is heat-flux. generated per unit length of rod  $(k_W/m)_{q_{aV}}^{1}$ . This is an average quantity for all rods. After a review of the reactors of the world (Ref.(14)), a figure of 11.0 KW/m was arrived at. This factor is related to the average volumetric heat flux thus-

 $q_{av}'' = q_{av}' / \pi r_{fu}^2$  where,  $r_{fu}$  = fuel pellet radius The volumetric power density at the core centre is:

$$q_0 = F_R^N * F_Z^N * q_{av}$$

where  $F_R^N$  &  $F_{\mathbf{Z}}^N$  are hot-channel factors as explained before.

since by virtue of definitioħ√

$$q_{av}^{(i)} = \frac{1}{V} \int_{\text{all } q_{O}}^{\text{in}} \cdot \cos(\frac{\pi}{He}z) \cdot \frac{(2.405)}{R+u} \cdot 2 \cdot \text{rdr}_{de}$$

where V= core volume

we arrive at the following relations :-

$$F_{R}^{N} = \frac{1}{2 \frac{J_{1}(LR)}{LR} + 2(\frac{C}{A}) \frac{I_{1}(mR)}{mR}}$$
, for a truncated Bessel's function flux-distribution,

$$F_{Z}^{N} = \frac{\pi}{2} * \frac{H}{He} / \sin \left(\frac{\pi}{2H_{e}} H\right), \text{ for truncated cosine}$$

$$= \frac{1.8197 * \pi * H}{He (-ACos(A) + B Cos(B) + Sin(A) - Sin(B))}, \text{ for truncated } (\pi-z).Sin (\pi-z) \text{ function}$$

where, 
$$A = \frac{H \pi}{He}$$
 and  $B = (\frac{He-H}{2He}\pi)$ .

Refer Appendix AS-1 for the above inferences.

## 4.3.3 TEMPERATURE DISTRIBUTIONS

(1) In fuel rod -

The basic heat conduction equation with heat generation is (in cylinderical coordinates )

$$\frac{d^2 T}{dr^2} + \frac{1}{r} \frac{dT}{dr} + \frac{q}{K_{Fu}} = 0$$

with boundary conditions as

T=To at r=o (fuel centre-line temperature)

$$\frac{dT}{dr} = 0$$
 at  $r=0$ 

the solution of the above equation is

$$T_{r} = To - \frac{q}{4K_{Fu}} r^{2},$$

showing a parabolic temperature distribution with the maximum at the fuel rod centre. Hence, at the fuel outer radius ( $r_{\rm Fu}$ ) ,

$$T_F = To - \frac{q}{4 K_{Fu}} r_{Fu}^2 \dots (Eqn 4.3)$$

During the steady state condition, all of the energy generated must be transferred out to the cladding — since  $K_{\overline{Fu}}$  changes with temperature, an iterative technique has been used to obtain the cladding thermal conductivity to within 1%.

If  $K_{Fu}(T)$  = a+bT where a and b are constants, then we find that the value of  $K_{Fu}$  to be used is precisely equal to  $K_{Fu}$  evaluated at the mean temperature  $\frac{To + T_F}{c}$ 

i.e. in Eqn. 4.3, 
$$K_{Fu}(T) = K_{Fu}(\frac{To + T_F}{2})$$

(Refer Appendix A4-2)

## (2) In gas gap

The temperature drop across the gas gap is taken as

$$T_{f} - T_{g} = \frac{\frac{1}{g} r_{Fu}}{2 h_{gap}} \dots (Eqn 4.4)$$

where  $^{h}$ gap = gap conductance = 0.6  $^{w/cm^2-K}$  (p.356, ref (12))

h is taken as constant throughout the core.

## (3) In the cladding

Technique used here is similar to that in the fuel rod.

The governing equation is :-

$$\frac{1}{r} \cdot \frac{d}{dr} (r \cdot \frac{dt}{dr}) = 0$$
 ... Eqn. (4.4b)

with initial conditions as

 $T = T_g$  at  $r = r_g$  (outer radius of gap )

$$\frac{d\mathbf{r}}{d\mathbf{r}} = \frac{\mathbf{r}}{\mathbf{r}} \frac{\mathbf{r}_{Fu}}{2K_{cT}} \mathbf{q}^{m} \quad \text{at} \qquad \mathbf{r} = \mathbf{r}_{g}$$

where,  $K_{cd}^{-}$  thermal conductivity of cladding.

Eqn. 4.4b gives a simple logarithmic solution

$$T = T_g - \frac{f^{(1)} r^2}{2 K_{cl}} + \ln(\frac{r_{cl}}{r_{Fl}}) \dots (Eqn 4.5)$$

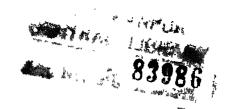
where r & outer cladding radius.

Here again, K is a linear function of temperature and hence an iterative technique has been used to obtain  $K_{\mbox{cl}}$  to within 1% occuracy,

$$K_{C1}(T) = K_{C1} \left( \frac{T_F + T_S}{2} \right)$$

## (4) In the coolant

All heat energy generated by the fuel must be ultimately transferred to the coolant through the fluid layers near the cladding outer surface. Newton's law of cooling has been used



for this purpose:-

 $\mathbf{T}_{\mathrm{B}}$  is a mass-weighted average temperature of the water in the flow channel.

As, 
$$q_s = q''' \pi (r_{Fu})^2 \triangle 1$$

$$A_s = 2 \pi r_{cl} \triangle 1$$

thus,

$$T_s - T_B = \frac{\frac{1}{2} r_{Fu}^2}{2 h r_{Col}^2}$$
 .... (Eqn 4.6)

The method of determining (h) is elucidated later in this section (4.3.5).

T<sub>R</sub> is to be known

before we start temperature calculations. After that,  $T_s, T_g, T_f$  and To are determined using equations 4.6,4.5,4.4 and 4.3 successively. Method of calculating  $T_B$  has been stated later (4.3.6).

## 4.3.4 COOLANT PRESSURE DROP

We shall determine only the pressure drop in the core here. There are 2 types of losses occuring.

(i) Frictional pressure drop along the channel,  $\Delta P_F$  (ii) entrance and exit permanent pressure losses,  $\Delta P_E$ .

(i)  $\triangle P_F$  occurs due to the shear stress on the flowing fluid by the walls of the flow channel. This is given by the relation:-

$$\Delta P_{F} = \frac{\mathbf{f} * \Delta i}{D_{e}} * \frac{\hat{S} V_{B}}{2g} \dots (Eqn 4.7)$$

where, f := friction factor

Al= segment axial length

 $\mathcal{E} \doteq \text{water density at } \mathbf{T}_{B}$ 

 $v_{B}$ = average channel coolant velo**c**ity

 $D_{e} = E_{q}uivalent$  channel diamter, and

g = gravitational accleration constant, 9.81 m/s<sup>2</sup>

Here, 
$$D_e = \frac{\text{flow irea}}{\text{wetted Perimeter}} = \frac{A}{2^{\pi}r_{cd}}$$
 'A' defined by (Eqn. 4.1)

The value of f depends on flow and surface conditions in channel. The flow conditions are characterized by Reynold's number, Re.

$$Re = \frac{\$ v_B D_e}{u}$$
 ..... (Eqn. 4.8)

where,  $\mu$ = Coefficient of viscosity of water.

Re should be greater than 2000 for turbulent flow that is desirable due to the higher heat transport rates. In our case,  $R_e = 237842.1$ . (see p. 28 of computer printouts).

The second condition, the surface condition is characterized by ratio of surface roughness ( $\epsilon$ ) height, to the equivalent diameter  $^{\epsilon/D}_{\epsilon}$ . The flow channel exhibits smooth tube behaviour if  $\epsilon < t$ , the laminar sublayer thickness. Hence the cladding outer surface

smoothness should be so controlled that this criterion is met.

The smooth circular tube friction factor  $(\mathbf{F}_{\text{cire}})$  is got by using this coorelation widely accepted in reactor work:

$$f_{cire} = 0.184 * R_e^{-0.20}$$
 ..... (Eqn 4.9)

The Deissler & Taylor correlation for the correction of circular tube data to the rod-bundle geometry has been used:-

$$\frac{\mathbf{f}}{\mathbf{f}_{circ}} = -3.475 + 8.053 \left(\frac{\mathbf{s}}{D_e}\right) - 4.705 \left(\frac{\mathbf{s}}{D_e}\right)^2 + 0.9162 \left(\frac{\mathbf{s}}{D_e}\right)^3$$
... (Eqn. 4.10)

This value of T has been used in Equation 4.7.

(ii)  $\triangle P_{\rm E}$  losses are the result of increased viscous energy dissipation resulting from increased turbulent activity at inlet and outlet.

$$P_E = K \frac{3 V_B^2}{2g}$$

where K = resistance coefficient for sudden contraction from large to small flow diameter; K=0.5 at core inlet, K=1.0 at outlet.

## 4.3.5 HEAT TRANSFER COEFFICIENT (h)

A two-step procedure has been obtained to calculate 'h'

(i) 'h' for flow in circular tubes in found first.

(ii) A correlation correction is applied then to obtain 'h' for actual reactor coolant flow geometry. No direct analytical methods for predicting 'h' for turbulent flow ...

exist. However, by use of an analogy between hear & momentum transport, dependence of 'h' on Re can be predicted. Then, by applying the results of a heat transfer analysis for laminar flow over a flat plate, an estimate of the prandtl number, Pr, dependence on heat transfer is obtained. In this analysis, the Dittus-Boelter correlation has been used:

$$N_{u_{circ}} = 0.023 * R_e^{0.8} * P_r^{0.4}$$
 .... (Eqn.4.11)

where Nucirc = Nusselt number for circular tube  $R_e = \text{Renault's number (given by Eqn.4.8)}$   $P_r = \frac{C_p \; \mu}{\kappa}$ 

Now, Deissler & Taylor correlation for the actual coolant channel is done, like in Eqn.4.10

$$\frac{\text{Nu}}{\text{Nu}_{\text{circ}}} = -3.475 + 8.053 \left(\frac{\text{S}}{\text{De}}\right) - 4.705 \left(\frac{\text{S}}{\text{De}}\right) + 0.9162 \left(\frac{\text{S}}{\text{De}}\right)^{3}$$
(Eqn. 4.12)
$$\text{since Nu} = \frac{\text{h De}}{\text{K}}$$

$$\text{h} = \frac{\text{Nu} * \text{K}}{\text{De}} \qquad (\text{Eqn. 4.13})$$

## 4.3.6 TEMPERATURE INCREASE BY THE FLOWING COOLANT

Coolant temperature varies from a minimum at the inlet to a maximum at the core exit. The temperature in our analysis is assumed to very discretally from one segment to another. The bulk temperature  $T_B$  at any point (required in

Section (4.3.3) is determined from an energy balance between the total energy added by heat transfer, and the energy rise of the coolant; i.e.

$$\mathbf{\tilde{m}} \cdot \mathbf{C}_{p} \Delta T = \mathbf{\tilde{q}}^{2} \pi \mathbf{r}_{fu}^{2} \Delta 1$$
,

where, .m = mass flow rate of coolant

 $\Delta 1$  = length of the segment

 $\Delta$ T= increase in Bulk temperature from one segment to another,  $(T_{B2} - T_{B1})$ 

Thus, 
$$T_{B2} = T_{B1} + \frac{\pi r_{fu}^2 \Delta l}{\tilde{m} c_p}$$
 (Eqn 4.14)

for the first segment  $T_{B1}$  = inlet temperature and thus  $T_{B2}$  is evaluated. For successive segments  $T_{B2}$  becomes  $T_{B1}$  and the calculation proceeds.

## 4.3.7 SPECIAL CONSIDERATIONS

Two important checks are required to ensure proper coolant conditions:-

(1) No Bulk-Boiling occurs anywhere in the core;

To ensure this  $T_B < T_{SAT}$ , the coolant saturation temperature at the local pressure. The critical location is, of course the core exit for the central rod where bulk temperature is maximum and pressure the minimum.

(2) No local boiling or sub-cooled boiling occurs near the surface of the fuel rod. Whenever  $T_s > T_{SAT}$  at a local point, this phenomenon may occur like during peak loads. This may result in Boiling burnout of the surface, To assess this, the local heat flux , is compared with the CHF, Critical Heat Flux (or DNB) at which state blanketing of the heat transfer surface by coalesced vapour bubbles is just imminent. Any further flux increase requires heat transfer through this blanket. Due to the low conductivity of the vapour blanket, a catastrophic increase in sr face temperature would result, leading to melting of the cladding.

Determination of the CHF has been done using the widely accepted Jens and Lottes correlation:

CHF 
$$\pm$$
 C  $(\frac{\dot{m}}{10^6})^{M}$   $(T_{SAT}-T_B)^{0.22}$  ... (Eqn 4.15)

where, C, M = pressure dependent constants(see sec.4.3.8)

Whenever sub-cooled flow boiling exists to any extent, Newton's law of cooling for determining  $T_{\vec{o}}$  is invalid (as 'h' in it does not reflect the increased agitation in the boiling film due to the vapour bubbles). Jens & Lottes correlation for sub-cooled boiling gives (in f.p.s. system)

$$T_s = 1.9 \left(\frac{1}{q}\right)^{O25} \exp\left(-P/900\right) + T_{SAT}$$
  
where,  $P = local coolant pressure$ 

$$\frac{1}{q} = \frac{r_{fu}^2}{2 r_{C1}}$$

ر پینید The CHFR (CHF ratio) defined as ratio of CHF and q, should hence be greater than 1 to satisfy condition (2) above.

### 4.3.8 OTHER EMPIRICAL CORRELATIONS

The thermal conductivities, viscosity, density and specific heat at constant pressure are all functions of temperature. As temperature in the coolant channel continuation varies, correlations for them would be required.

They are (in c.g.s. system)

$$K_{fu}(T_{4}) = 0.10308 - 0.14186 E-3 * T + 0.73263E-7 * T^{2}$$

$$K_{C_{1}}(T) = 0.14194 + 0.6924E-4 * T,$$

for the coolant:-

$$K (T) = 0.27656E-2 + 0.39731E-4 * T - 0.10152 E-6 * T^2$$

$$\mu$$
 (T) = 0.329E-2 - 0.12479E-4 \*T + 0.15296E-7 \* T<sup>2</sup>;

$$^{\circ}$$
 (T) = 0.738 + 0.6445 E-3 \*T - 0.45827E-5 \*  $^{\circ}$ 

$$C_p(T) = 17.677 - 0.1104 * T + 0.2338 E-3 * T^2;$$

certain other phenomena depend on local pressures. They are correlated as under ( P in p.s.i.)

$$T_{SAT}$$
 (P) = 0.23357E3 + 0.6129E-1 \* P - 0.5666E-5 #  $P^2$ ,

$$C(P) = 0.11312E1 - 0.78E-3 * P + 0.3312E-6 *P^2 - 0.56355 E-10 * P^3,$$

$$M(P) = 0.48141E-1 + 0.22471 E-3 * P + 0.8302E-9 *P2,$$
(C & M as in eqn 4.15)

Finally, a series expansion has been used to evaluate Bessel's functions  $J_{o}(x)$  &  $J_{1}(x)$  and modified Bessel's functions  $I_{o}(x)$  &  $I_{1}(x)$  (from ref (40)).

# 4.4 RESULTS AND COMMENTS

Analysis of core performance of merchant ships SAVANNAH, MUTSU and LENIN was done using the Thermal Hydraulic CODE & results obtained were within 1°C accuracy. A pellet diameter and clad thickness of respectively 0.858 cm & 0.66 mm was chosen after an optimization study using ref(14). Results for various combinations of pellet dia and clad thickness for a constant volume ratio of fuel & water (for satisfying Reactor Physics considerations) are given below; the design chosen (case 1) can hence be justified as being optimum:-

Parameter	Case 1	Case 2	Case 3	Case 4
Pellet size	0.858	1.000	1.000	0.700
Clad thickness	0.066	0.066	0.100	0.066
Pitch	1.30	1.766	1.810	1.262
Core dia (for 120 MWt)	134.29	182.41	186.99	130.34
Core Power Den	.63.51	34.42	32.76	67.41
Max fuel Centr line Tempr.	e- 1696.8	1678.6	1688.4	1725.3
Min. CHFR obtained	2.701	3.334	3.530	2.313
	1.615	2.946	3.000	1.809
Burnupflux	14698	16982	16530	10685

The thermal Hydraulic CODE can be used for various flux functions Sin(z), z. Sin(z) &  $(\pi_{-z})$ .  $Sin(\pi_{-z})$  by feeding an input 'flux code' 000,111 or 222 respectively. Some results obtained by this exercise ensue as follows:-

Parameter	Sin( Z )	z.Sin(z)	$(\pi - Z)$ . Sin $(\pi \cdot$
Minimum CHFR	3.248	2.701	2.797
Total $ extstyle{ iny F}_{\mathcal{Q}}^{ extstyle{ iny N}}$	3.705	4.367	4.367
Max. fuel C-Line tempr. (°C)	1541.4	1696.8	1696.8
Max. cladding tempr.(°C)	335.86	335 <b>,</b> 8 <b>7</b>	335.88
Flux beyond which bulk boiling/burnout occurs (times of average flux)	1.615	1.586	1.586
Coolant exit tempr. from bottest cnannel(°C)	316.33	316,92	316.91

Results obtained from the CODE are given in pages 28 to 36 of computer print-outs; flux distribution illustrated is Sin(z). For comperitive purposes, fuel-rod conditions for the hottest channel for Sin(z) &  $(\pi-z).Sin(\pi)$  distribution are tabulated in pages 46 to 48 of printouts.

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# CHAPTER-5

# REACTOR PHYSICS DESIGN

### RESUME

# 5.1 INTRODUCTION

- 5.1.1 Neutron cycle
- 5.1.2 Reactor Physics CODE

# 5.2 CRITICALITY OF THE REACTOR

- 5.2.1 Evaluation of kinf
- 5.2.2 Leakage and keff
- 5.2.3 Control requirement
- 5.2.4 Temperature & pressure effects
- 5.2.5 Heterogeneous vs homogeneous

# 5.3 FLUX DISTRIBUTION

# 5.4 RESULTS

### 5.1 INTRODUCTION

A nuclear reactor is an assembly of a proper size of fissionable material and other associated materials essential to sustain a chain reaction. The power generated is directly dependent on the neutron flux. It is of prominence to understand the behaviour of these neutrons in the reactor.

In this chapter, we consider those reactor-core calculations that provide  $k_{\mbox{eff}}$ , effective multiplication factor and the stationary neutron-flux distribution at Steady-state operation.  $k_{\mbox{eff}}$  is required to establish nuclear composition and configuration, which satisfies criticality and control requirements. The steady-state flux distribution must be known to calculate reaction rates and power distributions that are needed for the thermal & shielding design of the reactor.

Evaluation of  $k_{\rm eff}$  necessitates the determination of the 4 factors  $\eta$ ,  $\epsilon$ , p, f and non-leakage probabilities  $L_{\rm T}$  and  $L_{\rm F}$ . For sketching the flux distributions, 2-group 2-region theory has been used with water as the reflector Heterogeneous effects have been considered at all stages of calculation.

### 5.1.1 Neutron Cycle:

A typical history of 100 fast fission neutrons and how they sustain a chain reaction is illustrated in Fig(5.1). All important neutron interactions are indicated in it; the parameters used are applicable to the present design.

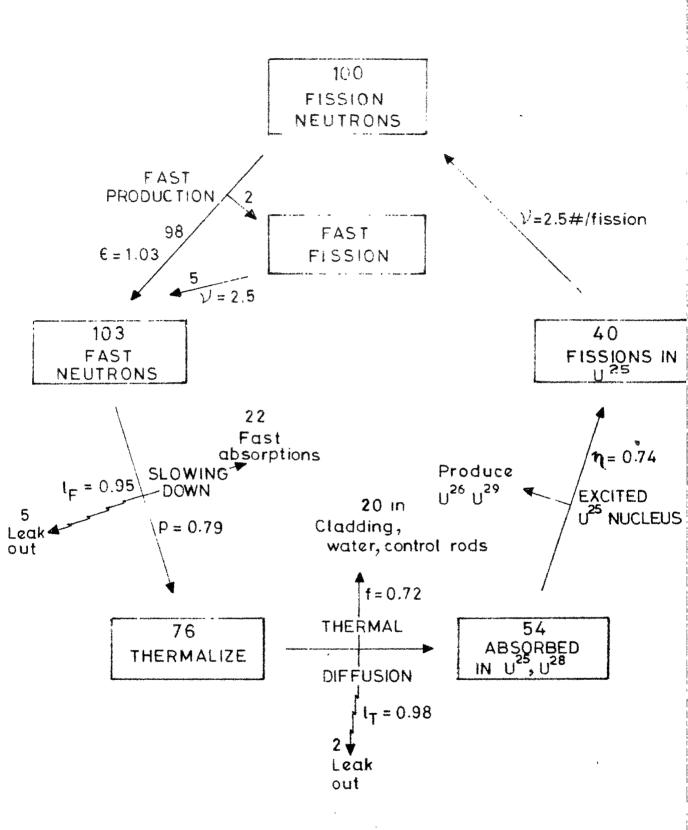


FIG. 5-1 CORE NEUTRON CYCLE

### 5.1.2 Reactor Physics Computer CODE

A computer CODE has been generated for determining  $k_{\mbox{eff}}$  and the flux distributions. The amount of 'poison' required in control rods has also been estimated. All parameters used have been corrected for the operating temperature and pressure. The inputs like core dimensions and temperatures of fuel & moderator have been taken from Chapter 4. An enrichment of 5.0% has been chosen (chapter 3 ). The scheme of fuel loading in reactor is as per chapter 3.

The scheme of computations is as follows. Input data are enrichment, fuel-rod & reactor dimensions, reflector thickness & average fuel & moderator temperatures. The only variable parameter fed in is the volume fraction (of moderator) of Pois on, Pfrac frac is changed by interpolation till the critical determinent = 0; this will denote a steady-state reactor operation with the nett control poison of Pfrac flux in both core and reflector are sketched for the above.

# 5.2 CRITICALITY OF THE REACTOR

# 5.2.1 Evaluation of kinf:

Considering the reactor core as homogeneous will be errenteous as neutrons may undergo several collisions within a fuel rod before encountering the moderator. Calculation of  $k_{\mbox{inf}} = \kappa$  epf still holds; but differences with respect to

homogeneous considerations should be noted.

ETA ( 功量 ) :-

This gives the ratio of neutrons produced to that absorbed in the fuel rod. Since absorption cross-section of Oxygen is essentially zero.

where,  $\gamma_{25}=2.47$  and  $\Sigma_{a25}$ ,  $\Sigma_{f25}$  is dependent on fuel enrichment (hereafter) and cross-sections corrected for average fuel temperature obtained from chapter 4.

### THERMAL UTILIZATION (f)

This gives the probability that a thermal neutron is absorbed in the fuel itself with respect to the whole core i.e. ratio of neutrons absorbed in fuel only, to that absorbed in fuel, moderator & other structural materials.

$$f = \frac{\sum_{\text{afu}} \varphi_{\text{Tfu}} \cdot \varphi_{\text{fu}}}{\sum_{\text{afu}} \varphi_{\text{Tfu}} \cdot \varphi_{\text{fu}} + \sum_{\text{am}} \varphi_{\text{Tm}} \cdot \varphi_{\text{m}} + \sum_{\text{ass}} \varphi_{\text{Tss}} \cdot \varphi_{\text{ss}}}$$

where, all fluxes and cross-sections are average values. Since  $\mathbf{p}_{\mathrm{Tss}} \ \cong \ \mathbf{p}_{\mathrm{Tm}}$  ,

$$f = \frac{\sum_{\text{afu}} V_{\text{fu}}}{\sum_{\text{afu}} V_{\text{fu}} + (\sum_{\text{am}} V_{\text{m}} + \sum_{\text{ass}} V_{\text{ss}}) Y_{\text{T}}} \dots \text{Eqn}(2)$$

where  $T = \frac{\varphi_{\text{TM}}}{\varphi_{\text{TM}}}$  is called thermal Disadvantage factor(TDF).

(ranges from 1.00 to 1.05).

This factor is peculiar of heterogeneous reactors, taking into consideration reduction of thermal flux in \*fuel rod.

due to self-absorption. As tis unknown, f is evolved through lattice functions for cylinderical fuel

rods:-

$$\frac{1}{f} = \frac{\sum_{am} \cdot v_m + \sum_{ass} v_{ss}}{\sum_{afu} \cdot v_{fu}} * F(x) + E(y,z)$$
...Eqn(3)

where F(x) and E(y,z) evolved from diffusion theory, are lattice functions defined by :-

$$F(x) = \frac{x + I_{0}(x)}{2I_{1}(x)}$$

$$E(y,z) = \frac{z^{2}-y^{2}}{2y} \cdot \cdot \cdot \cdot \cdot \frac{I_{0}(y)K_{1}(z) + K_{0}(y)I_{1}(z)}{I_{1}(z)K_{1}(y) - K_{1}(z)I_{1}(y)}$$

where, 
$$x = \frac{a}{L_{fu}}$$
,  $y = \frac{a}{L_{m}}$   $z = \frac{b}{L_{m}}$ 

a = fuel rod radius .

b = radius of equivalent fuel cell =  $\frac{\text{Pitch}}{\sqrt{\pi}}$ thermal diffusion lengths.

The above equations, however, are valid for a b and hence inaccurate for closely packed lattices. For x, y, z, individually being < 0.75, the following series expansions are guite accurate:-

$$F(x) = 1 + \sum_{i=1}^{\infty} \frac{1}{2 \times i} (\frac{x^{2i}}{2}) \dots \text{Eqn (4)}$$

$$E(y,z) = 1 + \frac{z^{2}}{2} \left\{ \frac{z^{2}}{z^{2} - y^{2}} \cdot \ln (\frac{z}{y}) + \sum_{i=2}^{\infty} \frac{(-1)^{i+1} + 3}{2 \times i} (\frac{y}{z})^{2(i-2)} \right\}$$

$$\dots \text{Eqn. (5)}$$

**.** . .

'f' is the most important factor that controls  $k_{\rm eff}$ . Control rod positions greatly alter it. The above treatment does not include control poison. In Eqn.(3), the value of  $\sum_{\rm am}$  has to be modified to include the effect of Boron Poison. This is done by considering the poison as being equally dispersed in moderator and a term ( $P_{\rm frac} * \sum_{\rm ap}$ ) now gets added, where  $\sum_{\rm ap} = \max_{\rm frac} \max_{\rm ap} \sum_{\rm frac} \max_{\rm frac} \sum_{\rm frac}$ 

### RESONANCE ESCAPE PROBABILITY ( p )

This is the probability that a fission neutron will escape capture in resonances in  $\mathbf{U}^{28}$  as it slows down to thermal energies. It is given by

$$p = \exp \left(-\frac{\sum_{fu}^{N} V_{fu}^{I} \cdot \emptyset_{fu}}{\sum_{fu}^{N} V_{fu}^{I} \cdot \emptyset_{fu}}\right) \qquad \text{Eqn.(6)}$$
where  $\emptyset_{i}$  = fast fluxes

Here we are neglecting fast absorptions in cladding material and Poison which are negligibly small.  $\frac{\emptyset_{m}}{\emptyset_{fu}}$ , above, called the disadvantage factor for resonance neutrons is unknown. So p can't be evaluated through Eqn.(6). In a similar manner to f, p is evaluated through lattice functions.

Defining  $f_r$ , resonance utilization factor

$$f_r = \frac{Fast absorptions in fuel resonance}{Total fast absorptions}$$
;

$$= \frac{\int_{\text{II}} \frac{1}{\text{V}_{\text{fu}}} \frac{1}{\text{V}_{fu}} \frac{1}{\text{V}_{\text{fu}}} \frac{1}{\text{V}_{fu}} \frac{1}{\text{V}_{\text{fu}}} \frac{1}{\text{V}_{\text{fu}}} \frac{1}{\text{V}_{\text{fu}}} \frac{1$$

As  $(\frac{\rho_m}{\rho_{fu}})$  is unknown, fraction to evaluated. We hence use the following lattice functions (for cylinderical rods):-

$$\frac{1}{f} = \frac{\sum_{sm} V_m}{V_{fu}} * F(x) + E(y,z) \dots Eqn.(9)$$

where, F(x) and E(y,z) have same meaning as Eqns.(4) & (5) with x,y,z being functions of fast diffusion lengths here. Knowing  $f_r$ , p is calculated using Eqn(8). In eqn.(10)  $\{\Sigma_{sm}\}$  is taken directly from tabulated experimental values - for water 1.46 cm<sup>-1</sup> ( P.232 Ref. (23)) and  $I_{eff}$  the effective resonance integral, is well represented for cylinderical fuel rods as :-

$$I_{\text{eff}} = A + \frac{C}{\sqrt{a \cdot 9}} \dots Eqn. (10)$$

where A,C are constants (Ref.ibid)

a = fuel rod radius

= fuel density.

Eqn. (10) & evaluates itself to 21.254 barns.

Note: Though listed values are for pure  ${\tt U}^{28}{\tt O}_2$  they are valid for slight fuel enrichments (upto 5%) as it does not significantly after the extent of resonance absorption in  ${\tt U}^{28}$ .

In Eqn.(9) the effect of Poison on  $\sum_{sm}$  should be considered. The effective values of  $\sum_{sm}$  should be taken.

$$\underset{\text{eff}}{\stackrel{?}{\underset{\text{eff}}{\mathcal{Z}}}} = \frac{(\stackrel{?}{\cancel{\chi}} \Sigma_{\text{sm}})_{\text{m}} + (\stackrel{?}{\cancel{\chi}} \Sigma_{\text{sp}})_{\text{p}}}{\Sigma_{\text{sm}} + \Sigma_{\text{sp}}} \dots \text{Eqn (11)}$$

and 
$$\sum_{\text{smeff}} = (\sum_{\text{sm}} + \sum_{\text{sp}})$$

FAST FISSION FACTOR ( $\epsilon$ .):-

All neutrons don't succeed in escaping from fuel and subsequently slowing down in moderator. Some are absorbed in resonances above fission threshold as well as upto the lower threshold of inelastic scattering in fuel, giving rise to fast fissions, a favourable phenomenon. E is the ratio of number of neutrons having first collision in moderator to the total produced in thermal fission. For determination of £, the method of pinard, Fleishman & Soodak (SFS) modified for closely-packed lattices has been used. The neutrons are classified into 3 energy-groups in fuel with corresponding neutron escape probabilities without having a collision in fuel as  $P_1, P_2$  &  $P_3$  defined by Wigner's approximate

$$P_{i} = \frac{1}{\bar{r} \sum_{it} + 1}$$
 for i=1 to 3 .... Eqn (12) where, 
$$\bar{r} = \frac{4}{\text{Surface area}}$$
 of fuel rod 
$$= 2 \cdot r_{fu}$$
 for cylinderical rods. 
$$\sum_{it} = \text{Total Group i cross-section.}$$

The 2 fractions of fission neutrons in the 2 energy groups, with the first above and the second below the fission threshold of 1 MeV, are given as  $v_1 = 0.561$  and  $v_2 = 0.439$ . The third group contains neutrons scattered from the first group into energies below fission threshold given by fractions:-

$$\beta_{1} = \frac{\gamma_{1} \gamma_{1} \sigma_{1f} + \sigma_{11}}{\sigma_{1t}} \dots \text{Eqn} \quad (13)$$

$$\beta_{2} = \frac{\sigma_{22}}{\sigma_{2t}} \quad ; \quad \beta_{3} = \frac{\sigma_{33}}{\sigma_{3t}}$$

Now,  $\epsilon$  is defined as the sum of 3 probability terms as :-

$$\varepsilon = \frac{V_{1} P_{1}}{1 - (1 - P_{1})\beta_{1}} + \left\{ V_{2} + \frac{V_{2} V_{1}}{\sigma_{1} (1 - (1 - P_{1}) \beta_{1})} \right\}^{*}$$

$$* \left\{ \frac{P_{2}}{1 - (1 - P_{2}) \beta_{2}} \right\} + \left\{ \frac{V_{1} (1 - P_{1}) \sigma_{13}}{\sigma_{1} (1 - (1 - P_{1}) \beta_{1})} \right\}^{*}$$

$$* \left\{ \frac{P_{3}}{1 - (1 - P_{3}) \beta_{3}} \right\} \dots \quad \text{Eqn (14)}$$

The cross-section used in Eqn.13 and Eqn. 14 are taken directly from p.402-406, Ref(23).

k<sub>inf</sub>:-

Having evaluated the above  $k_{inf}$  is given by  $k_{inf} = T^* \epsilon * p * f$ 

# 5.2.2 LEAKAGE AND keff

Since the material & geometric buckling have to be equal for a critical system  $B_g^2 = \frac{k_{inf}-1}{L_{th}}$  taking fast leakage into consideration:

$$k_{eff} = \frac{k_{inf} * exp (-BT)}{1 + L_{th}^{2} \cdot B^{2}} \dots Eqn (15)$$

In steady-state reactor operation,  $k_{eff} = 1.00$ 

# 5.2,3 CONTROL REQUIREMENT:-

The amount of Poison required is determined from the CODE by trial and error method for varying values of  $P_{\rm frac}$  such that the critical determinent (refer Eqn.63) is a minimum. This will be the steady-state value of Poison required to maintain criticality. The inbuilt reactivity of the core is determined by putting  $P_{\rm frac}=00$  and setting the core at room temperatures. The boron Poison required is evaluated by choosing a slightly higher value so that the reactor remains subcritical even in the cold condition.

### 5.2.4 TEMPERATURE AND PRESSURE EFFECTS:-

### (i) Thermal group constants:-

(a) The averaged thermal absorption and fission cross-sections are strong functions of temperature. Taking the Maxwellian distribution, they vary as

$$\sigma_{a}(T) = \frac{\sqrt{m}}{2} g_{a}^{(T)} (\frac{T_{0}}{T})^{0.5} * \sigma_{a} 2200$$
 Eqn.(16)

$$\sigma_{f}(T) = \frac{\sqrt{T}}{2} g_{f}(T) \frac{T_{O}^{O.5}}{T} * \sigma_{f}^{O.5}$$
 Eqn (17)

where,  $T_0 = 295.1 \text{ K}$  T = average fuel temperature  $g_a(T)$ ,  $g_f(T)$  are non- $\frac{1}{v}$  absorption and fission factors. respectively for deviation from Maxwellian distribution.

For materials other than fuel,  $g_a(T) = 1.0 \, \forall \, T$ The cross-sections for all materials have been corrected as above using following average temperatures:-

Moderator (in core ) ..... From Chapter-4 CODE.

Water (in reflector) ..... 280°E

Fuel temperature ..... From Chapter-4 CODE

Other materials in core ..... Average Coolant temperature

(b) The diffusion length for water is a strong function of temperature and pressure. An experimental value for  $L_{\rm th}$  . given by Deutsch ( p.92, Ref(22)) has been used:

$$\bar{L}_{th}(T,pr) = \frac{2.719}{9(T)} * (\frac{T+273.1}{295.1})$$

$$\frac{1.0614}{1+0.0614} \frac{1.0614}{(\frac{T+273.1}{295.1})^{0.5}}$$
Eqn (19)

where, pr = water pressure, psi T = water temperature, °C  $\Im(T) = \text{water density at p}_{r} \text{ and } T$ 

(c) For water,  $\sum_{\mathbf{a}} \propto$  N, number density, which in turn is  $\propto \Im(\mathbf{T})$  ;  $\sum_{\mathbf{a}} \propto \Im(\mathbf{T})$  .

As, S(T) = 0.93796 + 0.64448E-3\*T - 0.458271E-3 \*T<sup>2</sup> gm/cc Eqn. (20)

where, T= water temperature (for 2000psi pressurised water) .

So, 
$$\sum_{a} (T) = \Im(T) * (\frac{T}{T_{a}})^{0.5} * \sum_{a} (T_{0})$$

Next, to evaluate diffusion constant . D for water, we use the familiar equation

$$\bar{D} = L_{\text{fh}}^2 * \sum_{a} \dots Eqn (21)$$

We see that the  $\bar{\mathbf{D}}$  calculated in the above manner is reasonably accurate.

(ii) Fast group constants:-

(a) The neutron age,  $\tau$ , in water is not that much affected by temperature as pressure.  $\tau \propto \frac{1}{3^2}$ ; As temperature & pressure increases, density decreases thus increasing neutron age in water. We arrive at :

$$\tau \text{ (T,pr)} = \frac{\tau_0 * 0}{g(T)^2} \dots \text{Eqn.(22)}$$
where  $\tau_0 = 27 \text{ cm}^2$  is at atmospheric pressure  $\theta_0 = 1 \text{ gm/cc}$  and temperature of 22.1°C

(b) The fast neutron age in core is dependent on temperature in an indirect manner. A temperature increase results in a decrease of \$\frac{9}{2}\$, thus increasing the age. This has been elaborated in the subsection that follows.

### (iii) Heterogeneous Core constants:

(a ) In a heterogeneous lattice, the average absorption cross-section  $\widehat{\Sigma}_{as}^{\ *}$  is :-

$$\overline{\Sigma}_{as} = \sum_{afu} v_{fu} + (\sum_{am} + \sum_{ap}) v_{m} \neq \sum_{ass} v_{ss}$$
.. Eqn (23)

and 
$$\sum_{tr} = \sum_{trfu} v_{fu} + \sum_{trm} v_{m} + \sum_{trss} v_{ss}$$

 $\sum_{\text{trp}}$  being relatively very small may be neglected.

<sup>\*</sup> Hereafter subscript 's' stands for thermal/slow neutron parameters. Subscript 'f' stands for Fast neutron parameters.

(b) The extrapolation distance (E.D.) of the core is then

E.D. = 
$$\frac{0.71}{\sum_{tr}}$$
 .... Eqn(25)

(c) Since average diffusion coefficient,  $D_s$ , of Latice varies inversely as  $\sum_{tr}$ , it follows from Eqn.(24) that :-

$$\frac{1}{\bar{D}_{S}} = \frac{V_{fu}}{D_{fu}} - \frac{V_{fu}}{D_{M}} + \frac{V_{ss}}{D_{ss}}$$
(Or)  $\bar{D}_{s} = \frac{1}{\frac{V_{fu}}{D_{fu}} + \frac{V_{M}}{D_{M}} + \frac{V_{ss}}{D_{ss}}}$ 
Eqn (26)

(a) Now  $L_s$  , the thermal diffusion length of core, is determined from Eqn (26) & (23) :-  $L_s = \frac{D_s}{E_{s-1}} \qquad \qquad Eqn (27)$ 

(e) The neutron age in the core is determined from experimental values for age of a W-H<sub>2</sub>O mixture (p.206 Ref.(23)). In the above case, a change in temperature (& pressure) has the effect of reducing the atom density of water relative to fuel which is equivalent to increasing the metal-to-water ratio in volume.

As  $\Im$  is given by Eqn.20, the ratio of U-H<sub>2</sub>0 mixture, say,  $X = \frac{\text{Vol,of U}}{\text{Vol. of H}_20} * \frac{1}{\Im(T)}$ 

Using Fig 6.4 of ref  $^{(23)}$  , we arrive at the following correlation for age,  $\tau_1$  :-

$$\tau_1 = 19.8 + 12.5 * X - 5.0 * x^2$$
, for  $X \le 0.9$   
= 27.0 + 6.27 \* (X-0.9), for  $X > 0.9$ 

(f) In Eqn (26)  $D_m$  is taken from Eqn (21) but  $D_{SS}$ ,  $D_p$  and  $D_s$  are still unknown. These are individually calculated as :-

$$D_{s} = \frac{1}{3(\bar{\Sigma}_{2} + \bar{\Sigma}_{s}(1 - \mu_{0}))}$$
 Eqn (28)

(g) Finally, the fast diffusion constant,  $D_f$  in core since hydrogen scattering cross-section varies significantly with neutron energy, an artifice is used for core transport cross-section. Thexausing

$$\sum_{\text{af}} = \frac{\frac{\text{N I}_{\text{eff}}}{\text{eff}}}{\ln(\frac{E_{\text{O}}}{E_{\text{m}}})}$$
 Eqn (29)

and Eqn.(28),  $\bar{D}_{\rm f}$  is calculated. All the above calculations are shown in Appendix A5-1.

#### 5.2.5 HETEROGENEOUS VERSUS HOMOGENEOUS :-

We are now in a position to comprehend what effects would we have incurred had a homogeneous treatment of the reactor been done. As  $\frac{1}{2T} > 1$ , f (hetero)  $\left\langle \text{ f(homo)} \right\rangle$  due to the self-shielding effect of the fuel rods. However, p (hetero)  $\left\langle \text{ p(homo)} \right\rangle$  p(homo) as the above effect reduces the number of neutrons that are parasitically absorbed by fuel resonances. Thus, decrease in f is more than offset by increase in p . So, (f.p) hetero  $\left\langle \text{ (fp)} \right\rangle$  nomo.

The fission neutrons pass through a region of pure fuel where they are likely to induce fast fission, before emanating to the moderator. Hence, ( $\epsilon$ ) hetero  $\stackrel{>}{>}$  ( $\epsilon$ ) homo. This effect is not that pronounced as the other factors above.  $^{\eta}$  T does not, however, change.

In view of the above inequalities, k<sub>inf</sub> for heterogeneous lattices is greater than its homogeneous equivalet. A homogeneous treatment, though much simpler would consequently give erreneous results.

### 3. FLUX DISTRIBUTION

The thermal reactor consists of a heterogeneous multiplying core surrounded by a non-multiplying water reflector. Since the core consists of a closely-packed square lattice of fuel rods, it can be considered homogeneous for determining flux distributions in core & reflector. Despite its limitations, 2-group approximation has been used, as it is the simplest that will give reasonably accurate results for multi-region calculations.

The diffusion equations for fast & slow neutrons is given by :-

$$D_{f} \nabla^{2} \varphi_{f} - \sum_{f} \varphi_{f} + \frac{k_{inf}}{p} \sum_{s} \varphi_{s} = 0 \dots \text{Eqn (30)}$$

$$D_{s} \nabla^{2} \varphi_{s} - \sum_{s} \varphi_{s} + p \sum_{f} \varphi_{f} = 0 \dots \text{Eqn (31)}$$

where, all symbols have their usual meanings ,

 $\Sigma_{as}$  = thermal absorption cross-section

 $\Sigma_{rf}$  = slowing-down (fast removal) cross-section.

In core,  $k_{inf}$  1 and in reflector  $k_{inf} = 0.0$ 

The solution of Eqns (30), (31) are solutions of wave equations

$$\nabla^2 \varphi_{\text{f}} + B^2 \varphi_{\text{f}} = 0$$

$$\nabla^2 \, \mathcal{Q}_{s} + B^2 \, \mathcal{Q}_{s} = 0$$

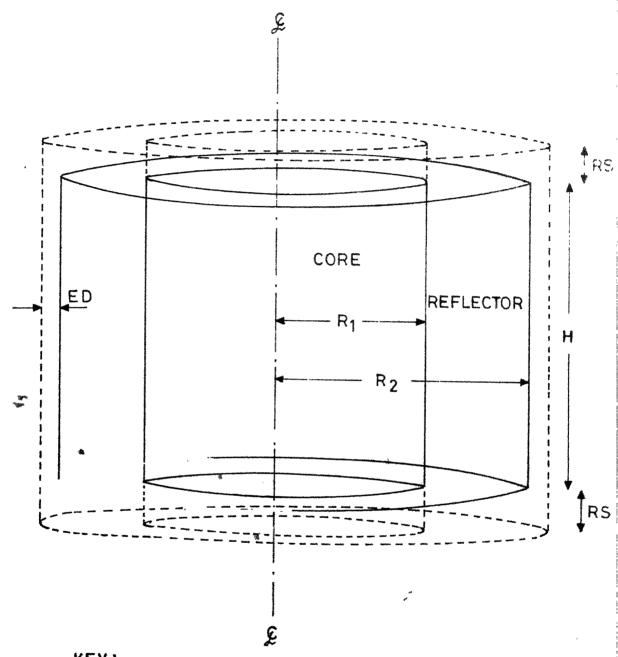
This implies the coupling of the solutions by the condition that coupling-coefficient, S , between fast & slow fluxes is

The criticality condition should be satisfied;

i.e. 
$$k_{\text{Gif}} = 1 = \frac{k_{\text{inf}}}{(1 + \frac{B^2}{x_s^2})(1 + \frac{B^2}{x_f^2})}$$
.... Eqn. (33)  
where  $x_s = 1/L_s$   
 $x_f = 1/L_f$ 

We shall use subscripts '1' for core and '2' for reflector.

Eqn (33) defines 2 values for B (refer fig.5.2) thus :-
$$B_{1}^{2} = \frac{-(x_{1f}^{2} + x_{1s}) + \sqrt{(x_{1f}^{2} + x_{1s}^{2})^{2} + 4x_{1f}^{2}(k_{inf}-1) \cdot x_{1s}^{2}}}{2}$$



KEY:

ED - Extrapolation distance

RS — Reflector savings

FIG. 5.2 CORE-REFLECTOR CONFIGURATION.

$$B_{1}^{'2} = \frac{-(x_{1f}^{2} + x_{1s}^{2}) - \sqrt{(x_{1f}^{2} + x_{1s}^{2})^{2} + 4 \cdot x_{1s}^{2} \cdot x_{1f}^{2} \cdot (k_{inf}^{-1})}}{2}$$

$$\dots \quad \text{Eqn. (35)}$$

$$B_{2}^{2} = -x_{2s}^{2} \qquad \dots \quad \text{Eqn. (36)}$$

$$B_2^{'2} = -x^2_{2f}$$
 ..... Eqn.(37)

Considering wave-equations are separable in both core & reflector,

$$\emptyset = \cos\left(\frac{\pi}{H + 2RS}\right) * F(r) \dots Eqn. (38)$$

where, RS = reflector saving\* =  $(\frac{D_{1S}}{D_{2S}})$  L2s  $(1-\exp(\frac{R_2-R}{L_{2S}})$  ) F(r): is the solution of the equation

$$\frac{d^2F}{dr^2} + \frac{1dF}{rdr} + (B^2 - (\frac{\pi}{H + 2RS})^2) *F = 0$$

since  $B^2$  has 2 values in both core & reflector (given by Eqns(34) to (37)), to define F(r) completely, a total of 4 equations will have to be satisfied:

$$\frac{d^2F_{1f}}{dr^2} + \frac{1}{r} \frac{dF_{1f}}{dr} + 1^2 F_{1f} = 0 \dots Eqn. (39)$$

$$\frac{d^2F_{1f}}{dr^2} + \frac{1}{r} \frac{dF_{1f}}{dr} - m^2 F_{1f} = 0 \dots Eqn (40)$$

$$\frac{d^{2} F_{2f}}{dr^{2}} + \frac{1}{r} \frac{d^{2} F_{2f}}{dr} - \mu_{s}^{2} F_{2f} = 0 \dots \text{ Eqn (41)}$$

<sup>\*</sup> From p.69, ref(24) .

$$\frac{d^2 F_{2f}}{dr^2} + \frac{1}{r} \frac{dF_{2f}}{dr} - \frac{\mu^2}{s} \cdot F_{2f} = 0 \quad \dots \quad \text{Eyn (42)}$$

Identical 4 more equations are there for  $F_{1s}$  and  $F_{2s}$  as well.

1, m,  $\mu_s$  and  $\mu_f$  are all +ve constants :-

$$= B_1^2 - (\frac{\pi}{H + 2RS})^2 \qquad Eqn (43)$$

$$m^2 = -B_1^{2} - (\frac{\pi^2}{H + 2PS})$$
 ..... Eqn (44)

$$\mu_{\epsilon}^{2} = -B_{2}^{2} + (\frac{\pi}{H + 2RS})^{2}$$
 ..... Eqn (45)

$$\mu_s^2 = -B_2^{\tau^2} + (\frac{\pi}{H + 2RS})^2$$
 ..... Eqn. (46)

The solutions of Eqns (39) to (42) are Bessel's functions. The complete solutions are as under :-

### In core

$$F_{1s}(r) = A J_0(lr) + C J_0(mr)$$
 ..... Eqn.(47)

$$F_{1f}(r) = A \cdot S_1 \cdot J_0(lr) + CS_1 \cdot I_0(mr) \dots Eqn (48)$$

### In reflector

$$F_{2s}(r) = E \cdot I_{O}(\mu_{s}r) + G \cdot K_{O}(\mu_{s}r) + H \cdot I_{O}(\mu_{f}r) + M \cdot K_{O}(\mu_{f}r)$$
..... Eqn. (49)

$$F_{2f}(r) = S_2 * (H \cdot I_0 (\mu_f r) + M \cdot k_0 (\mu_f r)) \dots Eqn. (50)$$

where  $S_i$  's given by Eqn. (32 ) are :-

$$S_{1} = \frac{\sum_{1 \text{as}} + D_{1} \cdot B_{1}^{2}}{P \cdot \sum_{1 \text{rf}}} \qquad Eqn (51)$$

$$S_{1} = \frac{\sum_{1 \text{as}} + D_{1} \cdot B_{1}^{2}}{P \cdot \sum_{1 \text{rf}}} \qquad Eqn (52)$$

$$S_{2} = 0.0 \qquad Eqn (53)$$

$$s_2' = \frac{\sum_{2as + D_{2s} B_2'}}{\sum_{2rf}}$$
 .... Eqn (54)

Eqns. (47) to (50) contain 6 unknown constants A, C, E, G, H and M. These can be determined by the following boundary conditions:-

$$F_{2f}(R_2) = 0$$
 ..... Eqn (55)

 $F_{2s}(R_2) = 0$  ..... Eqn (56)

 $F_{1f}(R_1) = F_{2f}(R_1)$  ..... Eqn (57)

 $F_{1s}(R_1) = F_{2s}(R_1)$  ..... Eqn (58)

 $D_{1f}\frac{d F_{1f}(R_1)}{dr} = D_{2f}\frac{d F_{2f}(R_1)}{dr}$  ..... Eqn (59)

 $D_{1s}\frac{d F_{1s}(R_1)}{dr} = D_{2s}\frac{d F_{2s}(R_1)}{dr}$  ..... Eqn (60)

Applying Eqns (55), (56) to (49), (50) gives

$$E = -G \cdot \frac{K_0 (\mu_{s} R_2)}{I_0 (\mu_{s} R_2)}$$
 Eqn. (61)

$$H = - M \cdot \frac{k_0(\mu_f^R_2)}{I_0(\mu_f^R_2)} \dots Eqn. (62)$$

using Eqns (57) to (62) in (47) to (50), we arrive at the following :-

<u> </u>	С	G	M			T.	
	Y12	Y13	Y14		0		
Y21	<b>Y2</b> 2	¥23	Y24		0	The state of the s	
Y31	Y32	Y33	Y34		0	Eqn.(63)	
Y41	Y42	Y43	Y44		0	1	
····						ŧ	

where, Y<sub>ij</sub> 's above are elements of the critical determinent as given in the CODE ( line nos 23900 to 25900 of main program )." , which coldings in relieve on in the only which has

given by Eqn(63) = 0; only then will A,C,G & M will have non-trivial values as the 4 equations are homogeneous.

Next, the first 3 equations of Eqn(63) are taken and constants C, M and G evaluated with respect to A using Crammer's rule. Finally, A is determined by the following method. Since the average thermal flux in the core is given by the relation:-

$$\varphi_{\text{sav}} = \frac{1}{\pi R^2 H} \int_{-H/2}^{H/2} \left\{ A \cdot J_0(lr) + C \cdot J_0(mr) \right\} \cdot \cos(\frac{z\pi}{H + 2RS}).$$

from A 3.1- 3, this works out

$$\overline{p}_{\text{sav}} = A \left\{ \frac{2J_{1}(1R_{1})}{1R_{1}} + 2\left(\frac{C}{A}\right) \frac{I_{1}(mR_{1})}{mR_{1}} \right\} * \left\{ \frac{2(H+2RS)}{\pi H} \cdot \sin \left(\frac{\pi H}{(H+2RS)\cdot 2}\right) \right\}$$

Hence, 
$$\frac{A}{\overline{g}_{sav}} = \frac{1}{2J_{\frac{1}{1}}(1R_{\frac{1}{1}}) + 2(\frac{C}{A})} \times \frac{H}{\frac{1}{mR_{\frac{1}{1}}}} \times \frac{H}{2(H-2RS)Sin(\frac{\pi H}{2(H+2RS)})}$$

.... Eqn (64)

It should be recalled that ( $\frac{C}{A}$ ) in Eqn.(64) is known and we obtain 'A' as the number of times of  $\emptyset_{\text{SaV}}$ . From this, the other 5 constants can be evaluated and since all constants in Eqns (47) to (50) are now known the radial flux functions in core & reflector can be easily sketched and is shown in Fig. 5.3

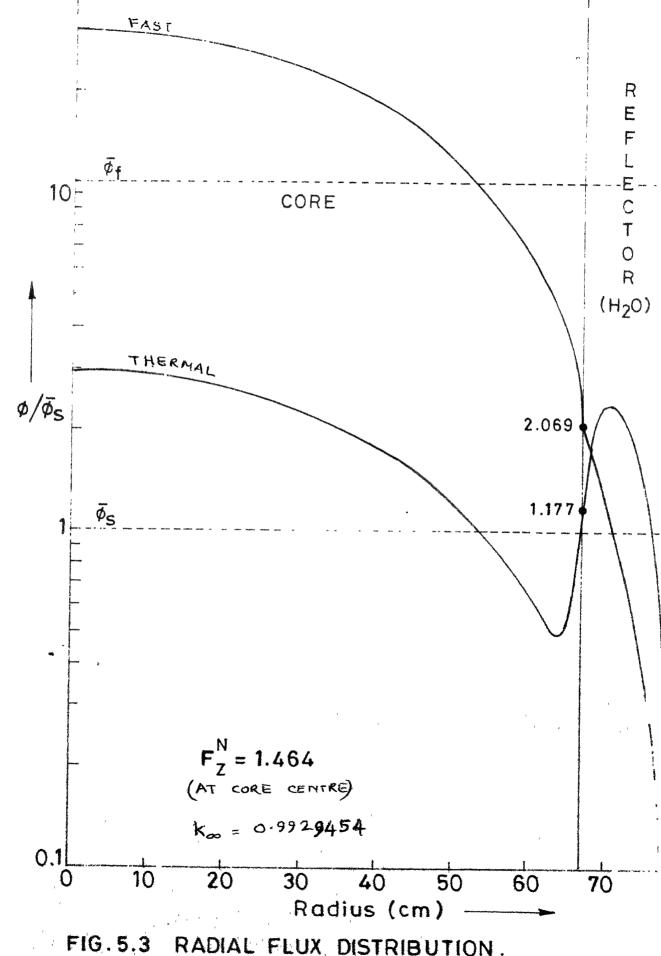


FIG. 5.3 RADIAL FLUX DISTRIBUTION.

### 5.4 RESULTS

A simple one group calculation of  $k_{\rm inf}$  versus number den. ratio of U<sup>28</sup> & water as per p.306, ref(23), gives a maximum  $k_{\rm inf}$  at a ratio of 0.156 for the nuclear parameters chosen; this implies a pitch of 2.12 cm for a fuel rod diameter of 0.858 cm as a core power density of 24.52 MW/m<sup>3</sup>. This is clearly undesirable for the compactness desired. However, a pitch of 1.30cm chosen, though resulting in lesser moderation is a compromise, with the operating point falling only 8% from the  $k_{\rm inf}$  peak.

Core criticality has been achieved at k<sub>eff</sub>=0.992945 with the aid of a 10.99 cm thick water reflector. The various intermediate parameters, criticality determinent & others are shown in file CHECK-OUT( p.39 of computer print-outs). Other nuclear parameters like cross-sections, etc. are displayed in file K.OUT (p.37-38 of Print-outs). Fig 5.3 maps the radial flux variation; a rise in thermal flux at core edge due to moderation by the water reflector is clearly seen.

Results of reactor control calculations (refer chap 7 evolves a volumetric Poison fraction of 0.92148E-3 for a clean reactor with a maximum of 2.35E-3 (with all rods in) to drive the reactor subcritical by 5%  $\Delta$ k/k in the cold condition. File PSN.OUT (p.40 of print-outs) lists some parameters discussed later in Chapter 7.

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### CHAPTER - 6

### REACTOR SHIELDING

# RESUME

- 6.1 INTRODUCTION
  - 6.1.1 Types of Shielding
  - 6.1.2 Shielding Requirements
- 6.2 SALIENT FEATURES
  - 6.2.1 Shielding Design Characteristics
  - 6.2.2 Dose Rates Permissible
  - 6.2.3 Optimization Techniques
- 6.3 RADIATION ATTENUATION IN SHIELD
  - 6.3.1 Nautron attenuation calculations
    - (i) Fast neutrons
    - (ii) Thermal neutrons
  - 6.3.2 Gamma Ray Attenuation calculations
    - (i) Core gammas
    - (ii)Capture gammas
  - 6.3.3 Emissions from reactor effluents
  - 6.3.4 Total Dose rates
  - 6.3.5 Weights of shielding materials
- 6.4 COMMENTS

Shielding of a marine

### 6.1 INTRODUCTION

reactor is of far greater importance than its landbased counterparts. Here, the peculiar space, weight and dose rate limitations require an optimization study concerning the shielding materials and the differential shielding thicknesses,

- on the massis of dose rate mapping. Reactor shielding is essential to :-
- (a) Not only protect the personnel working in close proximity to the reactor system but also to
- (b) Reduce radiation levels in the vicinity of instrumentation and other equipment that may be damaged by radiation;
- (c) Reduce the induced radioactivity of reactor components
  that may need to be serviced during shutdown (like primary
  loop components)
- (d) Prevent excessive radiation induced heating of the pressure vessel (PV).
- (e) Limit the neutron embrittlement of the PV.

The marine reactor shielding design would require a careful study of propagation of radiation through matter (i.e. shield material), system analysis of activity production and release in reactor effluents. It also requires other aspects of the ship & reactor design such as general plant layout & structural studies (not done here). The aim is to

utilize the large amounts of materials needed for shielding also for structural purposes to optimize on weight. For analysis a \*MARINE REACTOR SHIELDING CODE has been developed which has been referred to throughout.

### 6.1.1 TYPES OF SHIELDING

There are 3 Key factors in shielding design-cost, shield volume & shield weight. Any one of these may decide the type of shielding required. There are three types of shielding:-

- (i) Unit Shield that completely surrounds the reactor, like in land-based reactors.
- (iii) Shadow Shield- that shields only the crew and important instrumentation, like in aircraft or space reactors.

# 6.1.2 REACTOR SHIELDING REQUIREMENTS

The control of radiation from a ship-board reactor presents, in particular, the 2 following problems of design:-

- -shielding from neutron & gamma sources in a compact geometry layout.
- -management of safe release of gaseous activity to satisfy

the requirements of rapid access to the reactor containment after shutdown. Among these, only the former has been studied to some depth.

The scheme of reactor shielding revolves primarily around these 5 considerations:-

- (a) Slowing down the fast neutrons (an').
- (b) Capture of slowed down on1.
- (c) Determining the source of the secondary gamma radiations formed as a result of various neutron interactions in shield materials.
- (d) Attenuation of all forms of gamma radiation.
- (e) Determining the total dose rate of radiation emerging from the shield materials.

Let us examine the above points; for high energy neutrons, use of elements of moderate or high mass number is effective, as they are able to reduce their energies through inelastic scattering. Since elements of low mass numbers are the best moderators, H<sub>2</sub> in the form of water is used as a shield constituent for slowing down intermediate neutrons ( < 1 MeV). Hence a combination of a moderately heavy element like steel with water is used.

As a general rule, most of the V-rays originating from the core get absorbed in the shield region .

nearer to the core itself. It is the secondary  $V_{-}$ rays, however, (emitted due to thermal neutron capture within the shield) along with a tiny fraction of the core gammas that control the shield thickness required. The neutron attenuating material to an extent also serve this purpose. However, as  $V_{-}$ ray relaxation lengths are inversely proportional to material density, additional material of higher density (like Lead) is incorporated to attenuate the higher energy  $V_{-}$  rays.

A word about the 'thermal shield'. This is basically to safeguard the PV. High gamma flux from the core leads to very high heat generation rates in any structural elements placed there. If it were the PV, then the resulting large temperatures & thermal stresses when added to the already present high mechanical (pressure) stresses, would bring the total stress on it (PV) to an unacceptably high level. Hence, a thermal shield consisting of layers of stainless steel and water is placed between the core & PV. The arrangement is as shown in Fig. 6.1. The steel has a high melting point & excellent thermal conductivity. Energy is absorbed by attenuating V-radiation and inelastic scattering of fast neutrons. This heat is immense & is removed by the coolant flowing into the reactor core through these shield layers, thus contributing to the neft available energy from core.

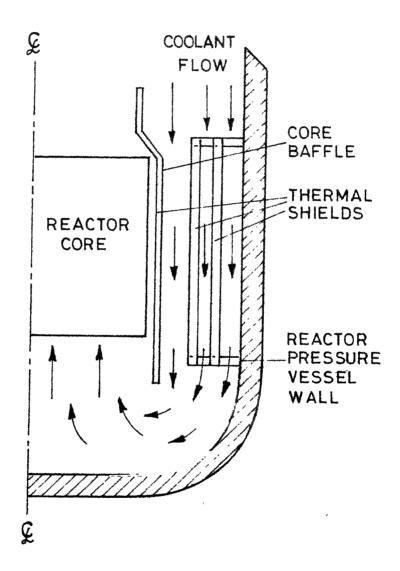


Fig. 6.1
Thermal shield in the PWR.

The core- $\sqrt{\ }$  energy is attenuated from  $\sim 10^{17}$  MeV/cm<sup>2</sup>-3 to  $\sim 10^9$  MeV/cm<sup>2</sup>-3 and the fast neutron flux from 0.28 x  $10^{14}$  #/cm<sup>2</sup>-s to 0.16 x  $10^9$  #/cm<sup>2</sup>-s before impinging onto the PV. Thus high thermal stresses and neutron induced embrittlement (by high-energy neutrons) is effectively reduced.

### 6.2 SALIENT FEATURES

## 6.2.1 SHIELDING DESIGN CHARACTERISTICS

The scheme used is as follows:-

- (a) Thermal shield: stainless steel (85 347) and water alternately used.
- (b) Pressure Vessel: made of carbon steel, as it is required to withstand high mechanical stresses.
- (c) Primary shielding: also called Neutron Shield Tank(NST)
  surrounds the PV-Made of carbon steel
  & water alternately, it has important
  mechanical support functions besides
  shielding, like supporting the entire
  PV,CRDM, Cooling ducts, part of
  primary piping, etc and also to resist
  shock load acting on the ship. The
  concentric layers of steel and water
  makes an optimal shield for both
  neutrons &V -rays. Lead is not used
  here due to its lower melting point
  & poorer mechanical properties.

(d) Secondary Shielding - It surrounds the containment vessel & the complete primary loop (steam generator, associated piping, primary pump, etc.). It attenuates to the allowed duse, radiations coming from coolant loops ( reactor effluents) - mainly  $\hat{V}$ -rays from  $o^{16}$  activation) and those escaping from primary shield. It's made up of one layer each of Lead & Polyethone. Concrete due to its much larger bulk for the same effectiveness has not been used. Study reveals that use of Boron based alloys here do not substantially aid in reducing the shield weight/bulk. Table 6.2 shows the thicknesses of the above shield materials evolved from the shielding CODE.

#### 6.2.2 PERMISSIBLE DOSE RATES

The occupational individual accummulated dose is limited by the well known equation D = 5.(N-18) rems, where N is age of the person. This implies a maximum dose rate of 2.5 mrem/hr. For personnel working in nuclear sites the limitation however is 1.5 rem/year or 0.75 mrem/hr. This is the design consideration in our shielding calculations. However a total (29) dose of 12 rem under emergency conditions has been allowed with doses excess of 5 rems being adjusted over the next 5 years.

TABLE 6.2

OPTIMAL SHIELD DESIGNED

SHIELDING TYPE	MATERIAL	THICKNESS (CMS)
REFLECTOR	WATER	10,99
THERMAL SHIELD	Stainless Steel (Core Baffle ) Water	1.27 13.90
-	Stainless Steel	3.00
	Water	3.50
	Stainless Steel	8.00
	Water .	10.25
PRESSURE	CARBON	10.00
VESSEL .	STEEL	12.00
	Water	32,00
PRIMARY	Carbon Steel	16.00
SHIELDING	Water	10.00
	Carbon Steel	19.00
	Water	31.50
EMPTY SPACE (for housing components of primary loop)	Air ,	200,00
SECONDARY	Lead	15.10
SHIELDING	Polyethene	13.70

CORE RADIUS

67.145 cms.

TOTAL SHIELDING OUTER

30.67 ft.

DIAMETER

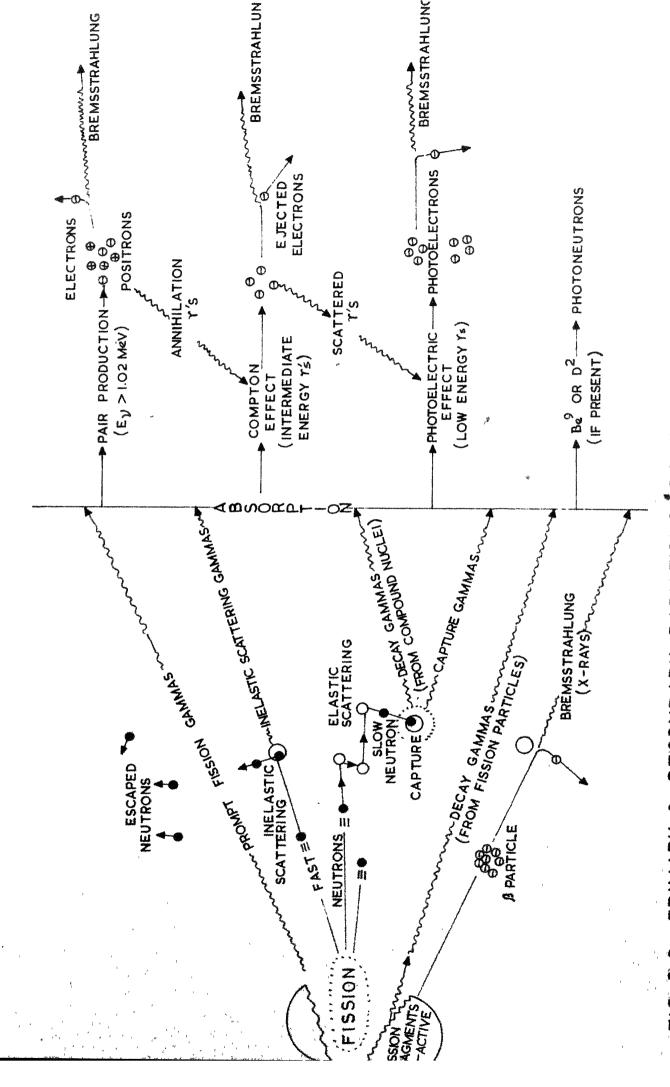
### 6.2.3 OPTIMIZATION TECHNIQUES

The search for the optimum shield consists in evaluating the weight of various possible shield designs giving (28) same dose rates at specified points. B. Chinaglia , has sketched weight variation  $\mathbb{Z}^{W}$  for the optimum configuration, as a function of neutron  $(D_n)$  to total dose  $(D_n + D\gamma)$  i.e.  $D_n/(D_n + D\gamma)$ . The curve proves that the minimum weight is found for  $D_n/(D_n + D\gamma)$  = 0.10. This gives the lead & polyethene thicknesses as mentioned.

The optimum primary shield with respect to weight is composed by laminations of heavy metal located at about the middle of NST. No strong difference between the use of iron only or iron and lead is found. Hence only carbon steel is used.

#### 6.3 RADIATION ATTENUATION IN SHIELD

The radiation from core includes  $\alpha$ ,  $\beta$  and  $\sqrt{-r}$  and reactions of various energies, fission fragments, protons &  $\alpha$ -particles from (n,p) &  $(n,\alpha)$  reactions and neutrines. Unly neutrons & gamma rays are considered for shielding design as they are most penetrating. The primary and secondary radiations from the core have been briefly summed up in Fig. (6-3). We shall consider neutrons & $\sqrt{-r}$  are separately.



PRIMARY & SECONDARY RADIATIONS SCHEMATIC

#### 6.3.1 NEUTRON ATTENUATION CALCULATIONS

The theory of neutron penetration through thick layers is different from ordinary theories of neutron diffusion used for criticality calculations where the interest is in the behaviour of average particles. But here, the interest is in those exceptional high-energy particles that do not undergo any interaction throughout the shield materials. The average neutrons that do the normal things are not very important as they stand no chance of getting for into the shield.

Neutrons are absorbed in the shield in 2 distinct stayes. First, high energy neutrons are slowed down by elastic/inelastic collisions; these slowed-down neutrons are then captured in shield materials easily as capture cross-secctions are high at low energies. We shall now consider these 2 stages separately.

#### (i) FAST NEUTRONS

### Theory of attenuation

These attenuate as per the following 3 forms:-

(a) Elastic Scattering- Here, neutron K.E. is lost by collision with target nuclei. Dependent on scattering nuclei mass, it is the most important form of energy loss for light nuclei like H, where a single collision may result in the removal of the neutron.

From 1.eV to 10KeV, this form is dominant.

- (b) Shadow Scattering: This occurs at energies greater than
  5 to 10 MeV wherein the neutron acts as a
  wave and is diffracted about the target
  nucleus. It occurs only when neutron wavelength is lesser than nuclear radius. At
  large neutron energies, its cross section
  approached R<sup>2</sup>, geometrical nuclear crosssection.
- (c) Inelastic Scattering: Its importance is that the incident neutron is strongly degraded since it loses the recoil energy of target nucleus plus energy equivalence of inelastic √-rays emitted. This is very important for heavy nuclei where allowable energy levels are numerous and smaller\_distances between ground state & first energy level. Its threshold varies from 6 MeV for ¢2 to few tenths—of—an MeV for Uranium. At high neutron energies, its cross—section also approaches πR².

In marine reactor design, we are interested in minimum weight. Limiting values of both (b) and (c) above approach  $\pi R^2$ . Hence total cross-section (T) approaches  $2\pi R^2$  at high neutron energies. As nuclear radius R=1.5 x  $10^{-13}$   $\star$  A<sup>1/3</sup> where A is mass number of the nucleus, the total mass cross-section becomes:

$$\frac{\sum_{T}}{Q} = \frac{6.022 \times 10^{23}}{A} (2\pi R^{2}) = \frac{0.0852}{A^{1/3}} cm^{2}/g$$

which means light elements like  $H_2$  give minimum shielding weights, justifying what was stated previously.

#### Equations used

Neutron flux follows the exponential attenuation law

$$\mathscr{Q}_{f}(x) = \mathscr{Q}_{\mathscr{C}} \cdot \exp(-\sum x)$$

where x = distance from source

Ø<sub>c</sub> = source strength

 $\sum$  = effective removal macroscopic cross-section

For 2 to 12 MeV neutrons

$$\sigma = 0.35 \times A^{0.42}$$
 barns

of material with mass no. A. This is used to evaluate  $\sum$  of unlisted materials like steel (refer Appendix A6.1) Applying inverse square law for spherical attenuation and considering  $\emptyset_{\vec{F}}(R)$  as flux at core edge,

$$\varphi_{\mathbf{f}}(\mathbf{x}) = \varphi_{\mathbf{f}}(\mathbf{R}) \cdot \exp(-\Sigma \cdot \mathbf{r}) \cdot \mathbf{R}^2 / \mathbf{r}^2 \text{ for } \mathbf{r} > \mathbf{R}$$

As more than one layer is present, the exponential term for 'n' layers gets modified to

$$(\sum_{r}) = \sum_{i=1}^{n} \sum_{i \neq i} t_{i}$$
 where  $\sum_{i=\text{ cross section }, t_{i}=\text{ thickness, of layer } i$ 

The attenuation prior to the P.V. wall occurs in the water and steel of thermal shield region. Experimental Data (p.153,(26)) for this region show that when build-up is considered.

point kernel can we represented by the sum of 2 exponential terms. For a large planar source of core, flux distribution in x cms of water,  $\emptyset_+^*$  (x), is

The attenuation of fast neutrons thro ugh z cms. of steel followed by x cms of water is then well approximated by :-

$$\emptyset_{f}(z,x) \stackrel{\sim}{=} \emptyset_{f}(x) * E_{1}(\Sigma_{s} \cdot z)$$

Where  $\Sigma_{ss}$  removal cross-sec for steel. Flux thus obtained is multiplied by  $\frac{R^2}{(R+z+x)^2}$  to account for the spherical geometry.

### Method used

The method used in SHIELDING CODE is 'Diffusion Removal Method'. Here, the basic assumptions are :-

- (1) The penetrating component of source neutrons consists of high energy neutrons that suffer only a small energy loss and uncollided neutrons.
- (2) Neutrons suffering large energy loss are regarded as being

removed from the beam.

(3) The removed neutrons are degraded in energy according to diffusion theory and don't travel significantly from point of removal.

The equations explained above have been used in the code to obtain the fast flux at every layer. The flux attenuation through the shield material is sketched in Fig. (6.4).

## (ii) THERMAL NEUTRONS

The source of thermal neutrons are :-

- (a) thermal flux emanating from the core.
- (b) neutrons removed from the fast-flux beam. These removed neutrons, forming local sources can be adequately described by diffusion theory. This source intensity, is  $\emptyset_{\mathbf{f}}(\mathbf{r}) * \sum$  . In any layer a distance L from core centre,

$$\varphi_{f}(r) = \varphi_{f}(L) * L^{2}/r^{2} * \exp(-\sum(r-L))$$

where  $\emptyset_{f}(L)$  = fast flux at inner face of the layer and r > L.

These neutrons can then be introduced into the highest energy group of an appropriate set of multigroup diffusion equations to calculate the lower energy neutron distributions. Here,

only 2 group ...

theory has been assumed. Hence, all above neutrons are assumed thermalized. (This only results in slightly higher dose rates).

If  $\phi_s(r)$  is the slow flux at any radius r,

$$\text{D}_{s}^{2} \not g_{s}(r) - \sum_{as} * g_{s}(r) + g_{f}(r) * \sum_{as} = 0$$
leakage term absorption local source term.

where  $D_s$  = diffusion constant of layer  $\sum_{as}$  = thermal absorption cross-section.

$$(\text{or}) \nabla^2 \mathscr{I}_{S}(r) - \overline{c}^2 \mathscr{I}_{S}(r) + Q = \frac{-\sum (r-L)}{r^2} = 0$$
where,  $c^2 = \sqrt{\sum_{as}/D_s}$ 

$$Q = \mathscr{I}_{F}(L) \cdot L^2$$

Evaluating for  $\nabla^2 = \frac{1}{r^2} \cdot \frac{d}{dr} (r^2 \underline{d})$  (spherical coordinates, considering only radial variation)

$$\emptyset_{S}(r) = -\frac{Ae^{-Cr}}{2 cr} + \frac{Qe^{\sum L}}{2 cr}$$
 (c- $\sum$ ).  $E_{1}(y)_{e}$  cr  $-E_{1}(x)_{e}$  -cr (refer Appendix A6-3)

where, 
$$x = (c-\Sigma)r$$
,  $y = x/(1+2c/(c-\Sigma))$ 

As 
$$e^{-cr} < e^{cr}$$
 we modify as  $\emptyset_S(r) = \frac{Ae^{-cr}}{2cr} + \frac{Q e^{L}}{2cr} (c-\Sigma) \cdot E_1(y) e^{cr}$  ...eqn (1)

This equation is difficult to evaluate. As the effect of Inverse square law is much lesser than exponential attenuation within a layer, the distance attenuation is neglected within the layer for  $\emptyset_S(r)$  evaluation. This is a resonable approximation if layer thickness  $\langle\langle L.$ 

Now diffusion equation reduses to :-

$$\nabla^{2} \, \emptyset_{s}(r) - c^{2} \, \emptyset_{s}(r) + Qe^{-\sum r} = 0$$
where, 
$$Q = \frac{\sum \sum L}{D_{s}} \, \emptyset_{f} (L)$$

The solution of this equation (refer Appendix A6.3) is:-

$$\varphi_{s}(r) = \frac{Ae^{-cr}}{r} + \frac{Qe^{-r}}{r} \left( \frac{r}{c^{2} - \Sigma^{2}} - \frac{2}{(c^{2} - \Sigma^{2})^{2}} - \right)$$

which is easily solvable; flux thus obtained is multiplied by  $L^2/r^2$  for distance attenuation. It must be mentioned that this method gives a slightly higher value for  $\emptyset_s(r)$  than Equation (1).

The thermal flux within every layer is thus obtained & has been mapped in Fig. 6.4. These flux values will be required later to evaluate the capture gamma-ray sources (local) within the snield material.

#### 6.3.2 GAMMA RAY ATTENUATION CALCULATIONS

#### THEORY OF ATTENUATION:

Depending on the  $\sqrt{\ }$ -energy and absorber mass-number, the 3 absorption processes of interest are photoelectric effect. Compton scattering and pair production (in MeV region). Secondary effects such as  $\sqrt{\ }$ - induced reactions, coherent scattering and Raman scattering have not been considered as their effects are negligible. For illustration,  $\sqrt{\ }$ -ray cross-section is shown as a function of energy for Iron in Fig. 6.5.

(a) Photoelectric effect: Most important absorption at low energies (<1 MeV) Energy is transferred to orbital electrons through Einsteins equation:

$$E = hy = w + \frac{1}{2} mv^2$$
Total energy work  $KE$  of electron function

It is a true absorption process as the V-ray gives up all its energy in one interaction. The cross-section for this interaction is proportional to  $z^n/$   $E^3$  where Z= Atomic number, E=V-ray energy in MeV.

& n = 3 to 5 depending on ray energy.

(b) Compton Scattering: Occurs at high energies. Here, √ -rays undergo billiard-ball type collision with electrons, according to compton's equation:

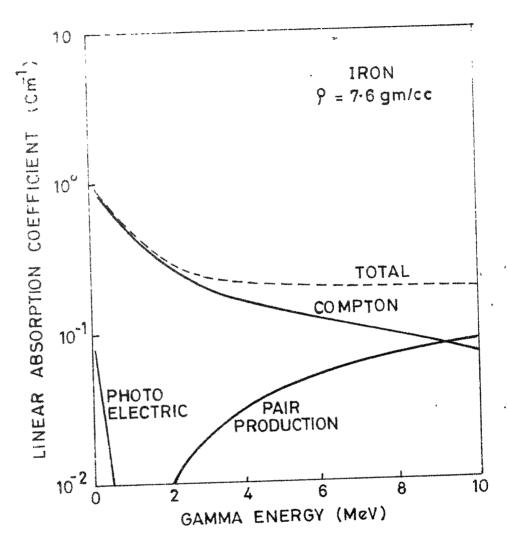


FIG. 6-5. GAMMA-RAY CROSS-SECTION FOR IRON.\*

\* Fig. 5.3, ref (26)

It is not a pure absorption process as fractional energy lost depends on incident angle. Its cross-section is proportional to  $\mathbb{Z}/\mathbb{E}$  ( nearly constant for all elements (except  $H_2$ ) where  $\mathbb{Z}/\mathbb{E}=0.5$ ).

(c) Pair production: At higher  $\sqrt{\ }$  energies, this starthing phenomenon occurs wherein under the effect of the coulomb field of the nuclues, a high  $\sqrt{\ }$  energy (>1.022 MeV) can give rise to an electron pair-positron & electron, with any excess energy appearing as particle kinetic energy. Positron always gets annuilated by combination with an electron giving 2,0.511 MeV  $\sqrt{\ }$ -rays. Its cross-section is proportional to  $Z^2$  (E-1.022). It is a true absorption process as annihilation radiation is soft, emitted isotropically and attenuated easily.

The above 3 process are all added together to give total  $\sqrt{-}$  macroscopic cross-section . For materials like stainless steel containing more than one nuclear species, the individual  $\mathbf{E}_{\mathbf{i}}$ 's are added together to give the total. This is snown in Appendix 6.1(b). From the table of massabsorption cross-sections for  $\sqrt{-}$ 's (p-762,(21)), it is clear that except  $\mathbf{H}_2$ , the most efficient  $\sqrt{-}$  absorbers are heavy elements like lead ( & iron, to a lesser extent) which have high cross-sections for both photoelectric absorption and pair production.

### (i.') CORE GAMMAS

TAB	LE	6.3
-----	----	-----

V_RAY SOURCE	PHOTON ENERGY - (MeV)				
	1 :	2	4	6	8
Prompt fission MeV/Fission	3.45	3.09	1.04	0.26	_
Fission product MeV/Fission	5.16	1.74	0.32	-	_
Total	8.61	4.83	1.36	0.26	_

$$S_{V} = 3.1 \times 10^{10} \cdot V_{D} = MeV/cm^{2} - s$$

where,  $V_{i}$ 's are chosen energy intervals from

1 to 8 MeV .

since the core absorbs  $\gamma$ -rays emitted by it, this self-absorption phenomenon has been considered. This reduces resultant radiation

level in the core outer surface by F  $_{\rm pi}$  times, where F  $_{\rm pi}$  is self-absorption function at the  $\sqrt{-}{\rm energy}~E_{\rm fi}$  .

 $F_{
m p} = {{
m Radiation \ intensity \ with \ self-absorption} \over {
m Radiation \ intensity \ without \ self-absorption}}$ 

For a cylindrical source viewed from the side,

If dose rates are to be considered at distances  $\gg$  R, then the reactor can be considered as a point isotropic source of strength  $S_i = S_V$  \* V\*Fpi MeV/\*, where V = core volume, for V-energy  $E_{\Gamma i}$ . This is the source strength used in the CODE.

In the CODE, the point kernel method has been employed where the reactor is considered as a source as above. Since V-rays follow the exponential attenuation law, in spherical coordinates, the V-flux will be :-

$$\emptyset$$
 (r) =  $\frac{S_i \cdot \exp(-\sum r)}{4 \pi r^2}$  where r= distance from source centre.

For attenuation through different layers of thickness  $\mathbf{t_i}$  and  $\mathbb{V}$  -absorption cross sections  $\Sigma_i$  , the exponential term becomes

$$-b = -\sum_{\text{all } i} (\Sigma_{i}t_{i}).$$

From the main beam of  $\sqrt[7]{}$ 's, the photons being scattered out . of any particular narrow beam are replaced to some extent by particles being scattered— in from adjucent beams. This results in an increase in particle flux-density depending on  $\sqrt[7]{}$ -energy & material and "b". Hence a factor  $\mathbb{B}_{D_{\overline{M}}}$ , isotropic point—source dose—rate build—up factor (>1) is included in the fluxequation.

$$\emptyset$$
  $(r, E_{\gamma_i}) = S_i \frac{B_{Di} (b(E_{\gamma_i}), E_{\gamma_i})}{4\pi r^2} \exp(-b(E_{\gamma_i}))$ 

when the total dose is required to be calculated, the effect of every E; is to be summed up. This equation has been used to obtain the effect of various energy fluxes at different layers.

### (ii) CAPTURE GAMMAS

These rays emitted throughout the shield, are directly dependent on the thermal neutron fluxes. From this, and a knowledge of material densities & cross-section, the secondary gamma source-rate may be calculated thus:-

Source (i, r) = 
$$\sum_{as}$$
 (i) \*  $\phi_s$  (r) photons/cm<sup>3</sup>-s

at layer i a distance r from core centre. In most cases, a spectrum of  $\sqrt{-}$ rays are emitted. These have to separately be considered thus,

Source (i, r, 
$$E_{-1}$$
) =  $\sum_{as}$ (i,  $E/i$ ) \*  $\emptyset_s$ (r)

Here, again,  $\mathbf{E}_{\mathbf{Y},\mathbf{i}}$  is assumed to vary in discrete steps from 1 to 10 MeV.

Since  $\sqrt{\ }$  -rays are generated throughout the shield, consideration must be given to the varying shield thickness available to them. So, each layer of the snield has been divided into a series of concentric rings of thickness. 1.0 cm and each of these are considered as separate sources. The total radiation outside the shield is obtained by summing the radiation obtained from each of these rings from all layers, plus that obtained from the core itself, following the Point-Kernel technique (described under "Core Gammas") of  $\sqrt{\ }$  -ray attenuation, for each energy interval,  $\sqrt{\ }$  This procedure has been adopted in the CODE.

# 6.3.3 EMISSIONS FROM REACTOR EFFLUENTS

The use of light water as coolant poses for lesser problem than other liquid coolant in this field. The major reaction of interest is:

 $0^{16}$  (n, p)  $N^{17}$  activation cross section 2.0E-5 barns;  $N^{17}$  emits gamma rays of everage energy 6.2MeV. The total activation energy (A) evaluates as:-

 $A_{\tau} = 8.2925 \text{ E-6} * \%_{H_2} * V_{H_2} \circ \text{,eff} * \exp (-0.09367 * \tau) \text{ MeV/s}$ 

where,  $\emptyset_{fv}$  = virgin fission neutron flux

V<sub>H2</sub>O,eff= effective water volume to be considered for shielding purposes.

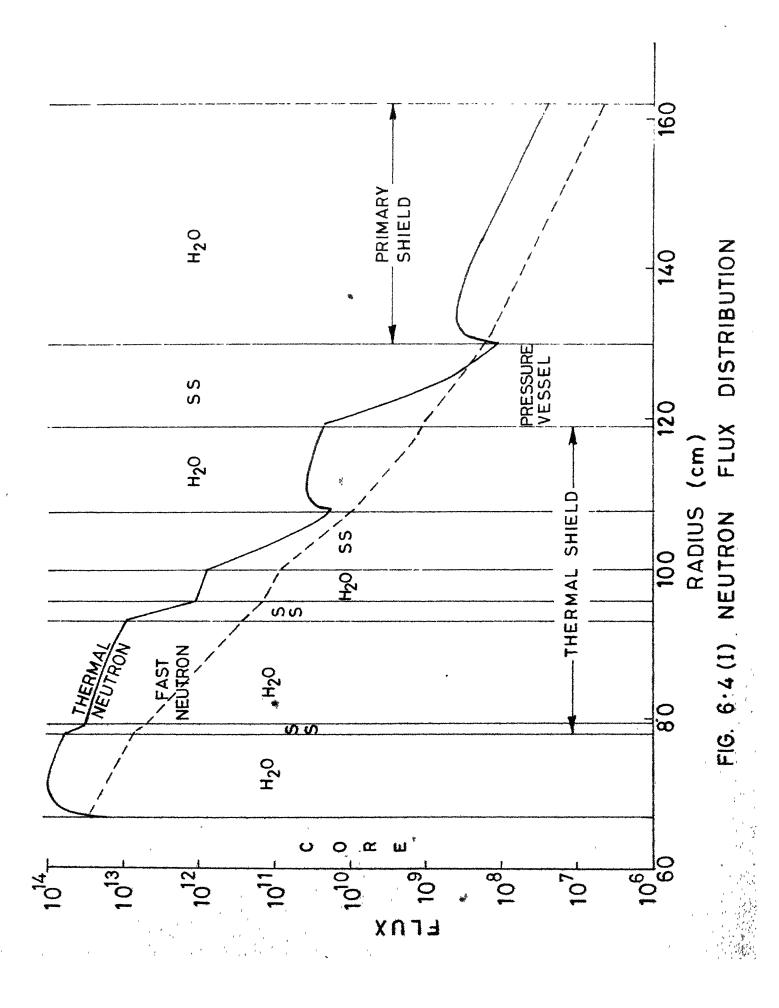
 $\tau$  = effective time constant for transport.

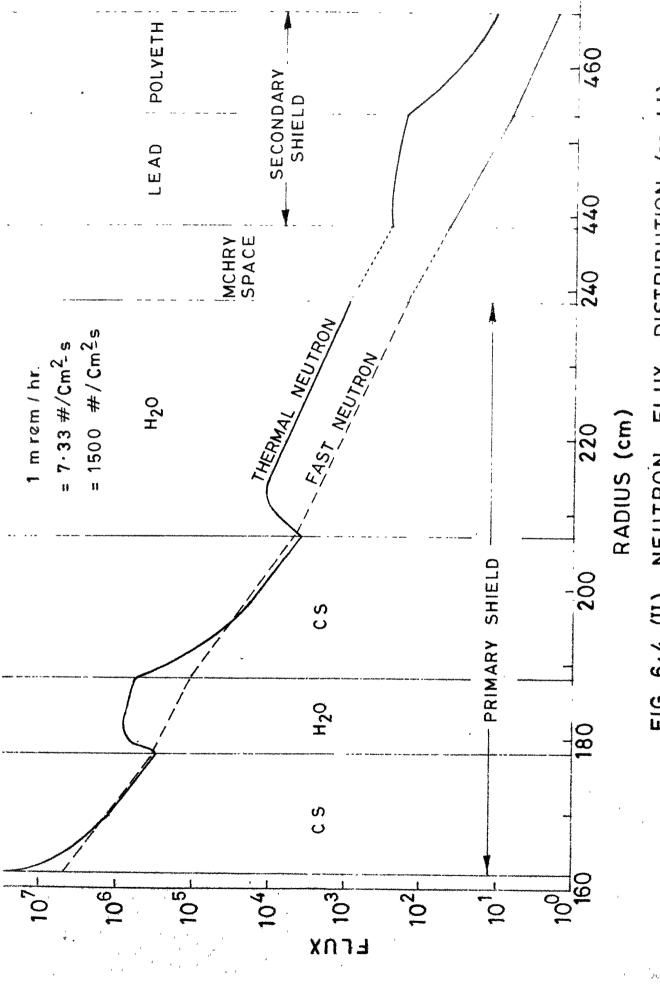
In the abscence of VH2O, eff and T and shape & diminsions of all primary components (extra-core) required to calculate equivalent effective flux for smielding, this emission has not been considered for reactor shielding here. However, since its magnitude is small, it does not introduce great errors in dose calculations.

### 6.3.4 TOTAL DOSE RATES

Once the neutron and gamma fluxes are known at all interfaces, it is easy to evaluate the total effective dose rates. For this, the flux for unit tissue dose (1 mrem/hr) is used as simple conversion factors (CF). Taken from P.7-66 of Ref(21) they are :-

Table 6.4 Fluxes for unit	tissue dose rates:
Particle	flux for 1 mrem/hr dose.
(a) Thermal neutrons	1500 #/cm <sup>2</sup> -s
(b) Fast neutrons (1 to 10 MeV)	7.333 # /cm <sup>2</sup> -s
(c) V-rays	Ŷ
1 MeV	577 MeV/cm <sup>2</sup> -s
1	· · · · · · · · · · · · · · · · · · ·





DISTRIBUTION (contd) NEUTRON FLUX FIG. 6-4 (II)

*	
4 MeV g	681 MeV/cm <sup>2</sup> -s 841 MeV/cm <sup>2</sup> -s 946 MeV/cm <sup>2</sup> -s 022 MeV/cm <sup>2</sup> -s

using these  ${\rm CF}_{\mbox{i}}$ , the total cose rates at different layers have been calculated & listed in the CODE results.

# 6.3.5 WEIGHTS OF SHIELDING MATTRIALS

In a marine reactor the shielding should weigh minimum possible while still being effective; once the shield dimensions have been arrived at after having analysed many combinations of varying thicknesses in the CODE, the approximate shielding weight has been calculated using simple geometry techniques. For the varying heights of different shield -layers, varying height-scaling factors have been arrived at, after extensive study of a comparative nature done on various marine reactors (information of only those available).

The overall shielding weight (including water-snields) comes to approximately 838.2 tons. The weights of the primary system, Core, Control Rod drive Mechanism (CRDM) and coolant & piping are to be separately considered for the total reactor

weight. An uncertainty error of 10% in the above determined value is anticipated.

## 6.4 COMMENTS

It has been demonstrated from the CODE output that the maximum dose rate from the secondary snield is 0.735 mrem/hr. and that from the primary shield 4.331 x 10 mrem/hr. Overall shield outer diameter is 30.62 Ft and weight 838.2 tons; a radial 200 cms space for the primary loop machinery has been assumed. With an increase in this space, the shield weight will increase substantially as the quantity of lead required increases.

The neutron flux at the core edge has been chosen in a conservative manner to ensure proper shield design under all operating conditions. Fluxes obtained from chapter-5 have been incremented by 2.304 times (1.269 Engg. hot-channel factor; 1.178 control-rod peaking factor- Z Sin(Z) over Sin(Z); 1.5408 flux increase due to core burnup).

The use of point-kernel technique with build-up factors, however, does not fully account the fact that in-scattered \$\sqrt{-}\-\text{rays}\$ is of a lower energy than incident \$\sqrt{-}\-\text{rays}\$, \$\mathbb{E}\_{\chi}\$. The scattered component consists of a spectrum of energies from 0 to \$\mathbb{E}\_{\chi}\$. This changes with distance traversed through shield. Further, the actual scattering process is anisotropic. So the dose rates obtained by slightly our analysis are/higher than the actual rates. As \$\sqrt{-}\-\text{ray}\$ attenuation is correctly described by the Boltzmann's transport equations, improved analysis results when transport codes are used.

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## CHAPTER-7

#### REACTOR CONTROL DESIGN

### RESUME

# 7.1 REACTIVITY COMPUTATIONS

- 7.1.1 Xe & Sm Poisoning Effects
- 7.1.2 Long-lived Fission Product Poisoning
- 7.1.3 Temperature Coefficients of Reactivity
- 7.1.4 Burnup & Reactivity Balance.

### 7.2 REACTOR CONTROL SYSTEM

- 7.2.1 Salient Features
- 7.2.2 The System
- 7.2.3 Control Scheme

## 7.3 STABILITY ANALYSIS

- 7.3.1 Computation of parameters
- 7.3.2 2-Temperature Feedback Analysis
- 7.3.3 Boiler Transfer Function

### 7.4 RESULTS & COMMENTS

In the design of a marine reactor, the control and instrumentation system is a key factor in providing an efficient safe and reliable plant. A warship has stringent manocuvring requirements which imposes large load variations in relatively shorter times. Consequently, the system should be stable under all conditions of operation with no unallowable overshoots. A knowledge of core reactivity balance and temperatu coefficients is required to assess the above.

The Reactor Physics CODE and subroutine XENON in specific (p.16 of com\_uter print-outs) have been referred to throughout this chapter.

## 7.1 RE. CTIVITY COMPUTATIONS

Two important fission products Xenon & Samarium absorb thermal neutrons substantially. In addition the long-lived fission products also absorb thermal neutrons. Thus, if the react were to remain critical it should have sufficient reactivity to override the above deleterious effects. In general, the only significant effects these poisons have on  $k_{\mbox{\footnotesize eff}}$  is a reduction of thermal utilization, f to a lower value f . The poison reactivity , is :-

$$\mathbf{Q}_{\mathbf{p}} = \frac{\mathbf{f} - \mathbf{f}}{\mathbf{f}} = -\sum_{\mathbf{ap}} * \mathbf{f} / \sum_{\mathbf{afu}} \dots \mathbf{Eqn.} (7.1)$$

The variation of above parameters with temperature should be considered.

7.1.1 
$$\frac{135}{\text{Ae}^{135}}$$
 and  $\frac{149}{\text{Poisoning}}$ :-

This is the most important fission product having a neutron absorption cross-section of 2.7 Mb(2200 m/s). The decay chain for this isotope is :-

Direct Fission Yiela=0.061 Direct Fission 
$$(Y_{I})$$
 Yiela=0.003 . (Stable)

Detailed explanations of differential equations involving the above chain are given in many books & will not be attempted here. The following results, nowever, ensure:-

$$\overline{\Sigma}_{ax} = \frac{(Y_{I} + Y_{X}) * \overline{\Sigma} \cdot \overline{\varphi}_{T}}{\varphi_{X} + \overline{\varphi}_{T}} \qquad \qquad Eqn(7.2)$$

where,  $\mathcal{P}_{\mathbf{x}} = \mathbf{\hat{\lambda}_{x}}/\bar{\sigma}_{\mathbf{ax}}$ , a temperature dependent function  $\mathbf{\hat{\Sigma}_{f}} = \mathbf{\hat{\Sigma}_{f}} = \mathbf{\hat{\lambda}_{raye}}$  fuel firsion cross-section  $\mathbf{\hat{\mathcal{P}}_{raye}} = \mathbf{\hat{\lambda}_{raye}}$  core thermal flux  $\mathbf{\hat{\Sigma}_{ax}} = \mathbf{\hat{\Sigma}_{raye}}$  state Xenon Concentration

Eqn.(7.2) substituted in Eqn.(7.1) (for  $\Sigma_{\rm ap}$ ) gives the Xe <sup>135</sup> activity at steady state. After reactor shutdown, Xe activity rises above this value. The maximum occurs at a time,  $t_{\rm max}$ ,

$$t_{\text{max}} = \frac{1}{\lambda_{\text{I}} - \lambda_{\text{X}}} \qquad * \text{ In } \left( \frac{\lambda_{\text{I}} / \lambda_{\text{X}}}{1 + (Y_{\text{I}} + Y_{\text{X}}) \cdot (\emptyset_{\text{I}} - \emptyset_{\text{X}}) / Y_{\text{I}} (\emptyset_{\text{X}} + \overline{\emptyset}_{\text{I}})} \right)$$
..... Eqn. (7.3)

where,  $\emptyset_{I} = \frac{\lambda_{I}}{\sigma_{ax}}$ 

The Xe concentration is then given by substituting  $t=t_{max}$  in the following Post-shutdown equation:-

$$x(t) = X_{0} e^{-\frac{\lambda_{1}}{\lambda_{1}}} + \frac{\lambda_{1} I_{0}}{\lambda_{1} - \lambda_{X}} (2^{-\frac{\lambda_{1}}{\lambda_{1}}} - e^{-\frac{\lambda_{1}}{\lambda_{1}}}) ... Eqn. (7.4)$$

$$(Y_{1} + Y_{X}) * \sum_{f} \bar{p}_{T}$$

$$(Y_{1} + Y_{X}) * \sum_{f} \bar$$

obtaining  $\hat{\Sigma}_{ax}$  from Eqn.(7.4) and substituting it in Eqn.(7.1), the maximum Xe activity is evaluated.

Though a lesser poison, this has a thermal absorption cross-section of 40.8 Kb. It 's decay chain is :-

Nd<sup>149</sup> 
$$\xrightarrow{\beta}$$
  $\xrightarrow{pm}$   $\xrightarrow{pm}$ 

The Steady-state  $\mathbf{S}\mathbf{m}$  absorption cross-section,  $\mathbf{\Sigma}_{\mathbf{a}\mathbf{S}}$ , is given by :-

Unlike Xe this is independent of neutron flux. The max. Sm concentration after shutdown is given by

$$S_{\text{max}} = S_{\text{o}} + P_{\text{o}} \dots Eqn (7.6)$$

occuring as t -> inf, where

$$S_{o} = Y_{p} \tilde{\Sigma}_{f} / \sigma_{a} s$$
 is subscript 'P' stands  $P_{o} = Y_{p} \tilde{\Sigma}_{f} \tilde{\beta}_{T} / \lambda_{p}$  for Prometnium.

Obtaining  $\Sigma_{\rm aS}$  from Eqn.(7.6) and substituting it in Eqn(7.1), the maximum Sm activity is evaluated.

# 7.1.2 LONG-LIVED FISSION FRODUCTS :-

These also absorb thermal neutrons. Many products naving varying cross sections for neutron absorption and decay-times ensue by U<sup>25</sup> burnup. (Refer Table 9.2, Ref(24)); for computing the long-term effects of the accumulated products, an average cross-section of 45 b per fission is chosen (p.108, kef(24)). This has been obtained neglecting the rapidly saturating products. Since the concentration of these products is essentially the burnt atoms of U<sup>25</sup>, it's macroscopic cross-

section,  $\Sigma_{\mathrm{afp}}$ , is given by :-

$$\Sigma_{\text{afv}} = 3_{\text{frac}} * n^{25} * 43£-24 \dots$$
 Eqn. (7.7)

where,  $B_{frac}$  = Fraction of  $U^{25}$  burnt at End of core life(see 7.1.4)  $n^{25}$  = number density of  $U^{25}$ ,  $\#/cm^2$ -s

Substituting Eqn (7.7 in Eqn. (7.1), the activity of the above products is obtained.

# 7.1.3 TEMPERATURE COEFFICIENTS OF KLACTIVITY :-

The temperature coefficients of reactivity ( $^{\circ}_{T}$ ) are the basic parameters required for meactor Stability Analysis. As  $k_{eff}$  changes with temperatures of operation, a knowledge of  $^{\circ}_{T}$ 's at various reactor operating levels both for the fuel & moderator is essential. Unlike land-based reactors, the load variations here are from full-load to below 20% for automatic control. Consequently,  $^{\circ}_{T}$ 's at various loads would be different and require separate calculations. For convenience only full load, 3/4,  $^{\frac{1}{2}}_{2}$  and  $^{\frac{1}{2}}_{2}$  loads, as well as full-load at EOL (End of Life) have been considered.

The basic equation for  $^{d}_{\mathrm{T}}$  is :-

$$\alpha_{\mathrm{T}}(\mathbf{k}_{\mathrm{eff}}) = \alpha_{\mathrm{T}}(\mathbf{k}_{\mathrm{inf}}) + \alpha_{\mathrm{T}}(\mathbf{p}_{\mathrm{F}}) + \alpha_{\mathrm{T}}(\mathbf{p}_{\mathrm{T}}) \dots \text{Eqn. (7.8}$$
where, 
$$\alpha_{\mathrm{T}}(\mathbf{i}) = \frac{1}{\mathbf{i}} * \frac{d\mathbf{i}}{d\mathbf{T}} \dots \text{Eqn. (7.9)}$$

i = Parameter involved

 $P_{p}$ ,  $P_{r}$  = Fast, Thermal Non-leakage probabilities.

Eqn(7.0) can be expanded as below:-

$$\propto_{\mathrm{T}} (\kappa_{\mathrm{inf}}) = \propto_{\mathrm{T}} (\eta) + \chi(\xi) + \chi(p) + \chi(f) \dots \text{ Eqn. (7.10)}$$

$$\alpha_{\mathrm{T}}(\mathbf{P}_{\mathrm{T}}) = \frac{-\mathbf{B}^{2}\mathbf{L}_{\mathrm{T}}^{2}}{1+\mathbf{B}^{2}\mathbf{L}_{\mathrm{T}}^{2}} (\alpha_{\mathrm{T}}(\mathbf{L}_{\mathrm{T}}^{2}) + \alpha_{\mathrm{T}}(\mathbf{B}^{2})) \dots \quad \text{Eqn (7.11)}$$

$$\mathcal{A}_{T}(P_{F}) = -B^{2} \tau_{T} (\mathcal{A}_{T} (\tau_{T}) + \mathcal{A}_{T}(B^{2})) \dots Eqn (7.12)$$

Each of the terms in Eqn. (7.10) to (7.12) can further be expanded but not done here. (Refer Chap. 13, Ref (23)).

The basic assumption for computations here is temperatures calculated are uniform for the materials involved, throughout the core. In the Reactor Physics CCDE, every parameter is corrected for the operating temperature (except the core dimension variation which is negligibly small). Hence  $\frac{1}{2}$  is determined by giving a small perturbation to the operating temperature and determining the consequent variation in  $k_{\rm eff}$  and hence  $\frac{1}{2}$  using Eqn (7.9). This was done for temperature perturbations of both fuel and moderator operating-temperatures individually, giving  $\frac{1}{2}$  and  $\frac{1}{2}$ , the respective temperature coefficients. The average fuel and moderator temperatures of different loads were obtained from the Thermal Hydraulics CCDE (chap 4) by varying the linear power ratin, of fuel rod

appropriately. Results obtained are summed up in Table 7.1.

Table 7.1 Reactivity Coefficients of Fuel & Moderator.

LOAD	Pfrac	"eff	AV. FUEL TEMPR	AV. MOI TEMPR	<b>%</b> f	
Full	0.9197E-3	0.99294	508.07	257.72	2.7378E-4	6.2327E-4
3/4	1.053E-3	0.99255	442.27	285.84	2.89631-4	6.0464E-4
1/2	1.1865±-3	   0.55296 	<b>3</b> 82.97	283.93	3.C667E-4	5.633E-4
1/4	1.3214£-3	0.59308	329.43	281.98	3.2488L-4	5.320 <b>6-</b> 4
EUL,	0.0	0.59254	503.37	257.72	2.3940E-4	7.00E-4

# 7.1.4 Burnup & Reactivity Balance

Knowledge of the fiel fraction burnt is necessary to obtain the core burnup and reactivity balance. This has been achieved using a term  $B_{\rm frac}$  ('BURNT' in CODE), ie that fraction of burnt  $U^{25}$ , below which the core is unable to override the law-Sm and fission product activities and thus becomes subcritical, with all control rous removed ( $P_{\rm frac}=0.0$ ). This state of core is termed EOL (End of Life).

The core inpuilt reactivity, reactivities required to come up from cold to not-zero-power, and zero to full-power are all determined by choosing the appropriate temperatures of

fuel & momerator in the CCDE and evaluating  $\kappa_{\rm eff}$  . At the ECL , core burnu, is given by the relation:-

Burnup (wiwa/ton) = 
$$\frac{(\text{Wt. of U}^{25} \text{ per ton of U0}_2 * ^3 \text{frac})}{\text{Wt. of U}^{25} \text{ burnt for producing 1 MWa}}$$

....Eqn(7.13)

and, finally, the core endurance (in days of full power ) is:-

(Reter line nos.6900 to 7400 of p.17 of computer printouts for Eqns(7.13) and (7.14)).

Having known the above results, the reactivity balance of the core is made as in Table 7.2. The amount of PoISON required in the control rods should be such that the core remains substitical even in the Cold condition. Hence, a  $P_{\rm frac}=2.35\rm E-3$  was found adequate to drive the core subcritical by over 4%  $\Delta$ k ( $R_{\rm eff}=0.9582$ ). This means as there are 6 control rods per assembly, by a simple geometric computation, the rod diameter: is 0.51 cm (0.494 cm  $B_4$ C pellet diameter), assuming a stainless steel cladding of thickness 0.53 mm .

TALLE 7.2 CORE REACTIVITY BALLANCE			
	_∆ <u>k_%</u>		
Cola to '0' power	9,6360		
for to full power	5.4634		
Ae, Sm poisoning	2.8563		
Ae,Sm override(at ECL)	0.7356		
Fission Produce Poisoning	1 <b>.8</b> 577		
Burnup considerations	10.2373		
e-matrice in the control of the cont			
Total inbuilt reactivity	30.7863		
Total Control rod wortn	34.93		
Burn up (Avcrage) 14697.8 MWā/ton			
Endurance (days of full pewer) - 84.7 days			
The state of the s			

Till now, the basic reactivity requirements, temperature coefficients & core burnup have been computed. Next the control system will be evolved and later certain stability analysis done.

#### 7.2 KLACTOR CONTROL SYSTEM

#### 7.2.1 Salient Features:-

The manoeuvring of warships imposes large load variations on the reactor. A conventional PAR control is inadequate for this purpose as it is designed for only a small variation from full load(upto 10%)— the basic signal it uses is the slow responding average coolant temperature change. In marine —reactors, however, an additional prompt signal will be required (Ref(32)) which 'feels' the power transient as soon as it starts, & disappears gradually at the end of load variation after which only the slower responding signal would be active. Care should be taken that the reactivity insertion rates do not make the reactor prompt critical. For this, the rate is restricted to 0.03  $\%\Delta\lambda$  (i.e.  $a_1$ rox. 0.040 $\beta$ ) based on the fact that reactor should respond by a 2.3%/s power variation to go from 90% to 20% in 30 secs (Ref(32)).

Thus, in the first part of the operational transient, the control system should act promptly and efficiently performing gross regulation and later time regulation to prevent it approaching unsafe conditions and oscillations around equalibrium.

# 7.2.2 The System :-

A simplified diagram of the system is snown in

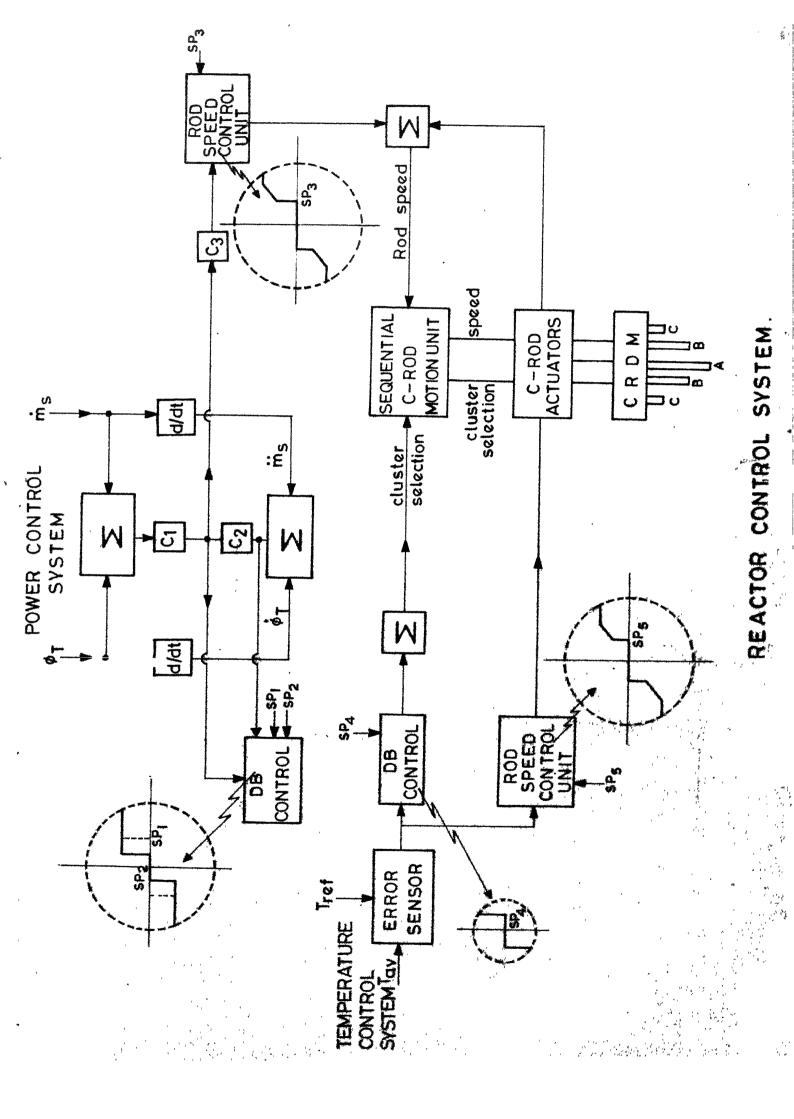


Fig. 7.1. It consists of 2 subsystems, viz. 'Power control system' (prompt acting) and 'temperature control system' (slow acting).

### (i) Power Cuntrol System:-

secondary steam flow rate,  $\dot{m}_{\rm S}$ , and core generated power (proportional to neutron flux,  $\varnothing_{\rm T}$ ). 2 additional terms, derivatives of the aforesaid, are added for enhancing prompt entrol, with scaling factors  $\varnothing_1 \propto \varepsilon_2$ . The resulting power error signal activates either control rod cluster(RCC) A, B or C depending on the signal magnitude. The is used to sense transient condition; if signal exceeds a certain value, DB(Dead Band) is changed from SF<sub>1</sub> (wide, normally) to SF<sub>2</sub> (narrow). Rod speed is controlled by an error signal similar to the above but with a different gain factor  $\varepsilon_3$ . The speed control unit assigns a minimum & maximum insertion rate (  $\equiv 2.3$  %/s power variation) as shown in the figure.

## (ii) Temperature Control System:-

Here main signal derives from difference between the primary coulant average tempr. (T. 7) and a constant reference tempr. Assent for rod-motion is given whenever error signal exceeds the tempr. DB. The characteristics of the various units are as shown in Fig. 7.1.

Signals obtained from the above 2 sum-systems are summed up to obtain the nett error signal. The sequential

control unit decides the RCC that is to be moved, with the speed assigned by the rod-speed centrol units. The centrol-rod actuators activate the particular RCC, thus finally verying  $\mathscr{C}_{\mathcal{T}}$ ; this feedback is reflected in the power control system resulting in a reduction of the original error signal; this effect continues ensuing automatic control.

#### 7.2.3 Control Scheme

Here, a brief concept of the rou-control strategy over the core operating line time is elucidated.

- (i) Control group is constituted of 3 RCC's A, B and C as in Fig. 3.3; each cluster moves as a bundle, independent of each other.
- (ii) A constitutes the 'Scham' rod, capable of shutting down the reactor and is kept fully retracted under normal operation.
- (iii) B constitutes 'coarse' and C, 'fine' ontrol clusters.
- (iv) Initially, B is kept fully inserted and C moved till it reaches the top limit.
- (v) Then C is fully inserted and B half extracted; C is moved up till it reaches the top limit.
- (vi) Finally, C is fully inscrted & B fully extracted; C is moved till it rescnes the top limit (This would then signify the end of core-life).

The above scheme is only a concept & should be supported by extensive calculations which is beyond the scope

of the present work.

#### 7.3 STABILITY AMALYSIS

7.3.1 Computation of some parameters:-

(a) The average neutron life-time, 1\* is

$$1* = \frac{1 + L_{th}^{2} B^{2}}{\hat{v} \cdot \hat{\Sigma}_{\bar{a}}}$$
 Eqn (7.15)

where,  $\tilde{v}$  = neutron space (average)  $\overline{\Sigma}_a$  = Fuel absorption cross-sec(average)

l\* changes with load as  $\Sigma_{\rm a}$  changes with operating fuel temperatures. Table 2.3 gives l\* for different loads.

(b) For neutronics calculations, one-precurs-or group-model nas been chosen. The transfer function,  $G_n(s)$ , is given by :-

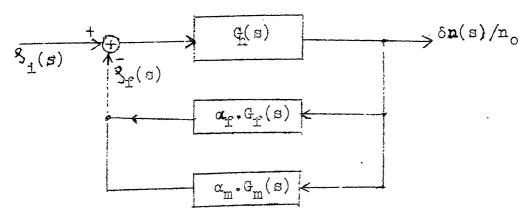
$$G_{n}(s) = \frac{\delta_{n}(s)/n_{0}}{\delta(s)} = \frac{s+\lambda}{\sum_{s=0}^{n} (s+\lambda+\beta/1)}$$

where, 
$$\lambda = 0.08 \text{ s}^{-1}$$
 one-group  $\beta = 0.0065$  values.

Rest of the symbols have their usual meaning.

## 7.3.2 Two-temperature Feedback :-

The control loop for temperature feedback effects of fuel and moderator is :-



We require to evaluate the moderator  $\cdot$  fuel transfer functions,  $^G_m \quad \text{and} \quad ^G_f \quad \cdot$ 

Taking an elementary heat belance for a fuel rod in the reactor and applying a small perturbation to the fuel temperature,  $T_{\pm}$ . We arrive at the following relation (from p.92, ref(34)).

$$G_{f} = \frac{\Delta T_{f}^{*}}{1+sT_{f}} \qquad ..... \qquad \text{Eqn (7.17)}$$

For the moderator a similar equation as above is obtained:-

$$G_{\rm m} = \frac{\Delta T_{\rm m}^*}{1 + e^{\tau_{\rm m}}} \qquad Eqn. (7.16)$$

where, 
$$\Delta T_{\rm f}^{\star} = (T_{\rm f} - T_{\rm c})$$
 at steady -state 
$$\Delta T_{\rm m}^{\star} = (T_{\rm m} - T_{\rm c})$$
 at steady state 
$$T_{\rm f} = {\rm fuel~time~constant} = {\rm m_f \cdot C_{pf}}/{\rm n_f}$$
 
$$h_{\rm f} = \frac{{\rm Power~produced~per~fuel~rod}}{\Delta T_{\rm f}^{\star}}$$

 $\tau_{\rm m}$  = moderator time constant.

Refer Appendix A7.1 for evaluation of  $\tau_{\rm f}$  and  $\tau_{\rm m}$ .

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The 2 fc aback paths can be combined to one as follows:-

$$H(s) = A \cdot \frac{s + \gamma}{(s + \frac{1}{\tau}) \cdot s + \frac{1}{\tau}}$$

$$\text{where } A = \frac{\alpha \cdot \Delta T_{f}^{*}}{\tau_{f}} + \frac{\alpha \cdot \Delta T_{m}^{*}}{\tau_{m}}$$

$$\gamma = \frac{H(C)}{A^{\tau}_{m} \cdot \tau_{f}} , H(C) = \alpha \cdot \Delta T_{f}^{*} + \alpha \cdot \Delta T_{m}^{*}$$

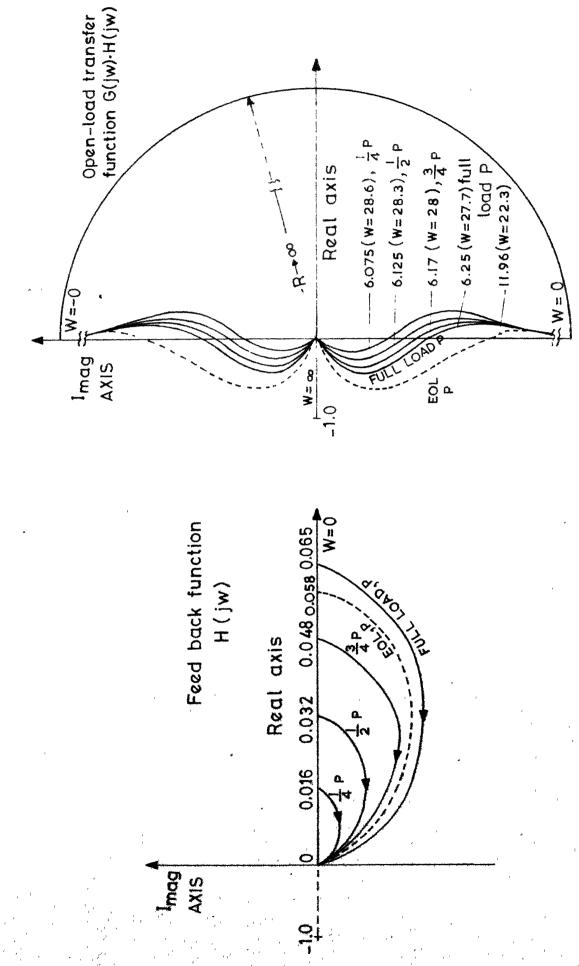
Hence the open loop transfer function is :-

$$G_{n}(s)*H(s) = \frac{A/1^{*} * (s+7) (s+\lambda)}{(s+1/\tau_{m}) (s+1/\tau_{f}) (s+\lambda+3/1^{*})} E_{4}n(7.20)$$

All functions calculated above are functions of operating temperatures and require individual consideration at part-loads. Results thus computed are presented in Table 7.3. The points of intersection of Eqn. (7.23) for different loads are evaluated by the normal rationalizing technique. Calculations are quite involved and hence not shown. The Myquist Plots consequently obtained for Eqns. (7.19) and (7.20) are sketched in Fig. 7.2

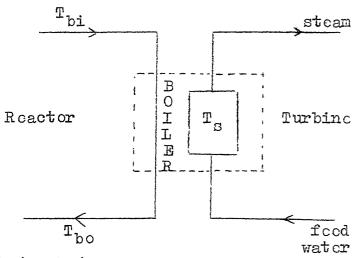
Table 7.3 Two Temperature Feedback Parameters

Parameter	Full Load	75%	50%	25%	EOL, FULL-LOAD
τ <sub><b>f</b></sub> (sec)	3.693	3.409	3.162	2.963	3.693
Δ <sub>T</sub> * ( <sup>O</sup> C)	220.19	156.44	99.05	47.46	220.19
τ <sub>m</sub> (sec)	0.483	0.482	0.481	0.480	0.483
AT <sub>m</sub> (sec)	7.72	5.84	3.93	1.98	7.72
н (0)	0.0651	0.0488	040326	0.0165	0.0581
A	0.0263	0.0206	0.0142	0.0074	0.0255~
γ	1.3882	1.4421	1.5088	1.5664	1.2788
l* (μs )	11.31	10.55	9.82	9.11	17.43
Points of I	ntersection	on Imagi	ary axis	of G(s).H(	s):-
w (H <sub>Z</sub> )	+ 27.74 -	+ 28-02	+28,31	+ 28.56	+ 22.33
GH (x10 <sup>5</sup> )	₹ <sup>6.252</sup>	<del>-</del> 6.169	<del>-</del> 6.126	<del>-</del> 6.073	<del>-</del> 11.956



NYQUIST PLOT OF 2-TEMPERATURE FEEDBACK SYSTEM FIG. 7.2

#### 7.3.3 Boiler Transfer Function



This figure shows the lumped model used.

Assumptions made in

this study are :-

- (i) Primary Temperature  $T_p = \frac{1}{2} (T_{bi} + T_{bo})$
- (ii) Secondary Temperature is that of saturated steam,  $T_{\rm S}$  which is a function of pressure.
- (iii) Steam-water mass in secondary side is constant.
- (iv) Throttle is kept constant; power output of boiler is proportional to secondary pressure,  $\rho_{\rm S}$ .

using basic heat balance for Boiler Power (BP) the following result ensu es (from p.99, ref(34)) for Boiler Transfer Function  $G_{\rm b}(s) = K \cdot \frac{1+\tau^- s}{1+\tau^+ s}$  .... Eqn(7.21)

Where 
$$K = \frac{X-1}{X+1}$$

$$X = 2 \frac{(T_{p} - T_{s})}{(T_{bi} - T_{bo})} * (1 + \frac{p_{s}/p_{s}}{(T_{p} - T_{s})})$$

$$\tau^{+} = \frac{(\text{m C}_{p}) \text{ secondary /BP}}{1/(T_{bi}-T_{s}) + p_{s}/p_{s}}$$

$$\tau^{-} = \frac{(\text{mC}_{p}) \text{ secondary / BP}}{1/(T_{bo}-T_{s}) + p_{s}/p_{s}}$$

In the above equation  $p_s$  is the slope of saturation curve . (d  $p_s/dT$ ) at the appropriate pressure of operation; it is yot by purturbing the following equation :- (p in p.s.i.)

$$T_s(p) = 235.7 + 0.061294*p - 0.5661E-5*p^2.$$

The secondary side pressure has been chosen as 500 psi at full ldad & proportionally lesser for part loads thereof (by virtue of assumption (IV) above). As before boiler transfer functions have to be evolved at various loads and results are in Table 7.4.  $\tau^+$  and  $\tau^-$  are still unknown (as secondary side design has not been done). The Bode plots, however, for Eqn.(7.21) may be plotted, but break frequencies cannot be determined. As  $w \to \inf$ , the plots tend to  $k \cdot \tau^-/\tau^+$  which is a design parameter, and at low frequencies, the plots tend to  $\kappa$ . Fig. 7.3 gives the plots obtained.

Table 7.4 Boiler Transfer function parameters.

Parameter	Full load	75%	50%	25%
T <sub>s</sub>	240.688	255.732	204.977	173.524
pu/ps (°C)	71.256	53.255	48,829	42.109
K	0.7675	0.9021	0.9404	0.9741
Κ <u>τ</u> +	0.628	0.823	0.905	0.964

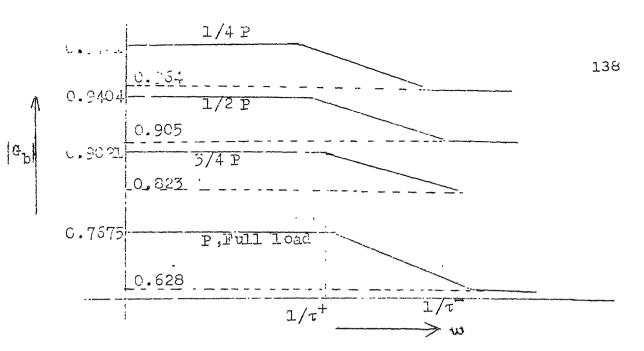


Fig. 7.3 Boiler Transter Function- Bode Plot

7.3 RESULTS AND COMMENTS

The Core Reactivity Balance is displayed in

Table 7.2. From figs. 7.2 & 7.3, the reactor is stable under all conditions of operation. Many parameters are nowever still, unknown & require extensive calculations to be determined. In the reactor control system  $\mathscr{A}_1$ ,  $\mathscr{A}_2$ ,  $\mathscr{A}_3$  and all dead-bands are yet to be evaluated & hence an overall study of the system would not be possible. Transient Analysis & reactor dynamics have not been done in the present study but do require careful consideration for check of unallowable overshoots. Throttle variations as described in Chap.4, ref(34), were studied to an extent; but further progress was not possible due to many unknown parameters beyond the scope of the present design.

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## CHAPTER -8

RESUME	REACTOR	ON	SHIE

8.1 SHIP'S MOTION EFFECTS
8.2 COLLISION BARRIER & GROUNDING PROTECTION
8.3 MISCELLANEOUS FEATURES

Integration of the reactor with the ship includes certain specific design considerations nitherto not discussed like ship's motion effects, induced vibrations, collision a grounding protection for reactor, etc.

### 8.1 Sale'S MUTICA, EFFECTS ON STEAM GENERATOR FERFORMANCE:-

Location of the reactor on board should be such as to minimize ship's roll & pitch on the steam generator-location at about the ship's CG(Centre of Gravity) would be ideal.

In the U-tube steam generator, feed water gains neat by a 2-phase natural circulation system-firstly, feed water absorbs thermal energy from primary coolant becoming partly steam; next, this steam-water mixture from the tube bundle passes through a steam swirl vane located in the riser which separates water from steam certifugally and subsequently through additional dr yers to decrease the moisture content. This 2 phase system, under the effect of snips 3-dimensional motion could present flow oscillations causing loss of heat transfer efficiency, large level fluctuations in the down comer, pulsation in Steam Supply, etc., thus forcing a barely stable reactor control unit into a region of instability. Special simulation computer CODES have to be developed to study the effects of snip motion on steam generator circulation; this is not attempted here but a brief sketch of the associated problem given.

The recirculation loop is divided into a number of small equal portions of, say,  $\triangle z$ . The normal heat balance is done for each element. Additionally, the rolling & pitching effects subject  $\triangle z$  to tangential & centrifugal forces, modifying the momentum equation. The dipping effect results in a modification of 'g' (accln due to gravity) by an oscillatory motion. Consequently, the thermodynamic stability of the recirculation loop in presence of the above effects is done. Finally comes the secondary water level control system. Power level, feed water flow & secondary pressure dynamically alter this level; this necessitates the development of an auto level control loop to ensure system stability.

Extensive studies in the ship motion effects have been done by NaSecolo, G. Selvaggi et al (Ref (37)) using 3 main computer CODES- Sabre-3M, F-111 MO and DCR-2. The study evaluates dynamic behaviour for following perturbations:-

Roll -  $30^{\circ}$  (max); period = 12 s.

Pitch -  $10^{\circ}$  (max); period = 7 s.

Dip - 0.3g ; period = 7 s.

Results obtained reflect the overall performance of a marine steam generator as summed up below:-

- (1) System presents an oscillatory performance for an impressed step perturbation.
- (ii) Insertion of an orificed plate suitably positioned in the downcomer region increases stability margin & damps the

oscillations induced by snip's motion offects.

- (iii) Steam quality increases with decreasing water level in the downcomer.
- (iv) System stability decreases with increasing steam generator inclination or lower system operating pressures.
- (v) System stability increases with lower pressure drops in heated zone or lower feld water temperatures.

#### 8.2 COLLISION AND GROUDING FROTECTION

protection is required to avoid relator demage consequenting in uncontrolled release of fission products (approx. 6 curies/W generated!). This is done by a grid structure of about 80 cm x 90 cm arranged between longitudinal bulkheads & outerhull, supported by decks bening the longitudinal bulkheads (ref(30)). This structure transfers the collision load into the transverse bulkheads of the reactor compartment, thus destroying the striking blow. As per a test program conducted (p.422, ref ibid), no mechanical damage will occur for components behind the collision structure; in addition, the protection is adequate against penetration of a jet aircraft at nominal speed.

For the grounding protection, a grid type support structure 140 cm night is located above a 200 cm night double-bottom (DB). If DB is damaged, the grid is capable of withstanding the weight of reactor containment. Consequently,

during severe loads, the DB being more easily deformable, acts as an elastic spring.

#### 8.2.3 MISCELLANEOUS FEATURES:-

Vibrations are excited by sea-motions, oscillatory propeller forces & auxiliaries; frequency range varies from < 1 Hz to 80 Hz. High energy vibrations from propellers are specially significant & require detailed analysis. As compared to conventional ships of equal power, the machinery weight as well as the normal cruising load on machinery is nigher by 1.7 & 3.5 times respectively (approximate figures). The Power consumed by the primary coolant pump is substantial.

The ship's speed depends on the SHP(Shaft Horse Power) developed by the engine. The speed versus SHP characteristics of a ship is dependent on the displacement, profile at the water line & certain other factors; it however follows an approximate cubic law with linear speed increments requiring cubic SHP increments. Consequently, at 50% of power developed, the ship achieves nearly 75% of its maximum speed. A rough estimate of 22 knots may be expected as the maximum speed of the ship presently under consideration, with a 30,000 SHP maximum power output (assuming 70% of steam to be used for propulsion only, and a plant efficiency of 22%).

An important aspect hitherto ignored is requirement of a secondary propulsion system. Coupled to the main gear box, a compact gas turbine of approximately 15000 SHP may be included so that, in the event of a main engine breakdown, the ship is still capable of making way at 65% of its maximum speed which, now, would correspond to that of 45000 SHP (\*25 knots).

# CHAPTER -9

## CONCLUSION

## RESUME

- 9.1 SUMMARY
- 9.2 SUGGESTIONS FOR FURTHER STUDY

By now, the salient aspects of marine reactor design have been covered. In conclusion, the destroyer class ship is about the smallest to which nuclear propulsion can be reasonably applied — a preliminary study of containment weight revea this (chap 6), as a propulsion machinery weight of  $\approx$  2500 tons is bound to accrue ( & a displacement of the ship of  $\approx$  8000 tons).

#### 9.1 SUMMARY

Some of the design parameters evolved are briefly summed up in Table 9.1. Since the various design processes are inherently interactive, change of a parameter may have a retrospective effect in other processes. In the shielding design a machinery space of 300 cms (instead of the 200cms assumed) would have resulted in a dose rate of 0.4982 mrem/hr outside the containment with a weight increase of 262.0 tons and diameter of 6.6 ft. This space can be fixed only after all components of primary/secondary loop are designed. Core burnup obtained has been low for a 5% enrichment. This timmulation at is due to the compact, close-latticed core configuration encsen that is so vital in reducing overall containment weight in marine reactors.

#### Table 9.1

## Design Characteristics

#### I GENERAL REACTOR DATA

A. Reactor Thermal Power ... 120 MW

No. of Primary coolant loops ... 2

B. Primary Coulant	
- System pressure	2000 psi
- Total flow rate	5553 tons/hr
- Inlet tempr.	280 °C
- average rise in core	15.42 °C
C. Fuel $(\mathbf{vo}_2)$	
- No. of core regions	1
- No. of fuel asslys.	29
- No. of fuel rods per ass	ly 282
- Enrichment	5 w %
- Core Power density	63.51 MW/m <sup>3</sup>
_ Eqbm. core average burnu	
- Wt. of $\mathtt{VO}_2$ in core	6.919 tons
D. Control rods	
- Type/Number	RCC/29
- Absorbing Material	$B_{\Delta}^{C}$
- Rods outer dia/pellet di	a 0:051/0.494 cm
E. Secondary System	
- Steam pressure (at full	load) 500 psi
→ Steam quality	0.9975
F. Plant Physical Parameters	
- Overall Wt. of shielding	838.2 tons
- Containment outer dia	30.67 ft.
NUCLEAR DESIGN DATA	
A. Structural characteristics	
- Core dia/height	134.29 cm/133.4cm
- Fuel rod & antrol rod cl	adding ss347
- Fuel cell type/pitch	square/1.30cm
- Fuel rod dia/pellet dia	0.99/0.858 cm

II.

-Volume fraction  $H_2 c/V_0$  in  $\infty re .... 1.592$ 

## B. Physical & performance characteristics

- Fuel type/density ..... sintered UO2/10.97gm/cc
- Fuel Enrichment -.... 5 w%
- Hut channel facturs

$$F_0^{IV} / F_0^{e} / \text{total } F_0$$
 ..... 3.44/1.04/3.58

 $F_R^N / F_H^e / \text{total } F_H$  ..... 1.994/1.22/2.105

- Flux functions analysed BOL/Normal/EOL  $zSin(z)/Sin(z)/(\pi-z)*$   $Sin(\pi-z)$ 

#### C. Control characteristics

- Type .... mechanical, RCC
- Absorbing material .... B<sub>A</sub>C(den 0.7 gm/cc)
- Rods per assembly/Nc.of asslys. ... 6/29

#### D. Kinetic characteristics

- Moderator tempr. coeff. (full load) ...-6.233E-4
- -Fuel tempr. coeff.(full load) ....-2.738E-4 Ak/k

## III. Core Reactivity Balance Refer Table 7.2.

## 9.2 Suggestions for further study

Some important aspects of marine reactor design not done in the present work are:-

- (a) Materials design The performance of only a few materials has been studied; optimization study of different reactor materials is suggested to evolve better design parameters.
- (b) Snip-motion effects on the steam generator require a study in far greater depth than mentioned in chapter 8. This problem

is peculiar of marine reactors and has a direct effect on overall system stability.

- (c) In-core instrumentation design requires careful consideration as it conveys core fluxes and temperatures at various points in the core; these signals structure the basic inputs for the reactor auto-control loop. Control rod worth evaluation is also suggested.

  (d) In the Shielding Design the radiation from reactor effluents requires evaluation after steam-generator and piping design is done; its magnitude is, however, small & the shielding thicknesses may require marginal modification to counteract this additional dose (e) The pressure-vessel & piping design for mechanical, thermal and other stresses necessitates careful checking out; in the present design a vessel thickness of 12 cm has been assumed based on available literature and not on calculations.
- (f) Design of pressurizer, steam generator, components of secondary loop & subsequent heat balance is also proposed.(g) Reactor start-up & shutdown procedures are suggested for the present design.

Study of an extensive topic as a reactor design in a limited time frame effects in simplifications & exclusions. The core flux functions for thermal hydraulic study do not precisely represent actual flux variations. Other flux functions as considered adequate may be assumed to evolve more

realistic performances. The core nuclear design (Reactor Physics & Shielding ) has been done using a heterogeneous 2-group theory with constant core temperatures for fuel & moderator—multigroup theory using local temperature variations and development of transport theory computer CODES is suggested; this evolves a more precise design, closer to a practical reactor unit. The reactor automatic control loop may be studied in detail, both for system stability & transient characteristics, once the loop constants (of Fig.7.1) are evaluated. Study of reactor transient for an ahead—astern simulation consisting of a load variation from 90% to 20% in 30 secs and immediate return to 90% in another 30 secs would be of significance in ascertaining the system performance.

An earnest attempt has been made to describe the complex, varied & multi-dimensional problem that a warship reactor design is. Both strategically and tactically, nuclear propulsion is the ultimate form of propulsion for warships today; it is obvious to all who pause to ponder this matter. It will remain so until a superior form of ocean propulsion for supporting modern weapon systems is architectured.

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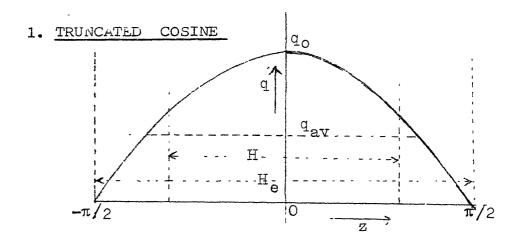
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### <u>APPENDIX</u>

## A 4.1 CALCULATION OF HOT-CHANNEL FACTORS

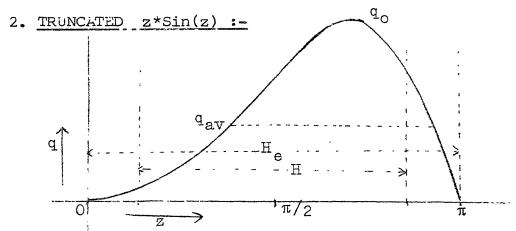


$$q(z) = q_0 * \cos \left(\frac{\pi}{H_e} z\right)$$

$$= \frac{2q_0}{H} \int_0^{H/2} \cos \left(\frac{\pi}{H_e} z\right) \cdot dz$$

$$= \frac{2}{\pi} \left(\frac{H_e}{H}\right) * q_0 * \sin \left(\frac{\pi H}{2H_e}\right)$$

• 
$$F_{Z} = \frac{q_{0}}{q_{av}} = \frac{\pi}{2} * \frac{H}{H_{e}} * \frac{1}{\sin(\frac{\pi H}{2H_{e}})}$$



Let us find the normalizing factor for z.Sin(z).

$$\frac{d}{dz}(z\sin z) = 0$$
 at maximum;

$$\Rightarrow$$
 Tan(z) = -z

The above eqn. is satisfied when z=2.02877

So, maximum = 
$$2.02877*Sin(2.02877) = 1.8197$$

We shall choose the axis as above in diagram.

$$q_{av} = \frac{q_0}{H} * \int_{E}^{H} \frac{z.sin.z.dz}{1.8197}$$
 where,  $e = \frac{H_e - H}{2}$ 

As z is distance in cms we will have to convert it to radiums -: -

$$q_{av} = \frac{q_0}{H} * \int_{e}^{H} \frac{\pi z}{H_e} * \sin(\frac{\pi z}{H_e})*dz * \frac{1}{1.8197}$$
Let  $x = \frac{\pi}{H_e}^z \Rightarrow dx = \frac{\pi}{H_e} \cdot dz$ 

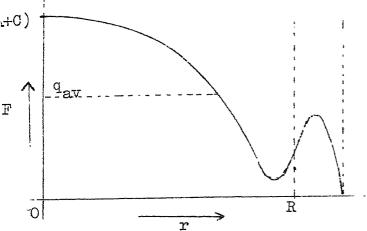
$$q_{av} = \frac{q_0}{1.8197} \cdot \frac{1}{H} \cdot \frac{H_e}{\pi} \qquad \int_{e}^{H} \frac{\pi}{H_e} \times . \sin x \cdot dx$$

$$= \frac{q_0}{1.8197} \cdot (\frac{H_e}{H}) \cdot \frac{1}{\pi} \left( -\frac{H\pi}{H_e} \cos \left( \frac{H\pi}{H_e} \right) + \frac{e^{\pi}}{H_e} \cdot \cos \left( \frac{e^{\pi}}{H_e} \right) + \sin \left( \frac{H\pi}{H_e} \right) - \sin \left( \frac{e^{\pi}}{H_e} \right) \right)$$

$$\sin \left( -\frac{e^{\pi}}{H_e} \right) \cdot \sin \left( \frac{H\pi}{H_e} \right) = \frac{e^{\pi}}{2H_e} =$$

$$F_{Z} = \frac{q_{0}}{q_{av}} = \frac{1.8197 * \pi * H}{H_{e}(-ACos(A) + BCos(B) + Sin(A) - Sin(B))}$$

#### 3. TRUNCATED BESSEL'S FUNCT: ON :



#### Function

$$F(r) = AJ_0(lr) + CI_0(mr)$$
  
 $R = core radius$ 

A,C, 1 & m are all constants determined

from the Reactor Physics CODE and hence known. By definition:-

$$q_{av} = \frac{1}{\pi R^2 H} \int_{0.0}^{H} \int_{0.0}^{R} F(r)$$
 \* (Axial function) \*2 rdrdz

The axial function integration is done in (1) and (2) above.

The radial integration is:-

$$q_{av} = \frac{1}{R^2} \int_{0}^{\infty} (A \cdot J_0(lr) + C \cdot J_0(mr)) * 2.r.dr$$

Since, 
$$\int lr.J_0(lr).dr = lr.J_1(lr)$$
  
and  $\int mr*J_0(mr)dr = mr*J_1(mr)$ ,

$$q_{av} = \frac{2}{R^2} \left( \frac{A}{1} \cdot R \cdot J_1(1R) + \frac{C}{m} \cdot R \cdot I_1(mR) \right)$$

At r= 0 , the peak flux occurs; its value is (A+C)

$$\frac{q_0}{q_{av}} = \frac{A + C}{2A \cdot J_1(lR) + 2C \cdot I_1(mR)}$$

$$= \frac{1 + \frac{C}{A}}{2 \cdot J_1(lR) + 2(\frac{C}{A}) \cdot I_1(mR)}$$

$$\frac{1}{lR} + \frac{2(\frac{C}{A}) \cdot I_1(mR)}{mR}$$
As  $\frac{C}{A}$  \( \lambda \)

$$\mathbf{F}_{R}^{N} = \frac{1}{2 J_{1}(1R) + 2 \cdot (\frac{C}{A}) \cdot \frac{J_{1}(mR)}{mR}}$$

# A 3.2 <u>DETERMINING</u> K<sub>fu</sub>:

Let  $K_{fu}(T) = a+bT$ , be a linear function of temperature.

AIM :- To determine what value of

K<sub>fu</sub>(T) is to be used in the

heat conduction equation,

Eqn.(4.3).

#### Solution

We shall develop an equation relating  $T_0$  and  $T_s$  using  $K_{fu}(T) = a+bT$  then compare this with Eqn.(4.3). In the steady-state condition

of thickness dr at radius r.Integrating from r=0 to r=r<sub>fu</sub>:-

$$(or) T_{f} = T_{0} - \frac{q^{2} \cdot r_{fu}}{4(a+b)(\frac{T_{0}+T_{f}}{2})}$$

This means  $K_{fu}(T)$  in Eqn (4.3) is evaluated at the arithmetic mean fuel temperature for determining  $T_f$  i.e. at  $T = \frac{T_0 + T_f}{2}$ 

A 5.1 <u>CALCULATION OF</u> D<sub>ss</sub> :-

Element	NUM DEN*	$\Sigma_{a}^{\star}$	σ <sub>s</sub> (b)	$\sum_{\mathbf{s}}$	(1- $\tilde{\mu}_0$ )	$\sum_{\mathbf{tr}}$
Fe	6.044 E22	0.093180	11.4	0.68902	0.9880	0.68075
Cr	1.6719E22	0.030758	4.2	0.07022	0.9871	0.06931
Ni	8,2291E21	0.025058	17.0	0.139895	0.9885	0.13829
s	1.7536 E21	0.000178	2.2	0.003858	0.976	0.00376
N <sub>b</sub>	4.1611 E20	0.000290	6.5	0.002705	0.9928	0.00269
Mn	1.7541 E20	0.001401	1.9	0.000333	0.9878	0.00033
С	3,2091 E20	0.0000009	4.7	0.001500	0.9440	0.00142
	- NOT - Mile Microstrage (Chipper Chipper Chip			kom wynnogo, wo''' kontronne olithuren ichelikul		
	Total	0.150867		0.90754		0.896555

<sup>\*</sup> Taken from Table A6.1

$$\overline{D}_{SS} = \frac{1}{3 \cdot (\sum_{a} + \sum_{tr})} = \frac{0.318241 \text{ cm}}{}$$

# A 5.2 CALCULATION OF D<sub>1f</sub>

The fast diffusion constant for core,  $\mathbf{D}_{1f}$  is given by the expression :-

$$D_{1f} = \frac{1}{3(\bar{\Sigma}_{1a} + \bar{\Sigma}_{s}(1 - \bar{\mu}_{0}))}$$
 .... Eqn.(1)

where,  $\Sigma_{1a}$  = av-fast absorption cross section.  $\Sigma_{s}$  = averaged scattering cross section.

since, the scattering cross section of Hydrogen varies strongly with neutron energy, we use an artifice to calculate its scattering cross-section. Let us make an initial guess of (40)= 10 barns -

The parameters are :-

#	Н.	O(total)	S. S.	Total
n (#/cm <sup>3</sup> )	0.3641E23	0.3622E23	0.840 <b>7</b> E22	
(b)	10	4.2	11.4	
3	1.0	0.12	0.353	
(1- \bar{\mu}_{O})	O <sub>4</sub> 333	0.258	0.988	
Σ́s	0.5094	0.15212	0.09584	0.7577

For the above parameters,

$$\mathcal{S}_{\text{reac}} = \frac{\sum_{i=1}^{n} \mathcal{Z}_{i} \mathcal{Z}_{si}}{\tilde{\Sigma}_{s} (\text{ToT})} = 0.6862$$

$$(1-\mu_{\bullet})_{\text{rxac}} = \frac{\sum_{i=1}^{3} (1-\mu_{\bullet})_{i} \cdot \bar{\Sigma}_{\text{si}}}{\bar{\Sigma}_{\text{s}} \text{ (ToT)}} = 0.55205$$

$$\bar{\Sigma}_{\text{s}} \text{ (ToT)} = \left[\frac{\ln(\frac{E_{\bullet}}{E_{\text{th}}})}{3\sqrt{3}(1-\mu_{\bullet})} \cdot \frac{1}{7}\right]^{\frac{1}{2}} = 0.7475$$

We see  $\tilde{\Sigma}_{\rm S}$  above & one from tabulation do not agree. So we guess higher values of  $\delta_{\rm S}({\rm H_2})$  and continue calculations. We obtain convergence when  $\delta_{\rm S}({\rm H_2})=13.7$ 

$$\mathcal{L}_{reac} = 0.69693$$
 $(1-\dot{\nu}_{reac}) = 0.54459$ 
 $\tilde{\Sigma}_{sreac} = 0.7488 \text{ cm}^{-1}$ 
Eqn.(2)

Next we have to determine  $\tilde{\Sigma}_{1a}$ .

$$\sum_{1a} = \frac{N-I_{eff}}{\ln(\frac{E_0}{E_{+h}})}$$

we know from calculation for 'p', that

$$I_{\text{eff}} = A + \frac{C}{\sqrt{a}} = 21.254 \text{ barns for UO}_2$$
.

$$\bar{\Sigma}_{1a}$$
 = 2.6323E22 \* 21-254E-24 = 0.03858 cm<sup>-1</sup> ..... Eqn (3)

From Eqns. (2) & (3), we can evolve  $D_{lf}$  through Eqn (1):-

$$\frac{1}{3 * (0.03858 + 0.54459 * 0.7488)}$$

$$= 0.74674 \text{ cm}^{-1}$$

THE THE PONCE	J	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		THERMAL CAPTURE		NEUTRON CROSS-SECTIONS	FAST	NEUTRON CROSS-SECTIONS
	Į.	PER CM		ENSITY	(barns)	g'+(barns) ∑ (cm <sup>-1</sup> )	o * (Haens)	
₽ 26 <sup>e</sup>	6.69	5.606	55.85		2,1535	0.13017	1.89591	0.114600
$^{ m C}_{24^{ m r}}$	18.0	1.444	52,01	1.6719E22	2,573	0.042968	1.84003	0,030763
N <sub>1</sub>	10.0	0.802	58,69	8.2291E21	4.254	0.035006	1.93582	0.015930
81 14	1.02	0.0818	28.09	1.7536E21	0.1418	0.000249	1.41992	0,002490
4 4	0.80	0.0642	92,91	4.1611E20	0.9748	0,000486	2,34776	0,000977
Mn 25	0.20	0.0160	54,93	1.7541E20 11.1664	11,1664	0.001959	1,88273	0,000330
ပ <sub>ပ္</sub>	90.0	0.0064	12,01	3.2091E20	86800.0	0,00398 0,000001	0.9942	0,000319
TOTAL -	100.0	8.02	1	ŧ	1	0.210759	1	0.165409
* Using 6	0 % tr ∨ 0 11 6	75.	400	100/1000 C To the task to the flow or the contract with	4 5 4 5 4	, 1 th		AND THE PROPERTY OF THE PROPERTY AND THE PROPERTY OF THE PROPE

<sup>+</sup>  $\delta$  (th) =  $\sqrt{\pi/3}$  \*  $\sigma$ (2200); At tempr. T,  $\Sigma$  (T) =  $\Sigma$  (th) \*  $\sqrt{295.1/(273.1+T)}$ Using @= 0.35\*A' for consituents unlisted in table 5.3, ref(26)

 $ilde{ heta}$  For carbon steel parameters are taken as that for  $ext{F}_{ ext{e}}$ 

A.6.1(b) Linear Apsorption Coefficient\* for dering regs run steinless steel®

CONSTI	WEIGHT	3, E,	=1 MeV		1 = 2 McV	: .a	V. = 4 M.V	V 4.	/ = 6 in.V		
W 1 Water tegens and a company company	(8)	1/2 NS	N	2/8	W	2/8	W	N (x	M —	M %	[A
ње 26	5,606	0.0595	0.0595 0.3356	0,0424	0.2377	0.035	,	430.	5.170-		
S1 14	0.0818	0,0635	5.194E-3	0.0447	3,65615-3	C. 3323	6.224m-3		2,266	0.0254 2.075	2.073
و ن	,0064	0.0636	.0064 0.0636 4.0701E-4	0.04444	2.8425-4	0.3334 1	1.5463-4 (0.0245		1.5062.4	.021:11.	1.3652-4
Cr , Ni 24 28 Np , Mn 41 25	2,3256	nd til denne an	0.138385	1	9960*0	0	 5.0767		0707	·	0. Jó&6
TOTAL	8,02	and had been seen and the seen	0.4775	1 - man - m	0.3402	<u>.</u>	 C. 2046		. 44.5	<u>.</u>	C. 2362
* from ref(21), pp. 762	ref(21)	, DD. 76	Same at a manus consenses at a service.	Contraction in the letter of							***

E taken as for Fe , since not listeu. 26 O for capon steel,  $\Sigma/8$  is taken sime as Fe. 26

#### A6.2 INCOMPLETE ERROR FUNCTIOS\*

$$E_{n} = \int_{1}^{\frac{e^{-tx}}{e^{-tx}}} \frac{e^{-tx}}{e^{-t}} dt = x^{n-1} \int_{x}^{\frac{e^{-t}}{e^{-t}}} dt$$

are called incomplete error functions.

They have series solutions.

$$E_0(x) = e^{-x}/x$$
  
 $E_n(x) = -E_{n-1}(x)$ 

In general,

$$E_{n}(x) = \sum_{\substack{m \neq 0 \\ m \neq n-1}} \frac{(-x)^{m}}{(n-1-m)m!} + (-1)^{n} \frac{x^{n-1}}{(n-1)!} (\sqrt{+\ln(x)} - A_{n})$$

where, 
$$V = 0.577216 \dots$$
,  $A_1 = 0$ ,  $A_n = \sum_{m=1}^{n-1} \left(\frac{1}{m}\right)$ 

In particular,

$$E_{1}(x) = -(y + \ln x) + x - \frac{x^{\frac{1}{4}}}{4} + \frac{x^{\frac{3}{8}}}{8} - \dots$$

$$E_{2}(x) = 1 + x(y + \ln x) - \frac{x^{2}}{2} + \frac{x^{\frac{3}{12}}}{12} - \frac{x^{4}}{32} + \dots$$

The following integral has been used :-

$$\int_{e}^{kx} \cdot E_{n}(ax+b) \cdot dx = \sum_{i=0}^{n-1} \frac{a^{i}}{k^{i+1}} \cdot e^{kx} \cdot E_{n-i}(ax+b) - \frac{a^{n-1} \cdot bk}{k^{n}} \cdot E_{1}(\frac{ax+b}{1-\frac{k}{k}})$$

<sup>\*</sup> Ref(31) page 355

In particular,

$$\int_{e}^{kx} E_{1}(ax+b) \cdot dx = \frac{e^{kx}}{k} E_{1}(ax+b) - \frac{e^{bk/a}}{k} * E_{1}(\frac{ax+b}{1-k/a})$$
If  $x \gg 10$ ,  $E_{r}(x)$  is well approximated by:-
$$E_{n}(x) \stackrel{\sim}{=} e^{-x} Q_{n}(x)$$
where,  $Q_{n}(x) = \frac{1}{x+n} + \frac{n}{(x+n)^{3}}$ 

(a) Solution 
$$z^{2} \varphi_{s}(r) - c^{2} \varphi_{s}(r) + Qe^{-\sum (r-L)} = 0$$
  

$$\nabla^{2} \varphi_{s}(r) - c^{2} \varphi_{s}(r) + P \frac{e^{-\sum r}}{r^{2}} = 0$$
where  $P = Qe^{+L\sum r}$ 

In spherical coordinates

$$\nabla^2 = \frac{1}{r^2} * \frac{d}{dr} (r^2, \frac{d}{dr})$$

$$\frac{1}{r} \left( r \frac{d^2 g_s}{dr^2} + 2 \frac{d g_s}{dr} \right) - c^2 g_s(r) + \frac{Pe^{-r \Sigma}}{r^2} = 0$$

Substituting  $r.\emptyset_{S}(r) = X$ , equation reduces to

$$(D^2-c^2) X = - \frac{p}{r} \frac{e^{-r\Sigma}}{r}$$

By using the simple integrating factor method by first considering (D+c) X=Y, solving for Y and later, solving for X, we get the equation:

$$X = \frac{Ae}{-2c} + Be^{cr} - P \cdot e^{cr} \int_{cr} dr \cdot e^{-2cr} \int_{r} e^{(c-\Sigma)r} \cdot dr$$
From appendix A6.2, 
$$\int_{cr} e^{(c-\Sigma)r} \cdot dr = -E_1((c-\Sigma)\cdot r)$$
As  $x = \emptyset_s *r$ 

$$V_s * r = -\frac{Ae^{-2cr}}{2c} + \frac{Be^{cr}}{2c} + Pe^{cr} \int_{cr} dr \cdot e^{-2cr} \cdot E_1(r \cdot (c+\Sigma))$$

Again using the integral identity of A6.2,

$$\varphi_{s}(r) = -\frac{Ae^{-2cr}}{2cr} + \frac{Be^{cr}}{r} + \frac{Pe^{cr}}{r} \left\{ \frac{(c-\Sigma)}{2c} \cdot E_{1} \left( \frac{(c-\Sigma)r}{1+\frac{2c}{c-\Sigma}} \right) - \frac{e^{-2cr}}{2c} \cdot E_{1} \left( \frac{(c-\Sigma)r}{1+\frac{2c}{c-\Sigma}} \right) \right\}$$

As  $\emptyset_s(r) \longrightarrow 0$  as  $r \longrightarrow \inf$  , B = 0 is essential.

Thus, substituting back for P, we obtain:-

$$\emptyset_{s}(r) = -\frac{Ae^{-2cr}}{2cr} + \frac{Qe^{L\sum}}{2cr} \left\{ (c-\sum) * E_{L}(Y)e^{cr} - E_{1}(X) * e^{-cr} \right\}$$
where,  $X = (c-\sum) \cdot r$ 

$$Y = X/(1 + \frac{2c}{c-x})$$

(b) Solution of 
$$\varphi_s^2(r) - c^2 \cdot \varphi_s(r) + Qe^{-Er} = 0$$
.  
Here the approach is similar. Substituting for

$$r * p_{g}(r) = X$$
, we obtain:-
$$(D^{2}-c^{2}) X = -Pr.e^{-r \sum_{i=1}^{n} (1)^{n}}$$

The complementary Function of this differential Eqn. is  $X = Ae^{-cr} + Be^{-cr}$ ;

The particular Integral is obtained by choosing a particular solution for  $X = (Dr + E)e^{-\sum r}$ ;

Putting this is eqn.(1), we obtain the coefficients

$$D = \frac{1}{c^2 - \sum^2} \quad ; \quad E = -\frac{2}{(c^2 - \sum^2)^2} \quad ,$$

Hence, 
$$\emptyset_{S}(r) = \frac{Ae^{-Cr}}{r} + \frac{Be^{Cr}}{r} + Q = \frac{e^{-\sum_{r}} (r - 2)}{r}$$

as 
$$\emptyset_{S}(\inf) = 0$$
, B=0

\*\*\*\*\*\*\*\*\*\*\*\*

FROM COKE A 6.4 TOTAL GAMMA EMISSIONS

SOURCE	*	$E\sqrt{=1}MeV$		$E_{V}=2$ Me	MeV	E/= 6 MeV	Action of the second	E, = 6 McV		EJ=8McV	
,	<u> </u>	hoton	Thotons Nett® Energy MeV		Photons Nett Energy MeV	Photons	Nett Bhergy MeV	*Protons	ons Nett		Photons Nett.
Prompt	Fission		3,45		3.09	Table of the second	1.04		0.26		A description of the second se
Fission	Product .	<u>'</u>	5,16		1.74		0,32		8		I
CAE'IUKE	CAPTURE GAMMAS:-		and dependent of the factory was before	and the separate sepa	n-velorita a de galacia de de casa de c	Andreas - William Control	er der "de ver" verfande sone under verden de sone de	the technic in the	TO THE TRANSPORT OF THE	•	A THE RESERVE THE PROPERTY OF
H, (in we	H, (in water)0.01099	60	1	1,115	0.11732		P. B	I	ŧ		ı
In stain	In stainless steel	1.0		en destributes (1.1 destributes (1.2 des	Principle of the special state	- Antoniosis (40.7.4.4.	under fin fe' get demertetet be ign.		Commission 1 or 4 20/4864 "Microstate", state, instituted	The contract of the contract o	M.) Thursday, and an array page of the day.
F.	0,09318	-	1	0.1	0.01597	0.24	0.07645	0.22	0,10512	0.5	0.31854
Ç	0,03076	0.37	9.726 0.16	0.16	8.4117E-3 ).12	3 0.12	0.01262	8.0	0.28389	69.0	0.14510
ĘN	0.02506			I	ı	0.14	0.01199	0,30	0.03846	0.72	0.12378
NP QN	0,00029		ı	ı	ı	0.54	5.155E-4	0.14	2.082E-4	1	ı
Si	0.00018		1	1.0	3.042E-4	2.29	1.3934E-4 0.4	0.4	3.742E-4	0.16	1.947E-4
TOTAL(MeV)	eV)		8,61973	73	4.97196	ACOM	1,46297	The contract of the contract o	0.68814		0.58761
* Taken	Taken at T=300°C applying 1/v	°C appl	Ying 1/	8	rrection. (	X) Nett	$\bigotimes$ Nett Energy= $\binom{V_X}{V_{\text{fue}}}$ *	x fue]*(	Eax ) * F	E. / * Totons	* E / * \perior fission;
				* <u>*</u>	material,	) (from	(x=material) (from p.116,ref(26))	£ (26)),			<b>)</b>

(x=material) (from p.116,ref(26)),

# A 7.1 EVALUATION OF MOLERATOR TIME CONSTANT $(\tau_m)$

Heat balance for a fuel rod channel gives :
leat added) = (heat supplied to cowlant) - (heat carried away

flowing coolant).

r) 
$$m^{C}_{p} \frac{d T_{ac}}{dt} = A h_{c} (T_{cl} - T_{ac}) + \hbar (T_{i} - T_{ac}) \dots Eqn(1)$$

where,  $T_i$  ,  $T_{ac}$  = coolant inlet/average temprs. in core  $T_{cl} = {}^{C}ladding \ outer \ tempr.$ 

m = coolant flow rate

minating T<sub>cl</sub> in Eqn(1) by substituting

$$T_{cl} = \frac{h_f T_{af} + h_c T_{ac}}{h_f + h_c}$$
 got by Steacy-state

t transfer between fuel & coolant, where  $h_{f}$ ,  $T_{af}$  are fuel transfer coefficient and average tempr. given by Eqn(7.17); obtain:-

$$\frac{d T_{ac}}{dt} = \frac{A h_{c}^{2}}{(h_{e} + h_{f})mC_{p}} (T_{af} - T_{ac}) - \frac{\dot{m}}{m} (T_{ac} - T_{i}) .. Eqn(2)$$

e moderator time constant is the coefficient of its differential

$$_{\rm m} = (Ah_{\rm C}^2/(h_{\rm C} + h_{\rm E}) mC_{\rm p} + m/m)^{-1}$$
... Eqn(3)

evaluated from Eqn(2) by putting  $\frac{dT_{ac}}{dt} = 0$ 

r Steady State condition). We obtain :-

the same of the first terms of the second second

$$h_{C} = \frac{1 + \sqrt{1 + 4DH_{f}}}{D}$$
 ..... Eqn (4)

where, 
$$D = A \cdot (T_{af}^{-T}_{ac}) / m C_p (T_{ac}^{-T}_{i})$$
;

since all terms in Eqn(3) are known,  $\tau_m$  is evaluated. As temperatures change with load variations,  $\tau_m$  varies with load variations as well .

\* \* \* \*